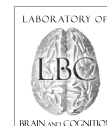


# Multi-echo EPI for task-based and resting-state fMRI

Javier González-Castillo

Section on Functional Imaging Methods, NIMH, NIH

July 2018, National Institutes of Health, Bethesda, MD



## ❖ WHAT IS MULTI-ECHO (ME) FMRI

## ❖ BASIC OPERATIONS WITH ME DATA

- Compute static  $S_0$  and  $T_2^*$  Maps
- Compute voxel-wise time-series of  $S_0$  (Non-BOLD) and  $T_2^*$  (BOLD)
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- Echo Time Dependence Analysis

## ❖ ADVANCE AUTOMATIC DENOISING WITH ME-ICA

- ME-ICA Pipeline
- ME-ICA Outputs
- ME-ICA Web Reporting Tool

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NeuroImage 154 (2017) 59–80



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NeuroImage

journal homepage: [www.elsevier.com/locate/neuroimage](http://www.elsevier.com/locate/neuroimage)



Multi-echo fMRI: A review of applications in fMRI denoising and analysis of BOLD signals



Prantik Kundu<sup>a,\*</sup>, Valerie Voon<sup>b</sup>, Priti Balchandani<sup>a</sup>, Michael V. Lombardo<sup>c</sup>, Benedikt A. Poser<sup>d</sup>, Peter A. Bandettini<sup>e</sup>

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<sup>b</sup> Behavioral and Clinical Neuroscience Institute, University of Cambridge, Cambridge, UK

<sup>c</sup> Department of Psychology and Center for Applied Neuroscience, University of Cyprus, Nicosia, Cyprus

<sup>d</sup> Department of Cognitive Neuroscience, Maastricht University, Maastricht, NL, The Netherlands

<sup>e</sup> Section on Functional Imaging Methods, National Institute of Mental Health, Bethesda, MD, USA

Intro to ME Signal Model  
+ ME-ICA Denoising

2018 IEEE 15th International Symposium on Biomedical Imaging (ISBI 2018)  
April 4-7, 2018, Washington, D.C., USA

## A TEMPORAL DECONVOLUTION ALGORITHM FOR MULTIECHO FUNCTIONAL MRI

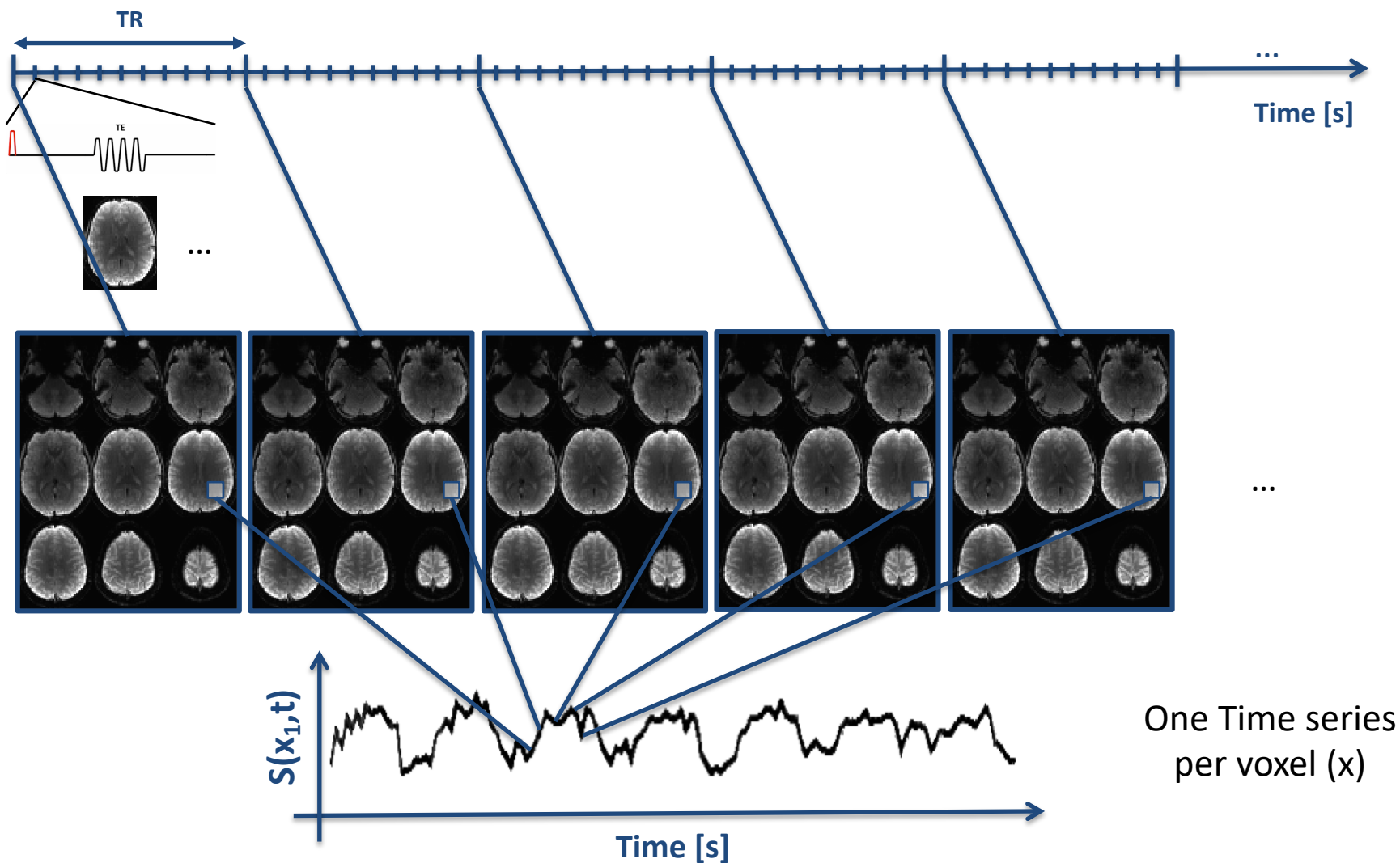
César Caballero Gaudes<sup>1</sup>, Peter A. Bandettini<sup>2,3</sup>, Javier Gonzalez-Castillo<sup>2</sup>

<sup>1</sup>Basque Center on Cognition, Brain and Language, San Sebastian, Spain

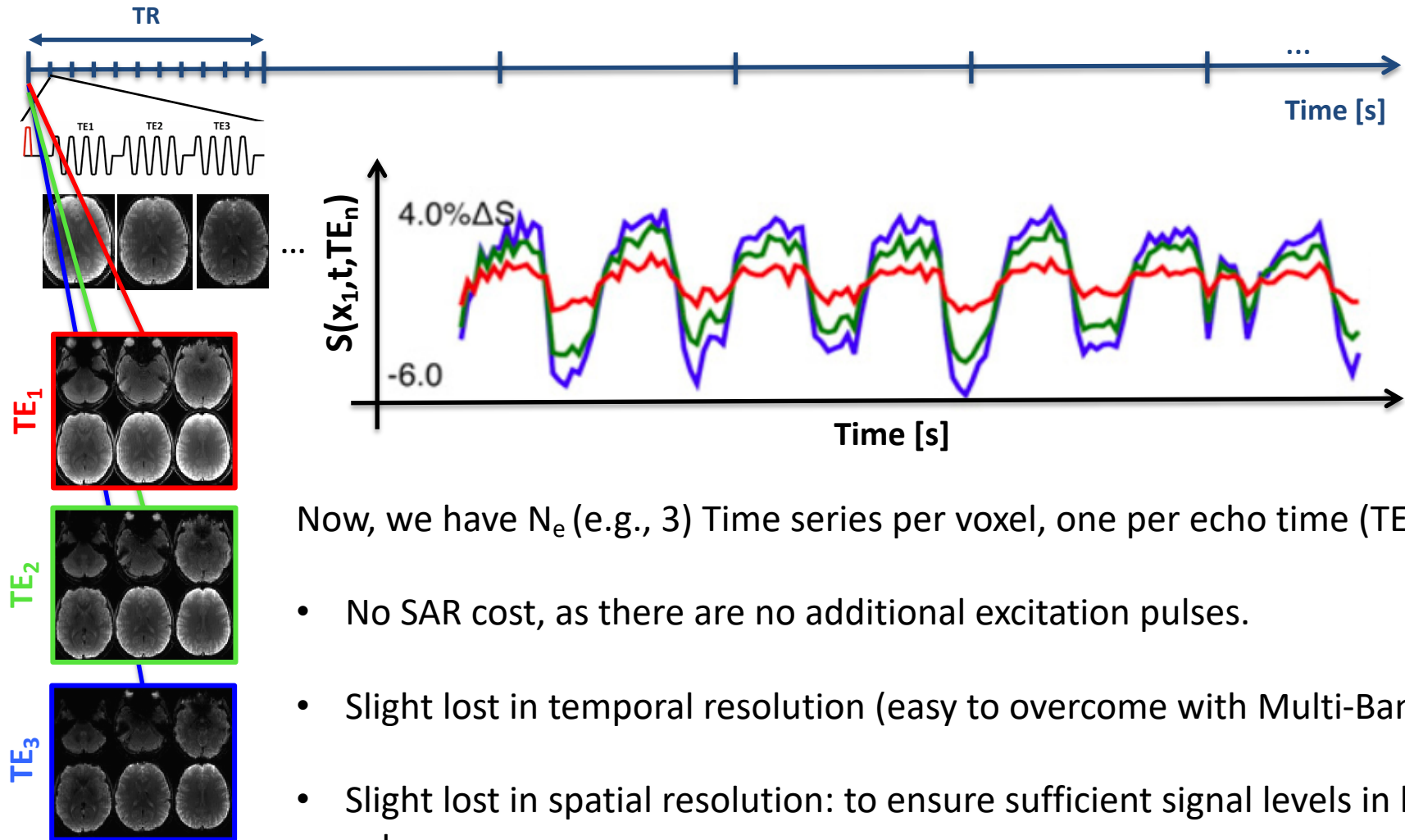
<sup>2</sup>Section on Functional Imaging Methods, NIMH, NIH, Bethesda, MD, USA

<sup>3</sup>Functional MRI Core, NIH, Bethesda, MD, USA

ME Formulation for fMRI  
Deconvolution of Sparse Events

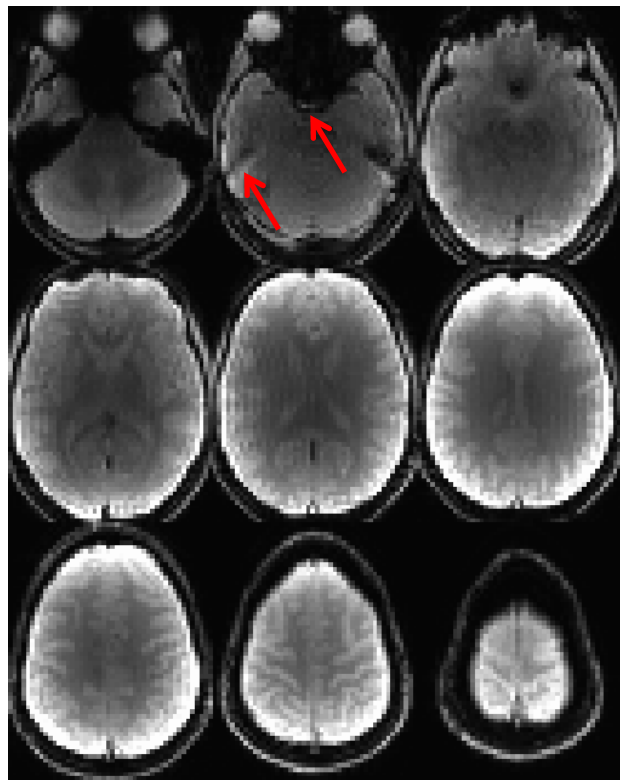
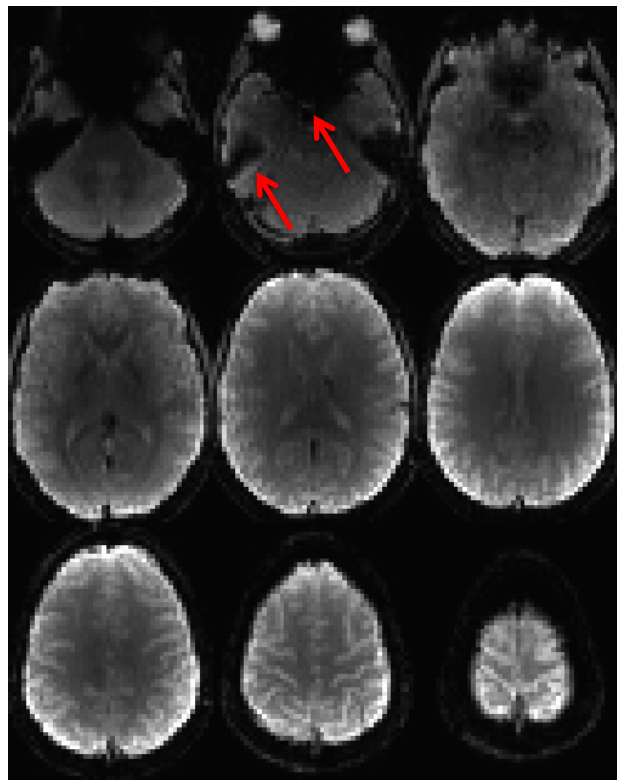
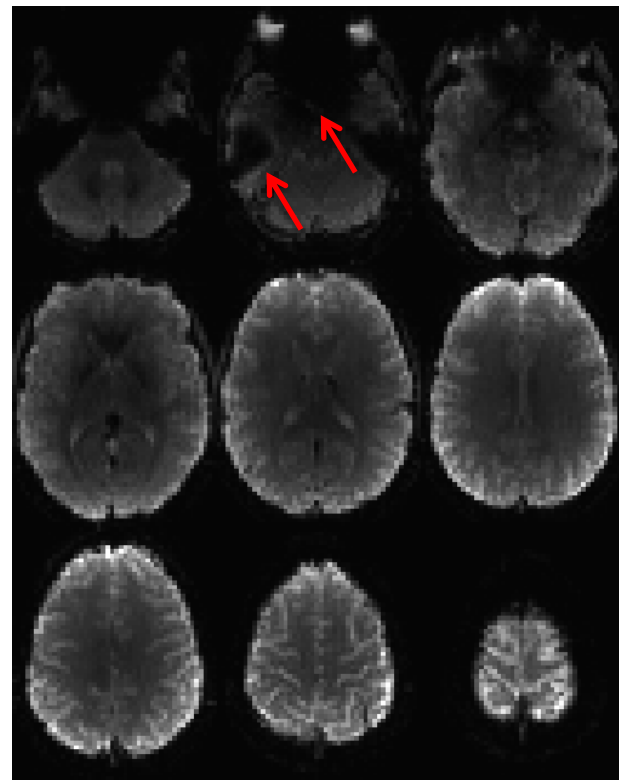






Now, we have  $N_e$  (e.g., 3) Time series per voxel, one per echo time ( $TE_n$ ):

- No SAR cost, as there are no additional excitation pulses.
- Slight lost in temporal resolution (easy to overcome with Multi-Band).
- Slight lost in spatial resolution: to ensure sufficient signal levels in last echo.

$TE_1$  $TE_2$  $TE_3$ 

16

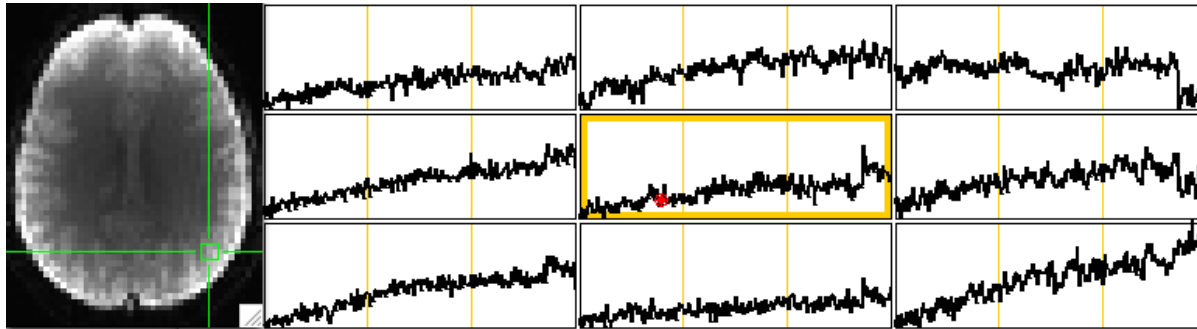
907

16

907

16

907



Signal in voxel  $x$ , at time point  $t$ , measured at echo time  $TE$

$$S(x, t, TE) = \underbrace{S_o(x, t)}_{\text{Captures local fluctuations due to T1 changes (e.g., inflow) and HW instabilities}} \underbrace{e^{-R_2^*(x, t) \cdot TE}}_{\text{Captures local fluctuations in field inhomogeneity (including BOLD)}} + \text{Noise}$$

Captures local fluctuations due to T1 changes (e.g., inflow) and HW instabilities

Captures local fluctuations in field inhomogeneity (including BOLD)

$$S_o(x, t) = \overline{S_o(x)} + \Delta S_o(x, t)$$

$$\Delta S_o(x, t) \ll \overline{S_o(x)}, \forall x$$

$$R_2^*(x, t) = \overline{R_2^*(x)} + \Delta R_2^*(x, t)$$

$$\Delta R_2^*(x, t) \ll \overline{R_2^*(x)}, \forall x$$

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$$S(x, t, TE) = S_o(x, t) e^{-R_2^*(x, t) TE}$$

$$S_o(x, t) = \overline{S_o(x)} + \Delta S_o(x, t)$$

$$R_2^*(x, t) = \overline{R_2^*(x)} + \Delta R_2^*(x, t)$$

By definition, the average across time of  $\Delta S_o(x, t)$  and  $\Delta R_2^*(x, t)$  are zero, and then it follows that the average signal across time for a given voxel (x) and echo time (TE) is:

$$\overline{S(x, TE)} = \overline{S_o(x)} \cdot e^{-\overline{R_2^*(x)} \cdot TE}$$



$$\log(\overline{S(x, TE)}) = \log(\overline{S_o(x)} \cdot e^{-\overline{R_2^*(x)} \cdot TE})$$

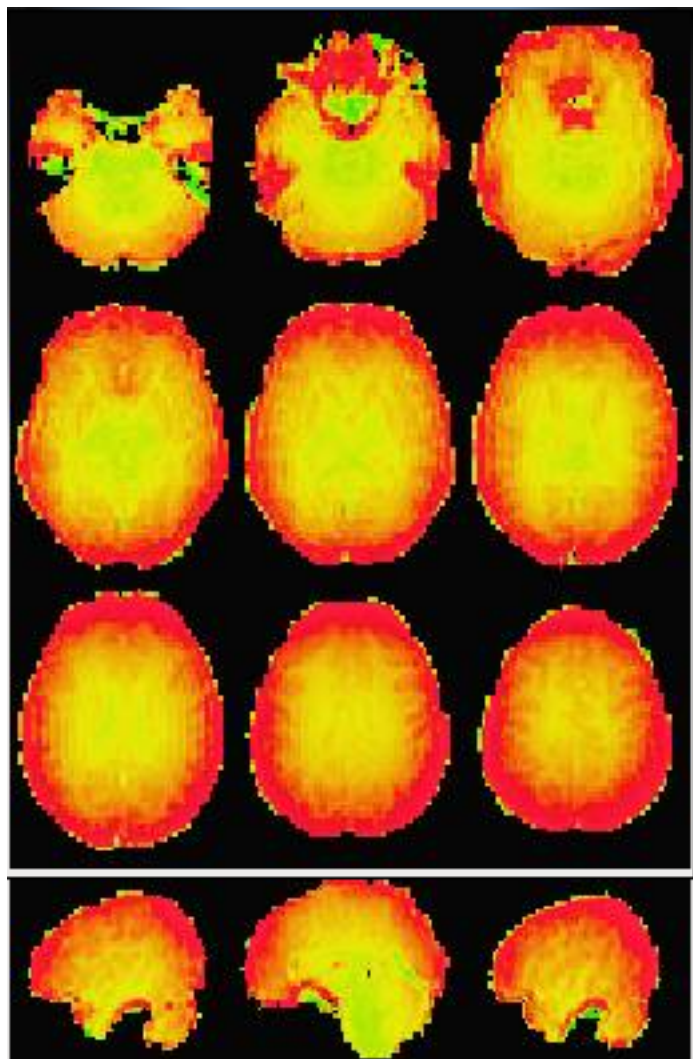


$$\log(\overline{S(x, TE)}) = -\overline{R_2^*(x)} \cdot TE + \log(\overline{S_o(x)})$$

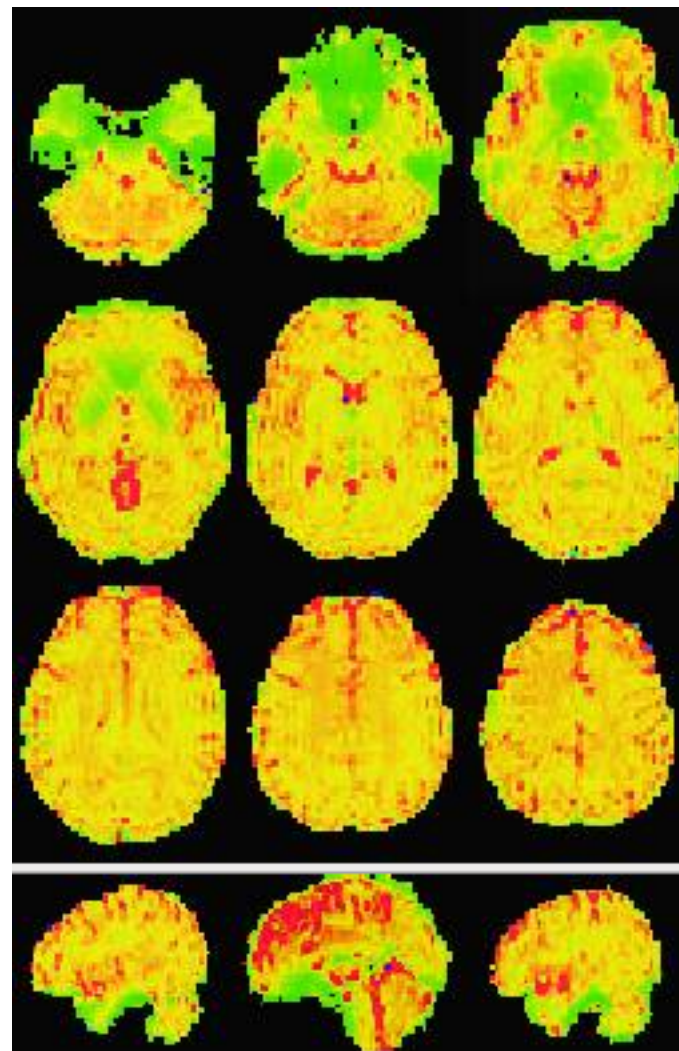
$$y(x, TE) = a(x) * TE + b(x)$$

Linear  
system of  
equations for  
3 echoes

$$\begin{cases} \log(\overline{S(x, TE_1)}) = -\overline{R_2^*(x)} \cdot TE_1 + \log(\overline{S_o(x)}) \\ \log(\overline{S(x, TE_2)}) = -\overline{R_2^*(x)} \cdot TE_2 + \log(\overline{S_o(x)}) \\ \log(\overline{S(x, TE_3)}) = -\overline{R_2^*(x)} \cdot TE_3 + \log(\overline{S_o(x)}) \end{cases}$$



Static S<sub>0</sub> Map (s0v.nii)



Static T<sub>2</sub><sup>\*</sup> Map (t2sv.nii)

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$$S(x, t, TE) = S_o(x, t) e^{-R_2^*(x, t) TE}$$

$$S_o(x, t) = \overline{S_o(x)} + \Delta S_o(x, t)$$

$$R_2^*(x, t) = \overline{R_2^*(x)} + \Delta R_2^*(x, t)$$

$$\overline{S(x, TE)} = \overline{S_o(x)} \cdot e^{-\overline{R_2^*(x)} TE}$$

$$S(x, t, TE) = \left[ \overline{S_o(x)} + \Delta S_o(x, t) \right] \cdot e^{\left[ -\overline{R_2^*(x)} + \Delta R_2^*(x, t) \right] TE} \quad (1)$$

$$S(x, t, TE) = \overline{S(x, TE)} \left[ 1 + \frac{\Delta S_o(x, t)}{\overline{S_o(x)}} \right] \cdot e^{-\Delta R_2^*(x, t) TE} \quad (2)$$

Using a first order Taylor expansion for the exponential term:  $e^{-\Delta R_2^*(x, t) TE} \approx (1 - \Delta R_2^*(x, t) \cdot TE)$

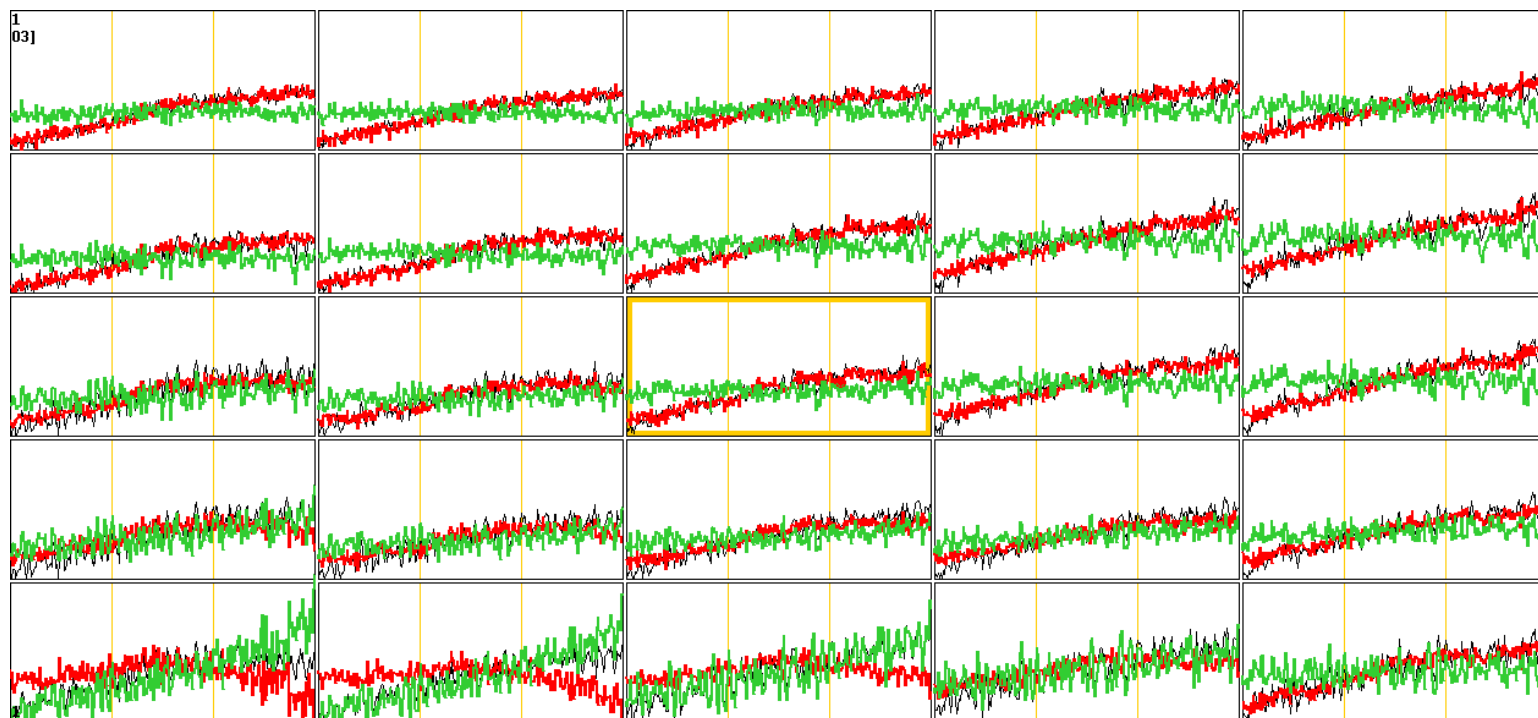
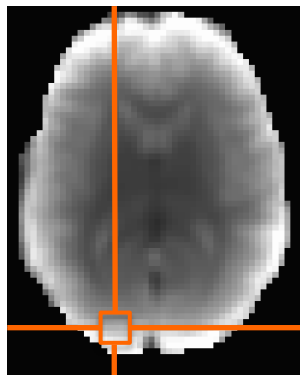
$$S(x, t, TE) \approx \overline{S(x, TE)} \left[ 1 - \Delta R_2^*(x, t) \cdot TE + \frac{\Delta S_o(x, t)}{\overline{S_o(x)}} - \frac{\Delta R_2^*(x, t) \cdot TE \cdot \Delta S_o(x, t)}{\overline{S_o(x)}} \right] \quad (3)$$

$$S(x, t, TE) \approx \overline{S(x, TE)} \left[ 1 - \Delta R_2^*(x, t) \cdot TE + \frac{\Delta S_o(x, t)}{\overline{S_o(x)}} \right] \quad (4)$$

$$\left. \begin{array}{l} \Delta \rho(x, t) = \Delta S_o(x, t) / \overline{S_o(x)} \\ \Delta \kappa(x, t) = \Delta R_2^*(x, t) \cdot \overline{TE} \end{array} \right\} \rightarrow S(x, t, TE) \approx \overline{S(x, TE)} \cdot \left[ 1 + \Delta \rho(x, t) - \frac{TE}{\overline{TE}} \Delta \kappa(x, t) \right] \quad (5)$$

$$S(x, t, TE) - \overline{S(x, TE)} \approx \overline{S(x, TE)} \left[ \Delta \rho(x, t) - \frac{TE}{\overline{TE}} \Delta \kappa(x, t) \right] \quad (6)$$

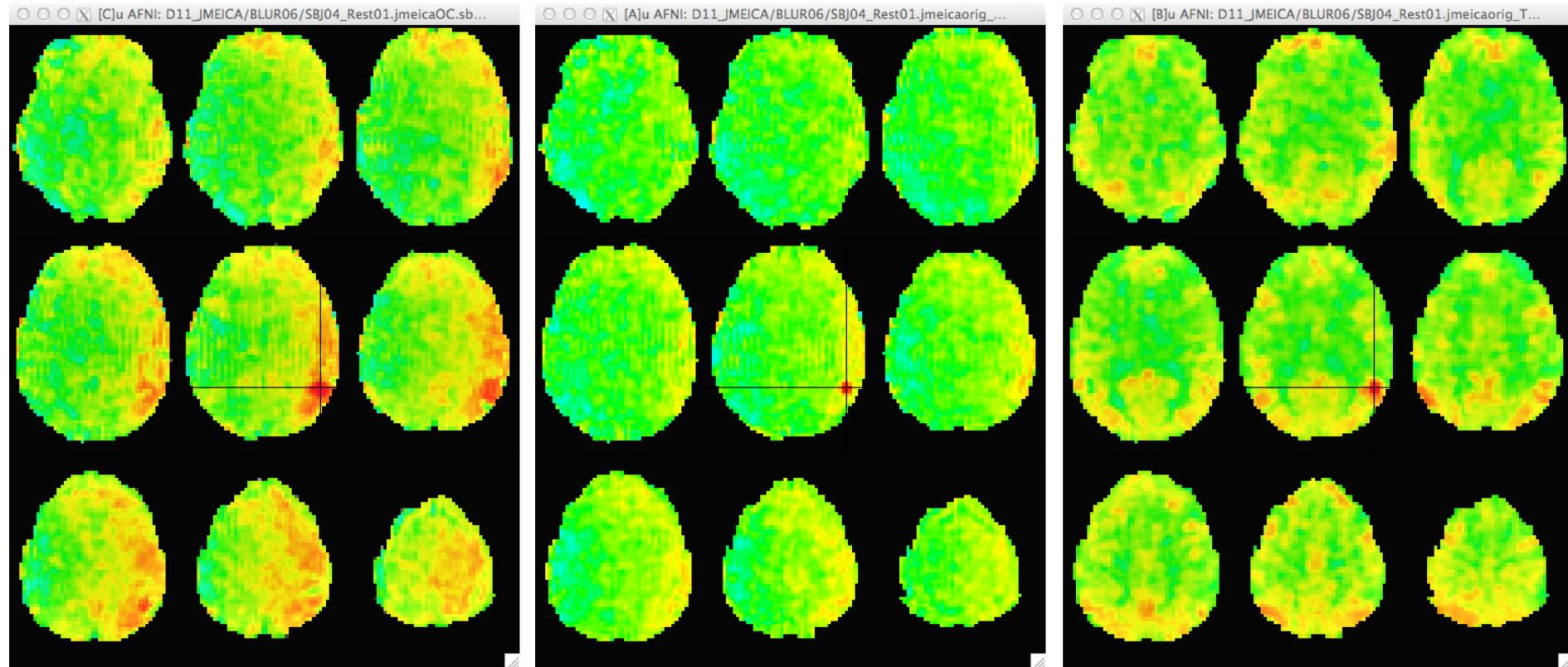




—  $S(x,t,TE_2)$

—  $\Delta S_0(x,t)$

—  $\Delta R_2^*(x,t)$



Raw Data

 $\Delta S_0$  $\Delta R_2^*$ 

Motion Correction & Smoothing (6mm)  
No Filtering | No Detrending

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We have  $N_e$  pseudo-concurrent measurements  $\rightarrow$  why not simply combine them to reduce uncorrelated white noise present in each individual measurement?

### 1. Simple Summation

$$\hat{S}(x,t) = \sum_{n=1}^N S(x,t,TE_n)$$

- Noisy data at longer echoes reduce the overall gain in sensitivity.

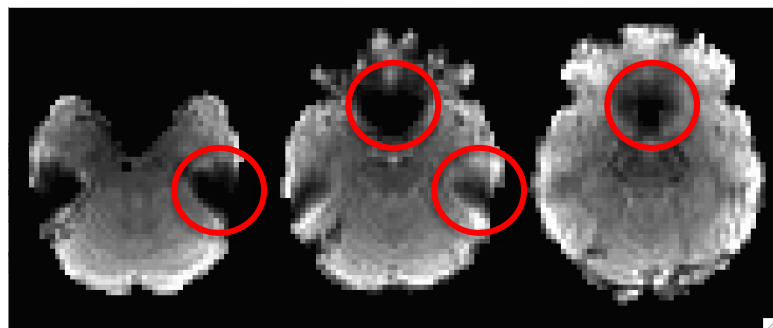
### 2. Weighted Summation

$$\hat{S}(x,t) = \sum_{n=1}^N S(x,t,TE_n) \cdot w_v(TE_n)$$

$$w_v(TE_n) = \frac{TE_n e^{-TE_n/T_{2,v}^*}}{\sum_n TE_n \cdot e^{-TE_n/T_{2,v}^*}}$$

- Helps to spatially maximize CNR and also to recover some signal level in regions affected by drop-out.

*Posse et al., MRM 1999*

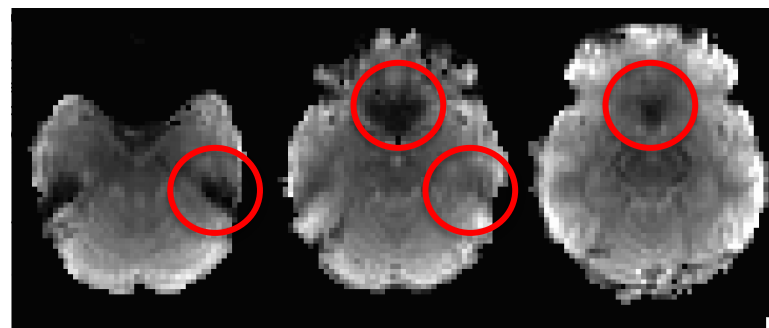


SINGLE ECHO

500



0



OPTIMALLY COMBINED

We have  $N_e$  pseudo-concurrent measurements, why not simply combine them to reduce uncorrelated white noise present in each individual measurement.

### 1. Simple Summation

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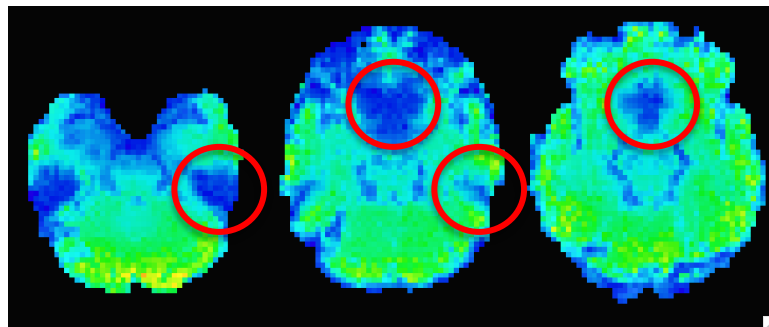
### 2. Weighted Summation

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$$w_v(TE_n) = \frac{TE_n e^{-TE_n/T_{2,v}^*}}{\sum_n TE_n \cdot e^{-TE_n/T_{2,v}^*}}$$

- Optimizes CNR compared to Single Echo.
- Helps to spatially maximize CNR, by helping recover some signal in regions with large drop-outs at regular single echo acquisitions.

*Posse et al., MRM 1999*

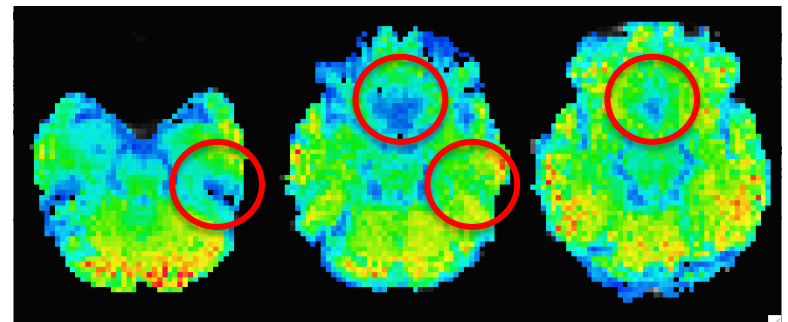


SINGLE ECHO

150



0



OPTIMALLY COMBINED

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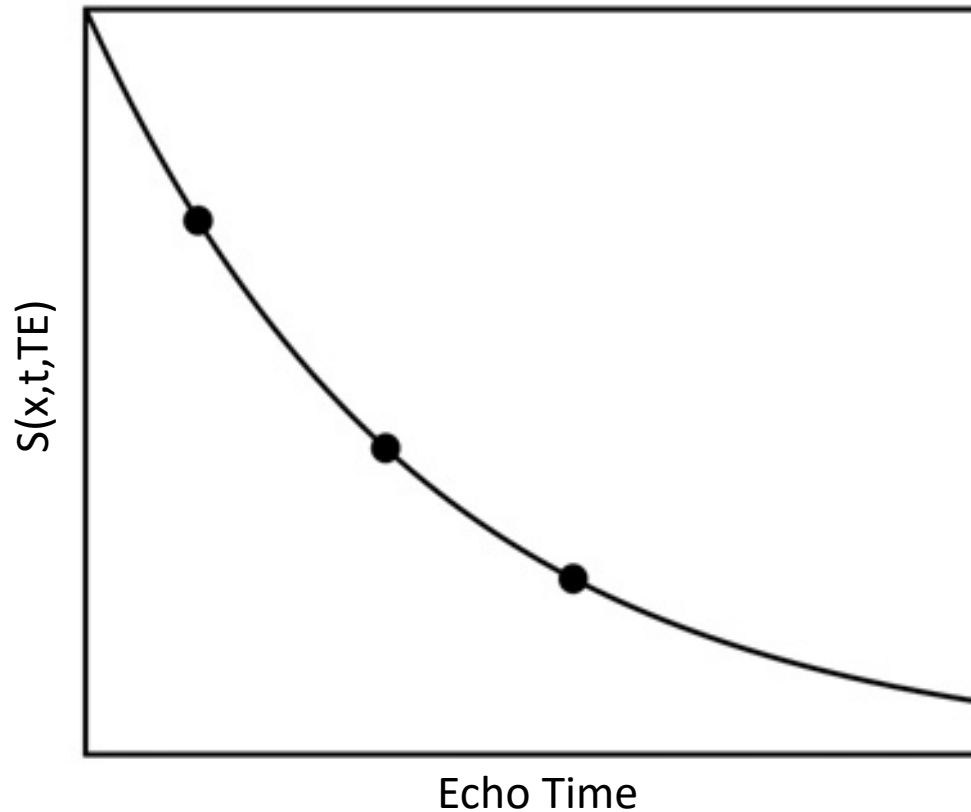
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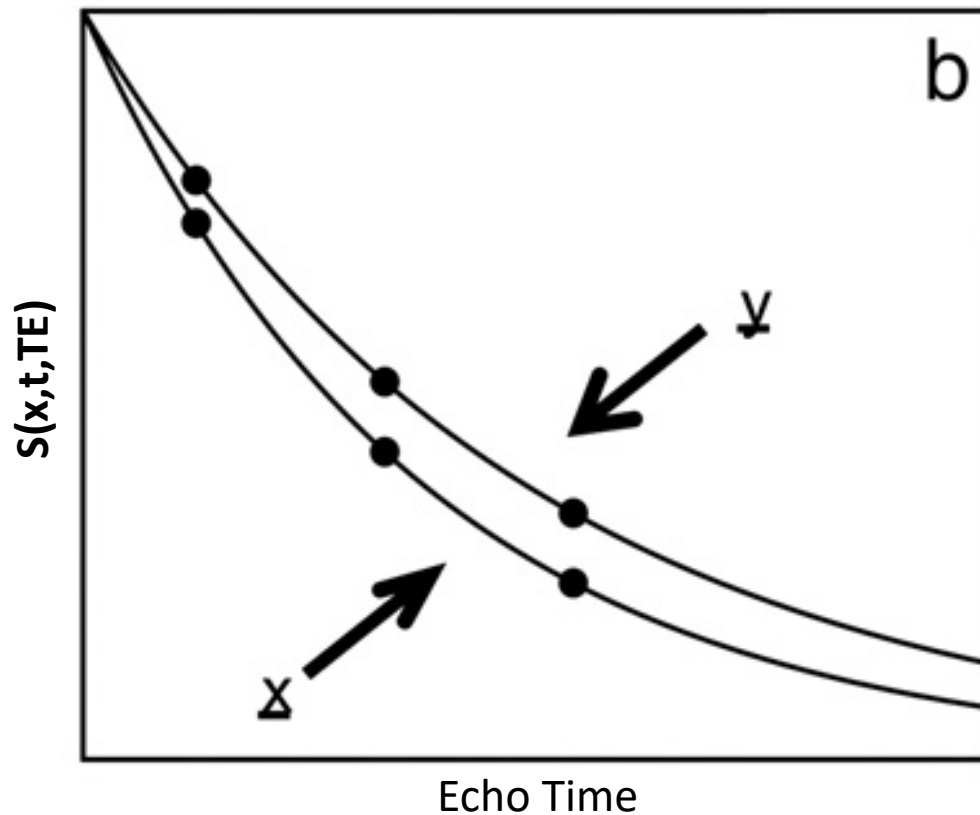
$$S(x,t,TE) = S_o(x,t)e^{-R_2^*(x,t)TE}$$

Let's assume that a given voxel (x) and time (t) ....  $S_o(x,t)=5000$  and  $T2^*(x,t)=30ms$



$$S(x,t,TE) = S_o(x,t) e^{-R_2^*(x,t) \cdot TE}$$

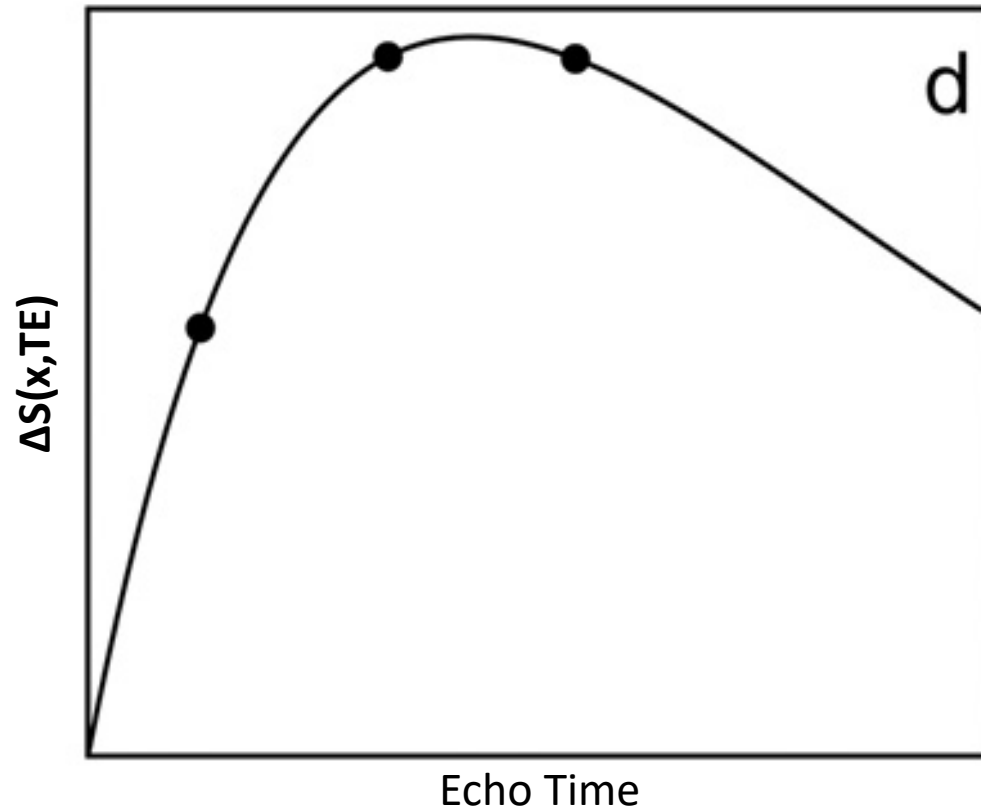
Let's assume now, that a local change in oxygenation happens ( $T_2^*$  effect)





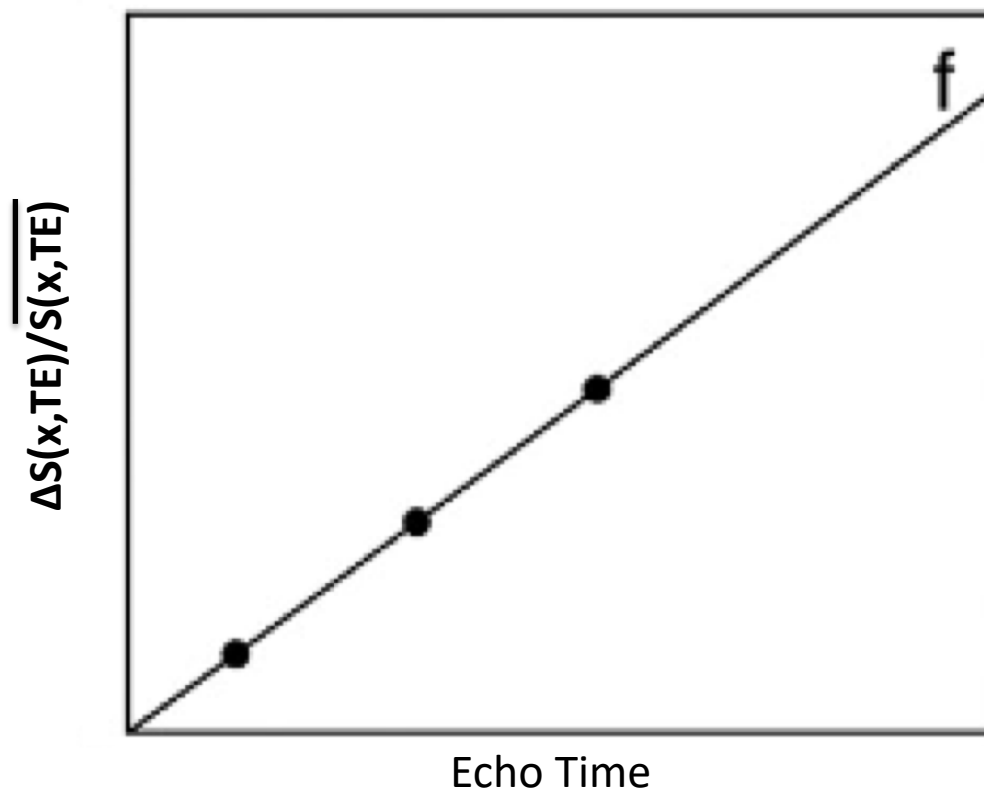
$$S(x, t, TE) = S_o(x, t) e^{-R_2^*(x, t) TE}$$

We could then use the difference between two curves to examine which is the optimal TE to maximize BOLD contrast



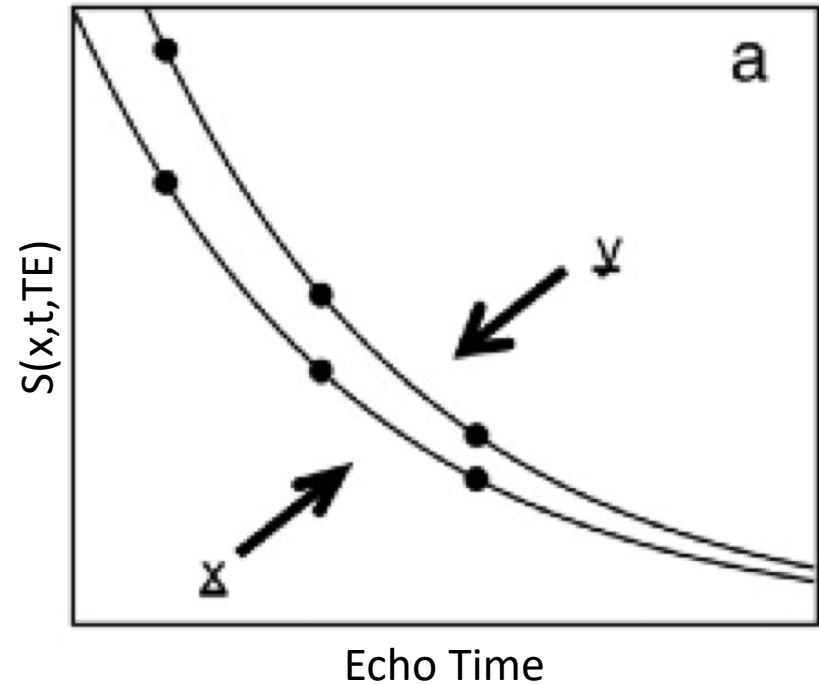
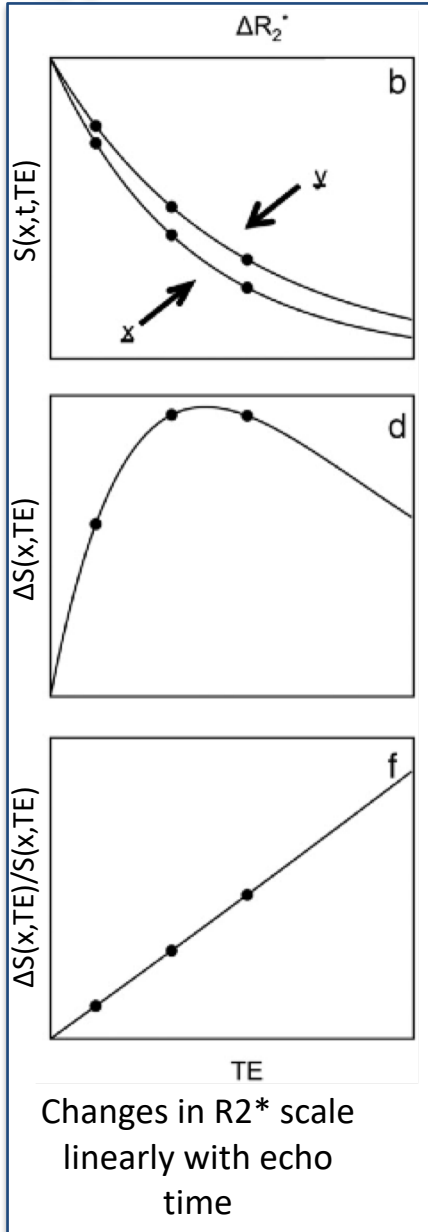
$$S(x, t, TE) = S_o(x, t) e^{-R_2^*(x, t) \cdot TE}$$

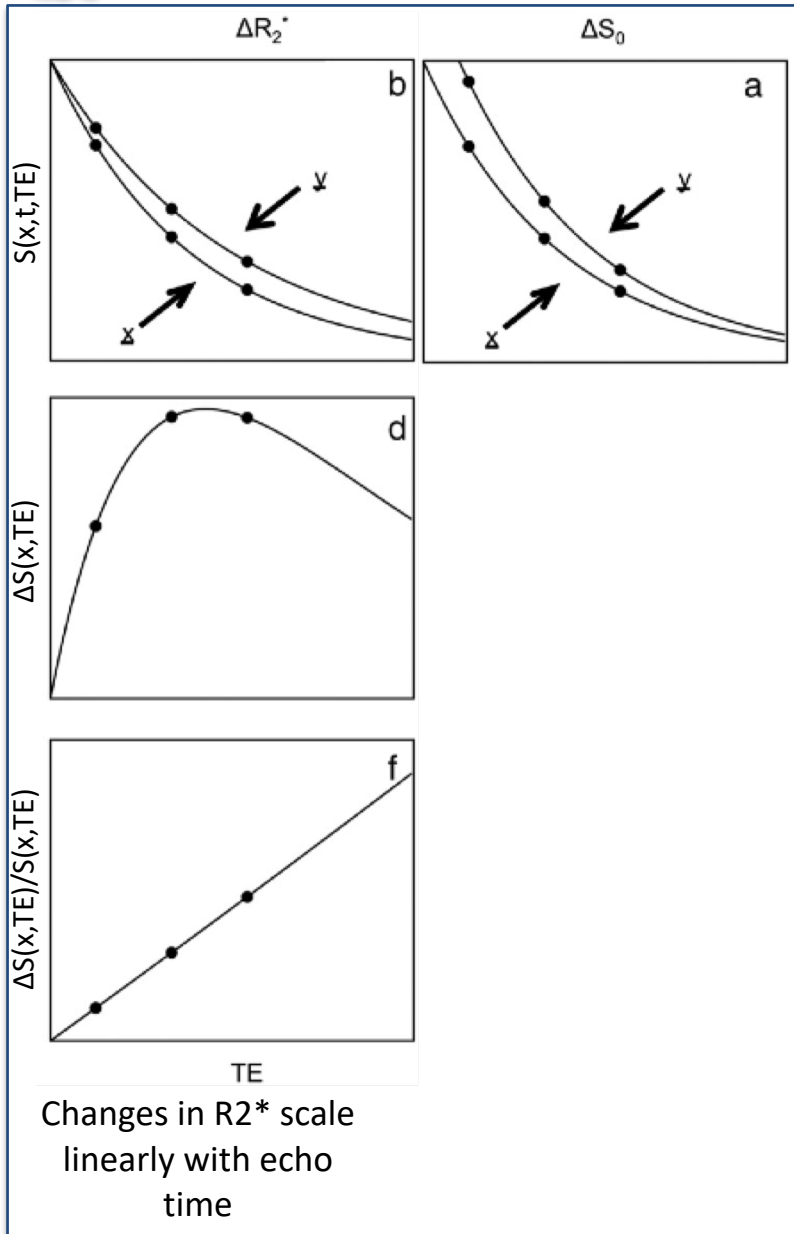
Most importantly for our discussion, for  $T_2^*$  signal changes, there is a linear relationship between echo time and measured signal (in terms of signal percent change)



$$S(x, t, TE) = S_o(x, t) e^{-R_2^*(x, t) \cdot TE}$$

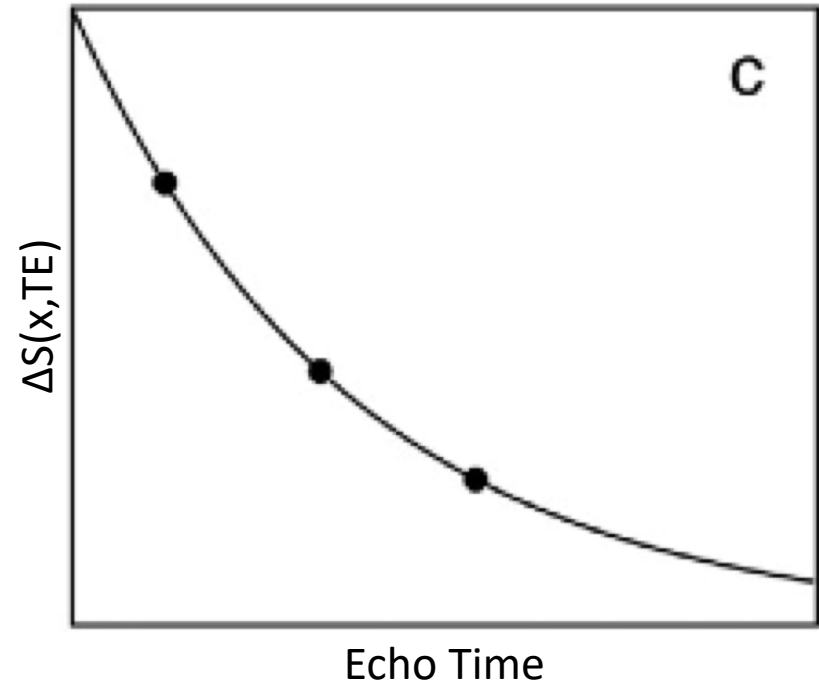
Let's now examine what happens when there is a change in  $S_o$  (T1 effect)

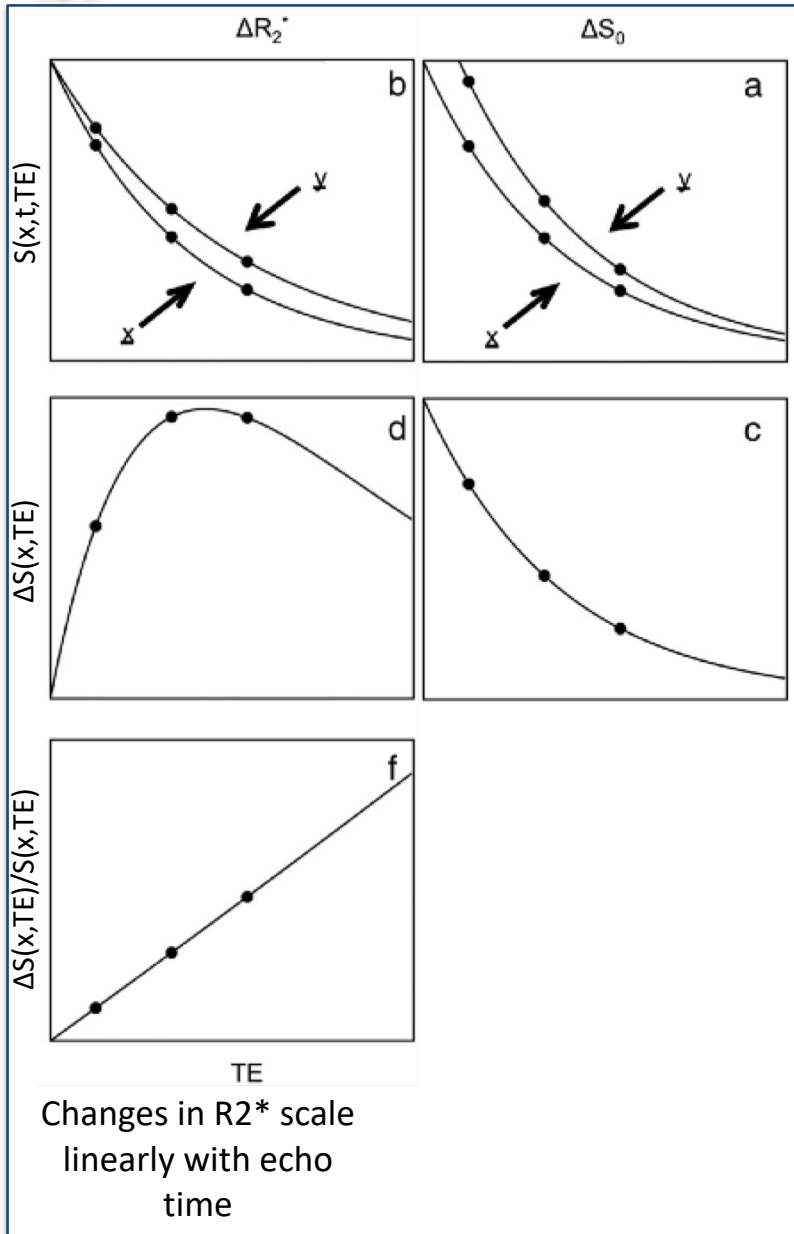




$$S(x,t,TE) = S_o(x,t)e^{-R_2^*(x,t)TE}$$

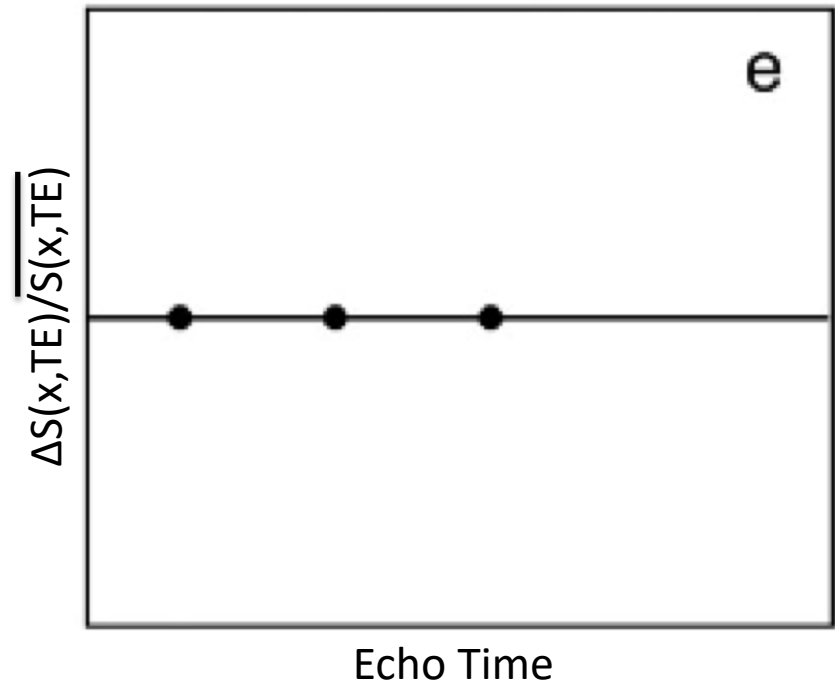
This time the difference between both curves looks very different

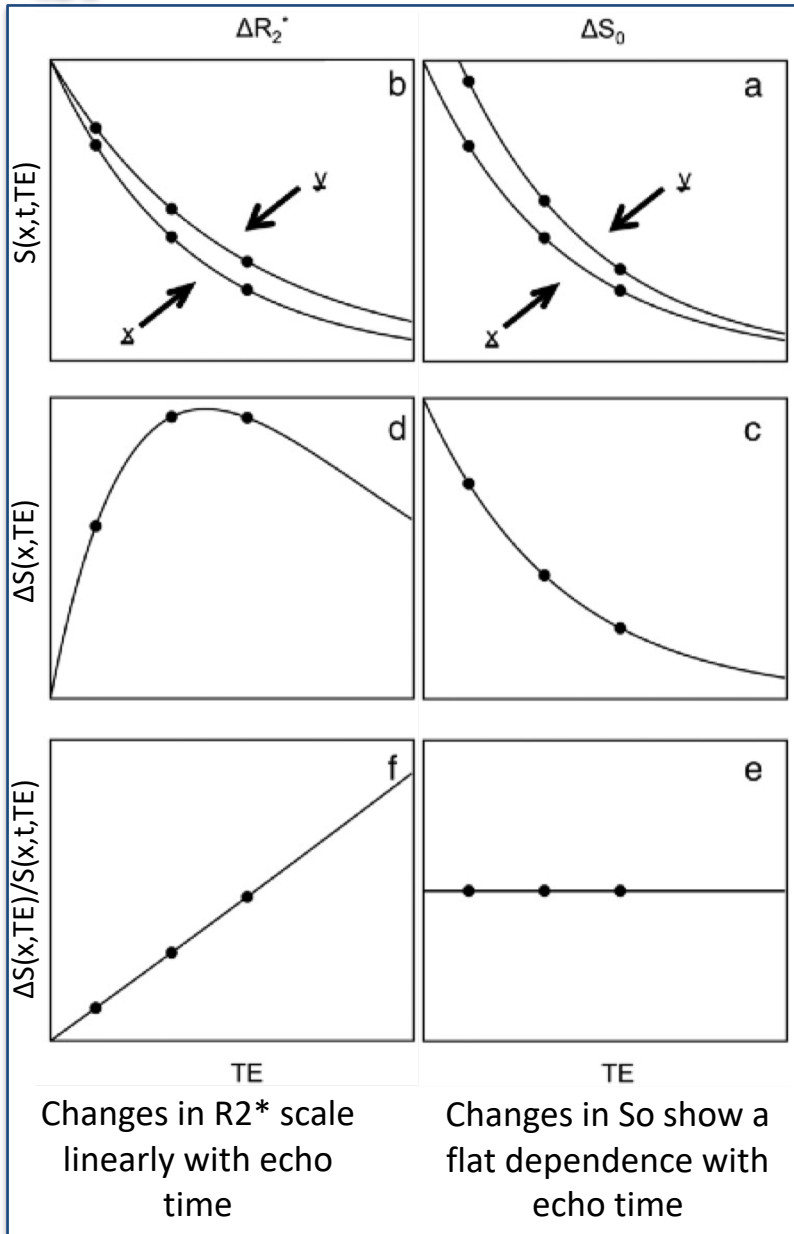




$$S(x,t,TE) = S_o(x,t)e^{-R_2^*(x,t) \cdot TE}$$

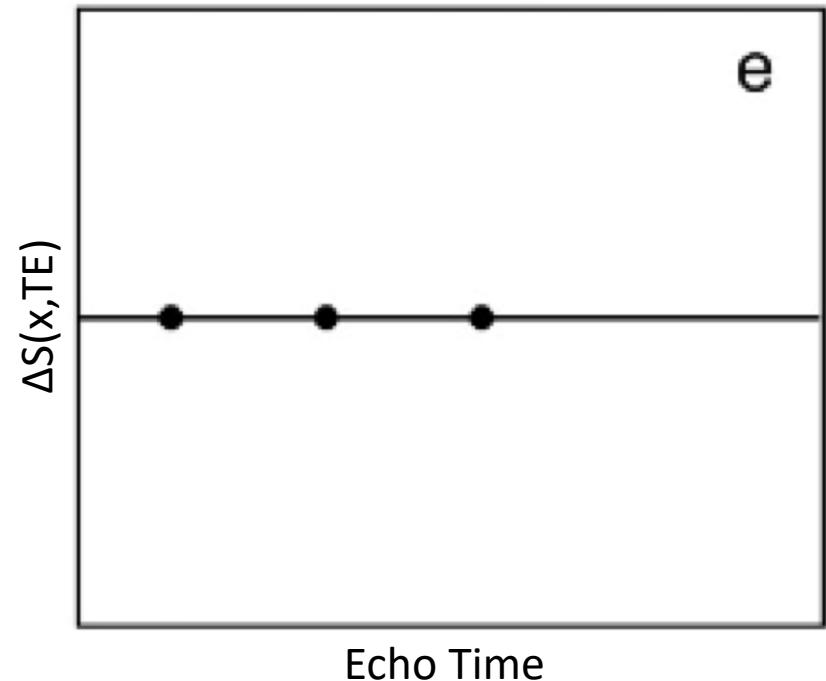
In term of signal percent change, changes in  $R_2^*$  So have a flat dependence with echo time



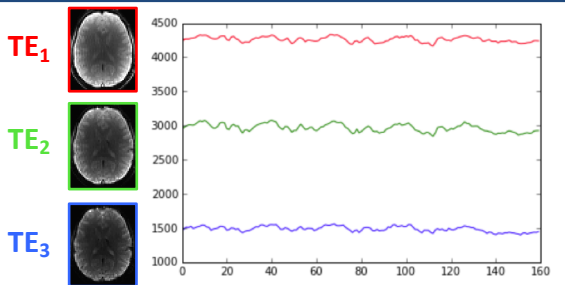


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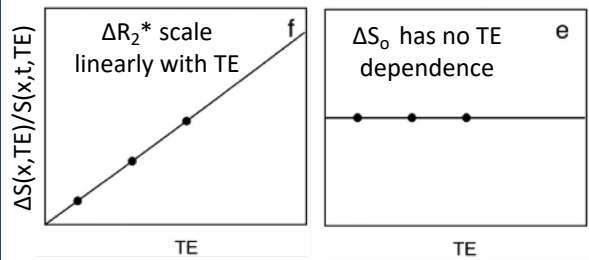
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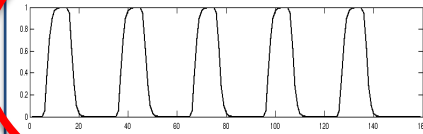
MULTI-ECHO DATASET



TE-DEPENDENCE MODEL

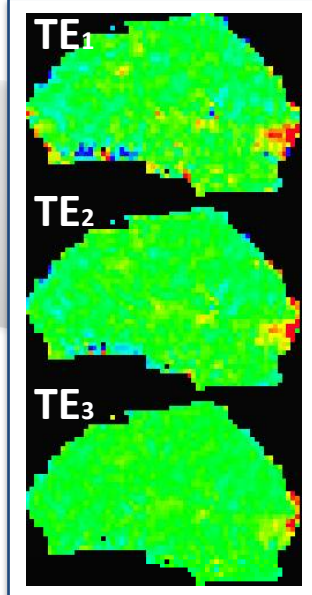


TIMESERIES OF INTEREST

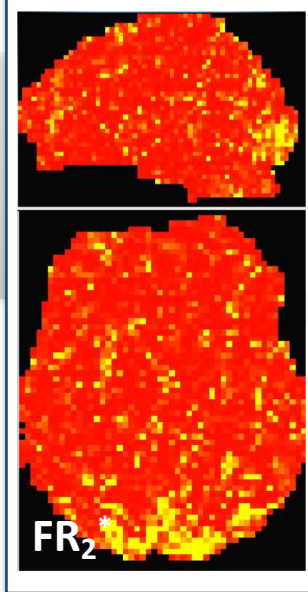


Task Paradigm

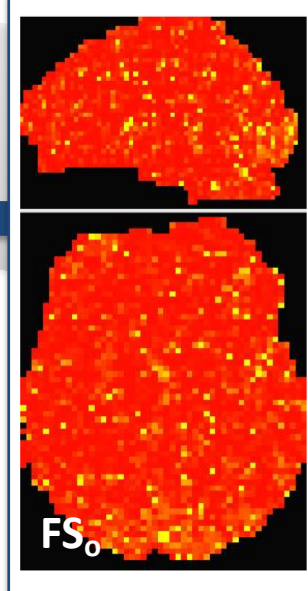
[1] Voxel-wise Fit against all TEs



[2] Voxel-wise Goodness of Fit to R2\* Model



[3] Voxel-wise Goodness of Fit to S0 Model



[4] Compute Avg. Metric for each model

$$\kappa = \frac{\sum_{AllVoxels} z_v^2 F_{v,R_2^*}}{\sum_{AllVoxels} z_v^2} = 98.41$$

$$\rho = \frac{\sum_{AllVoxels} z_v^2 F_{v,S_0}}{\sum_{AllVoxels} z_v^2} = 26.02$$

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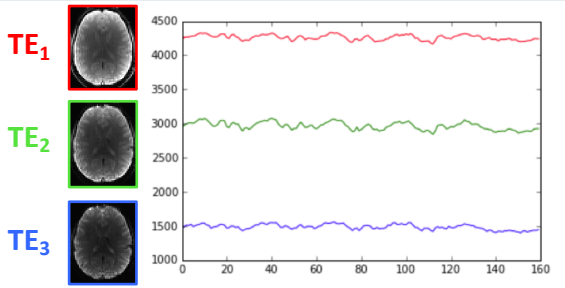
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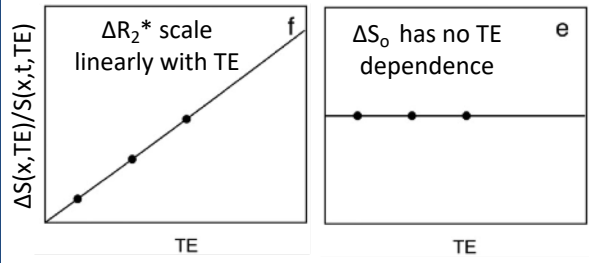
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MULTI-ECHO  
DATASET

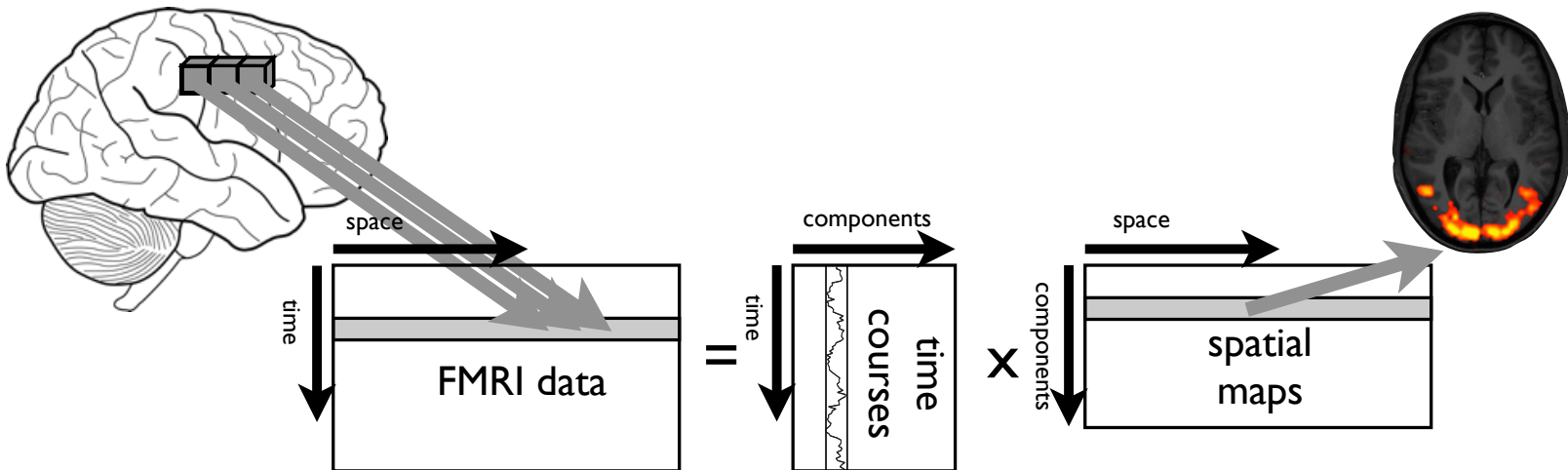


TE-DEPENDENCE  
MODEL



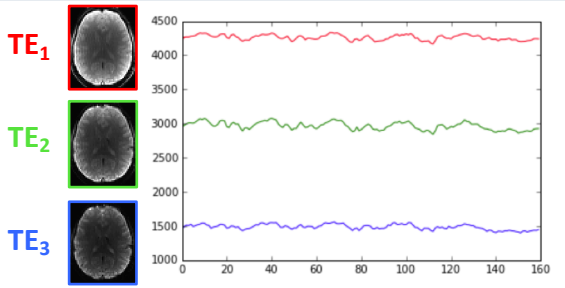
TIMESERIES OF INTEREST

ICA Representative  
Timeseries

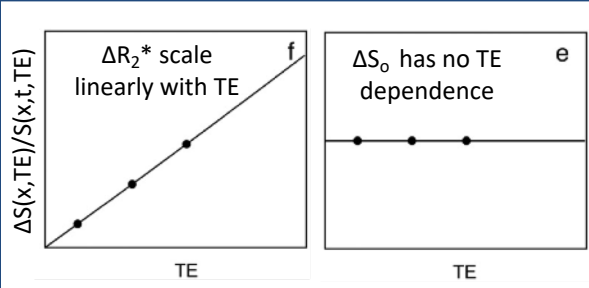


Data is represented as a 2D matrix and decomposed into factor matrices (or modes)

MULTI-ECHO  
DATASET



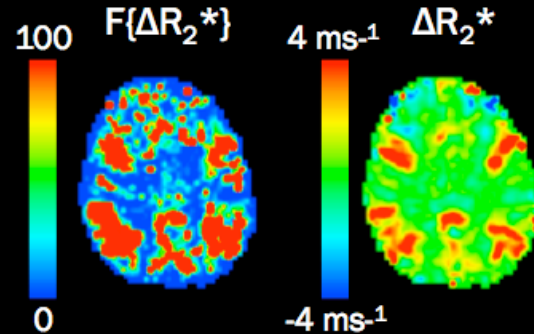
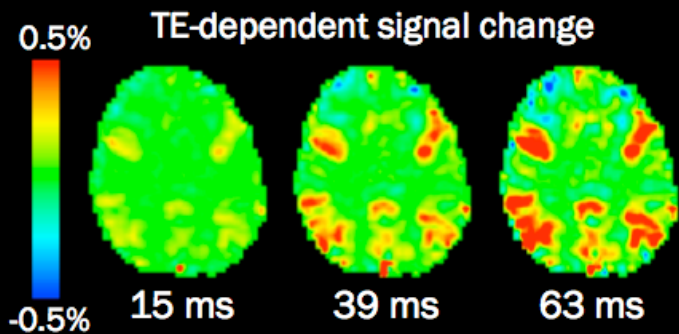
TE-DEPENDENCE  
MODEL



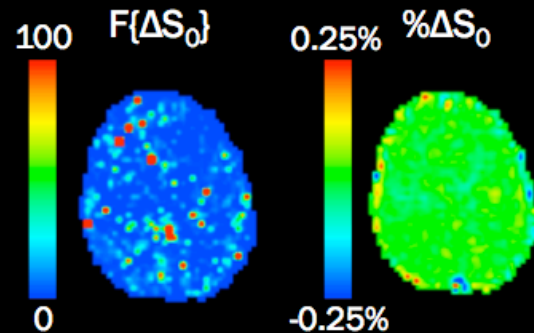
TIMESERIES OF INTEREST

ICA Representative  
Timeseries

(a) Functional Network Component



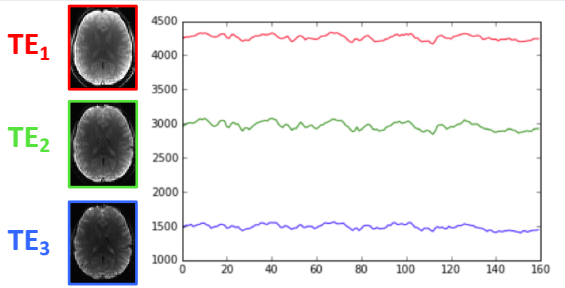
Component time course



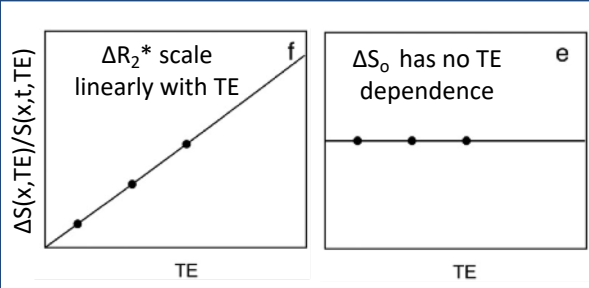
Kappa ( $\kappa$ ) = 210

Rho ( $\rho$ ) = 10

MULTI-ECHO  
DATASET



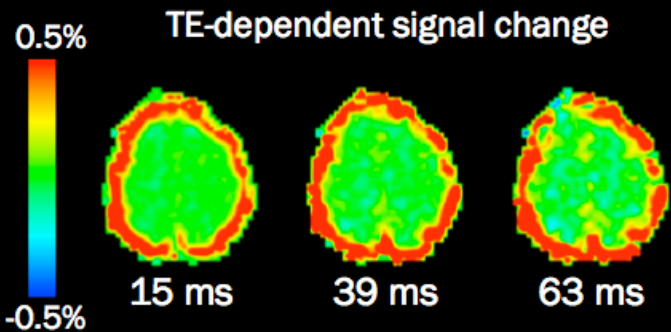
TE-DEPENDENCE  
MODEL



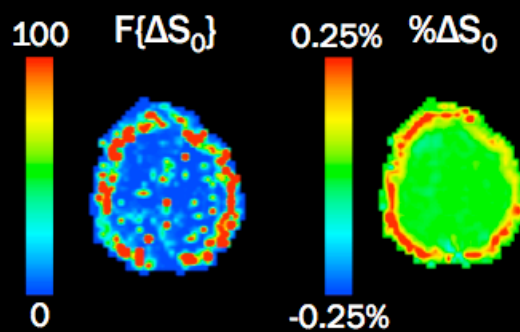
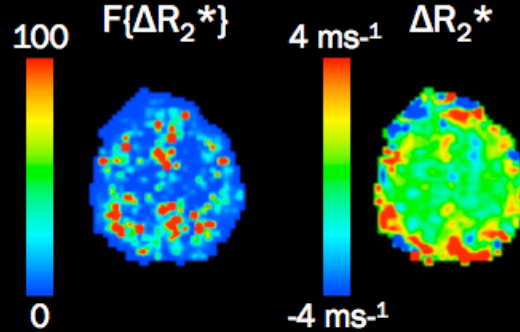
TIMESERIES OF INTEREST

ICA Representative  
Timeseries

## (b) Artifact Component



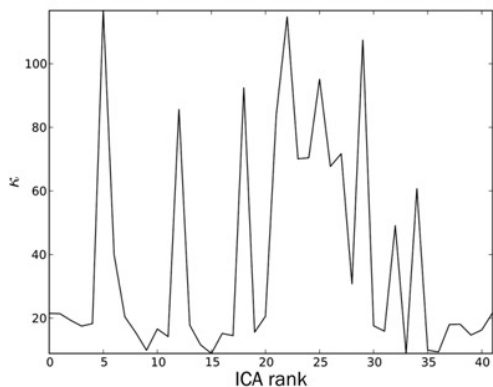
Component time course



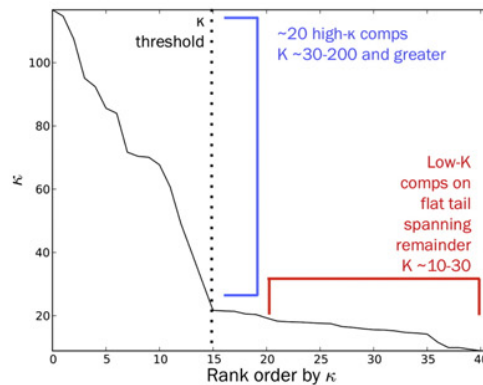
Kappa ( $\kappa$ ) = 32

Rho ( $\rho$ ) = 81

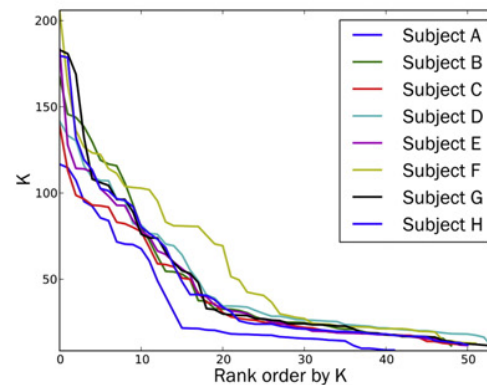
a  $\kappa$  vs. ICA rank



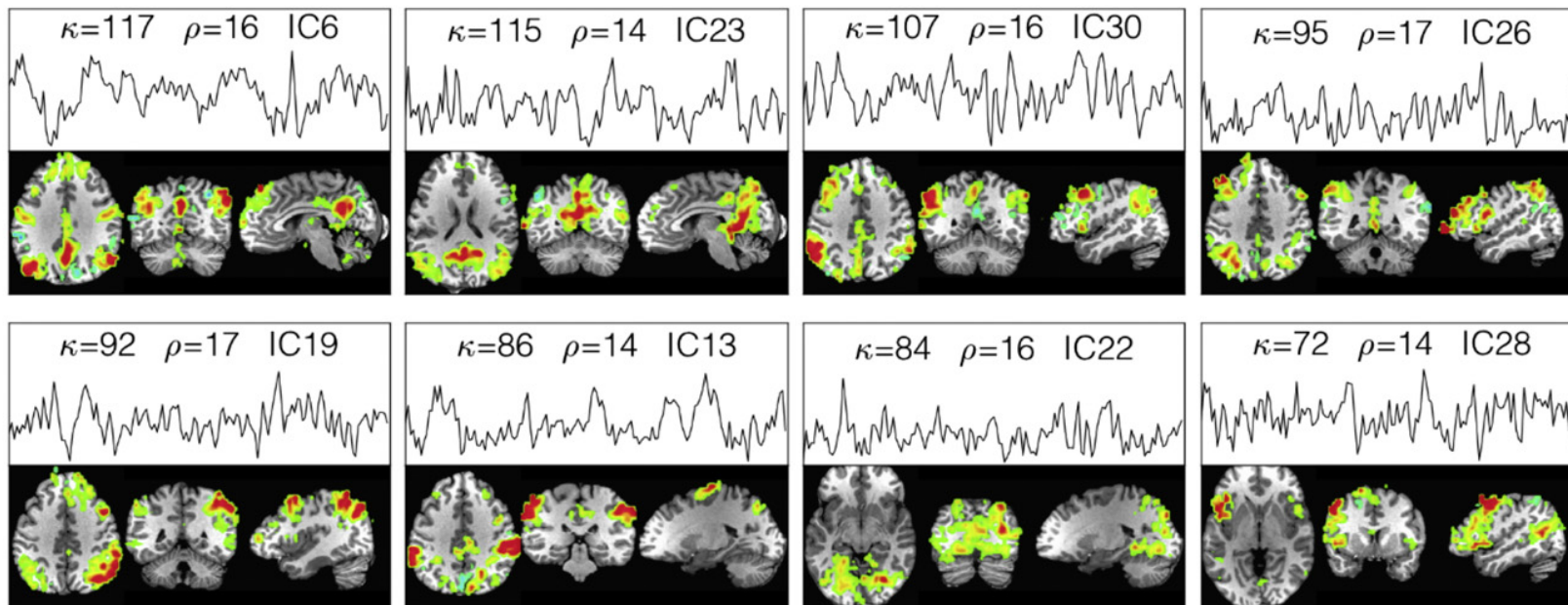
b  $\kappa$  spectrum



c  $\kappa$  spectra across subjects

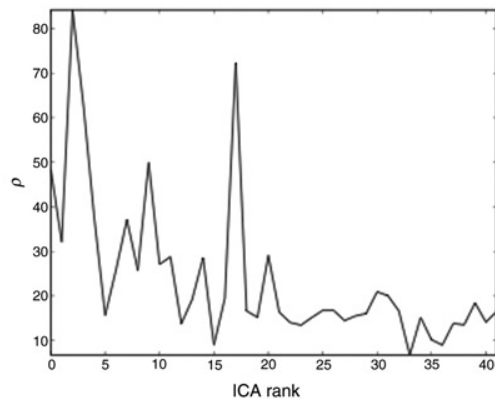


d  $\Delta R_2^*$  maps of top  $\kappa$  ranked components for a representative subject

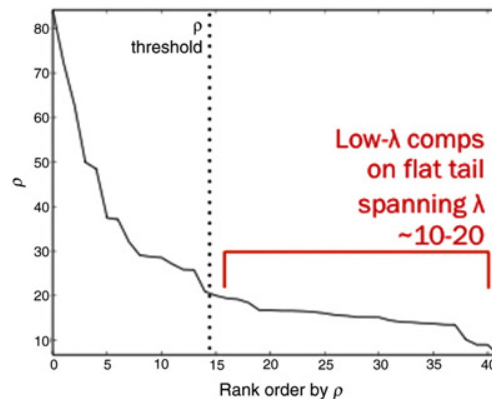




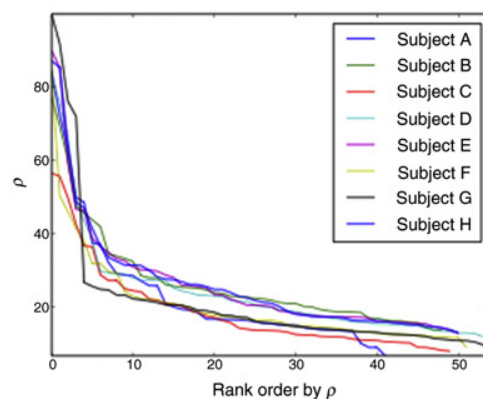
a  $\rho$  vs. ICA rank



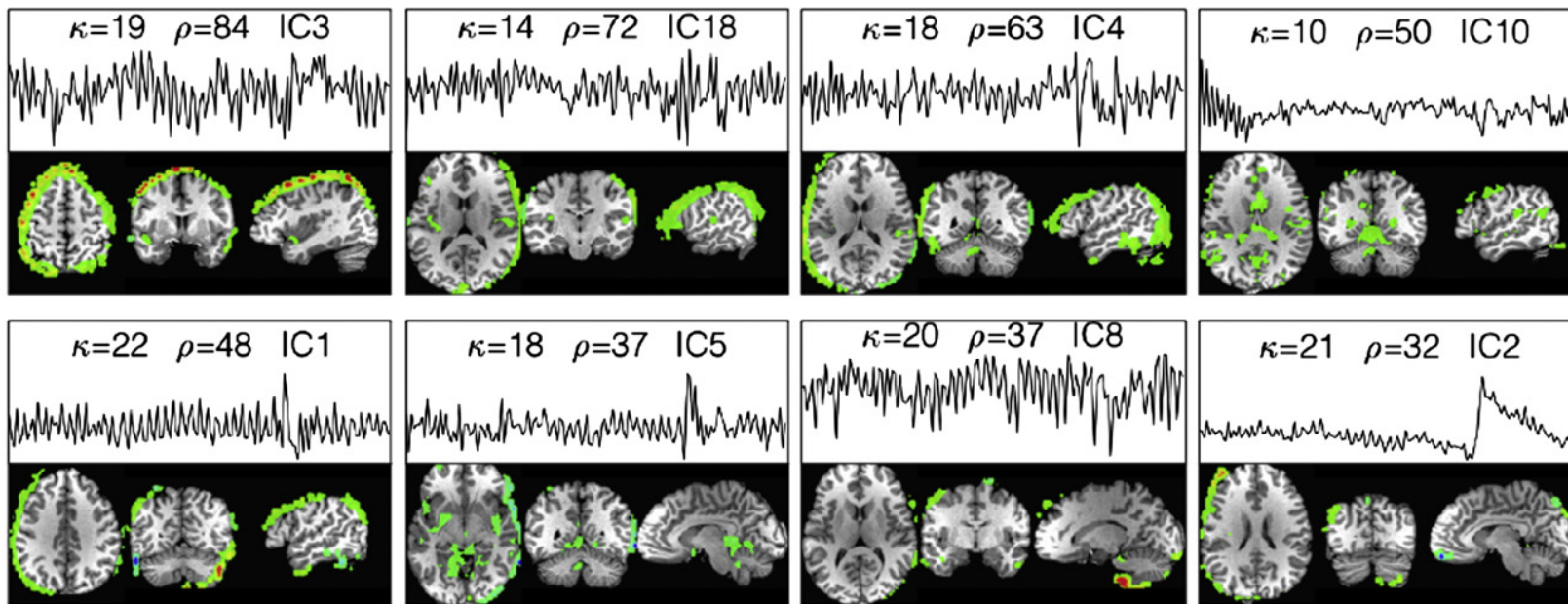
b  $\rho$ -spectrum

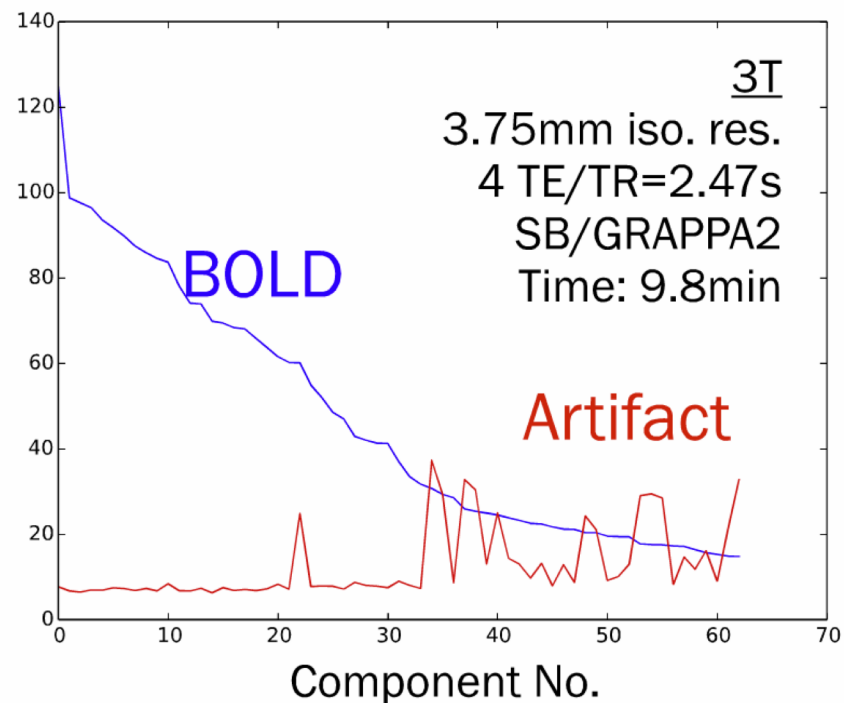
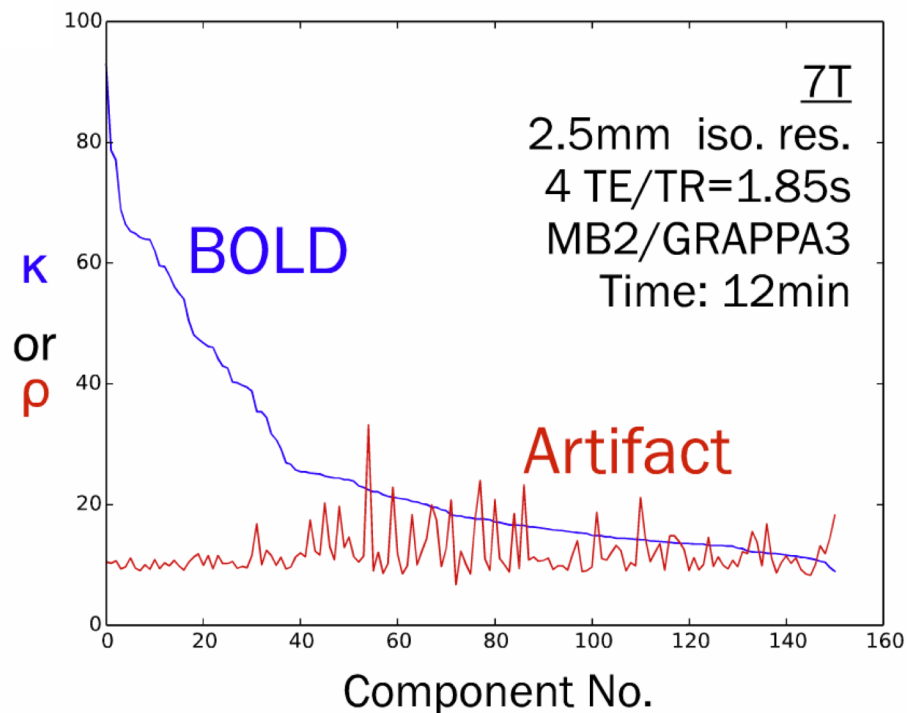


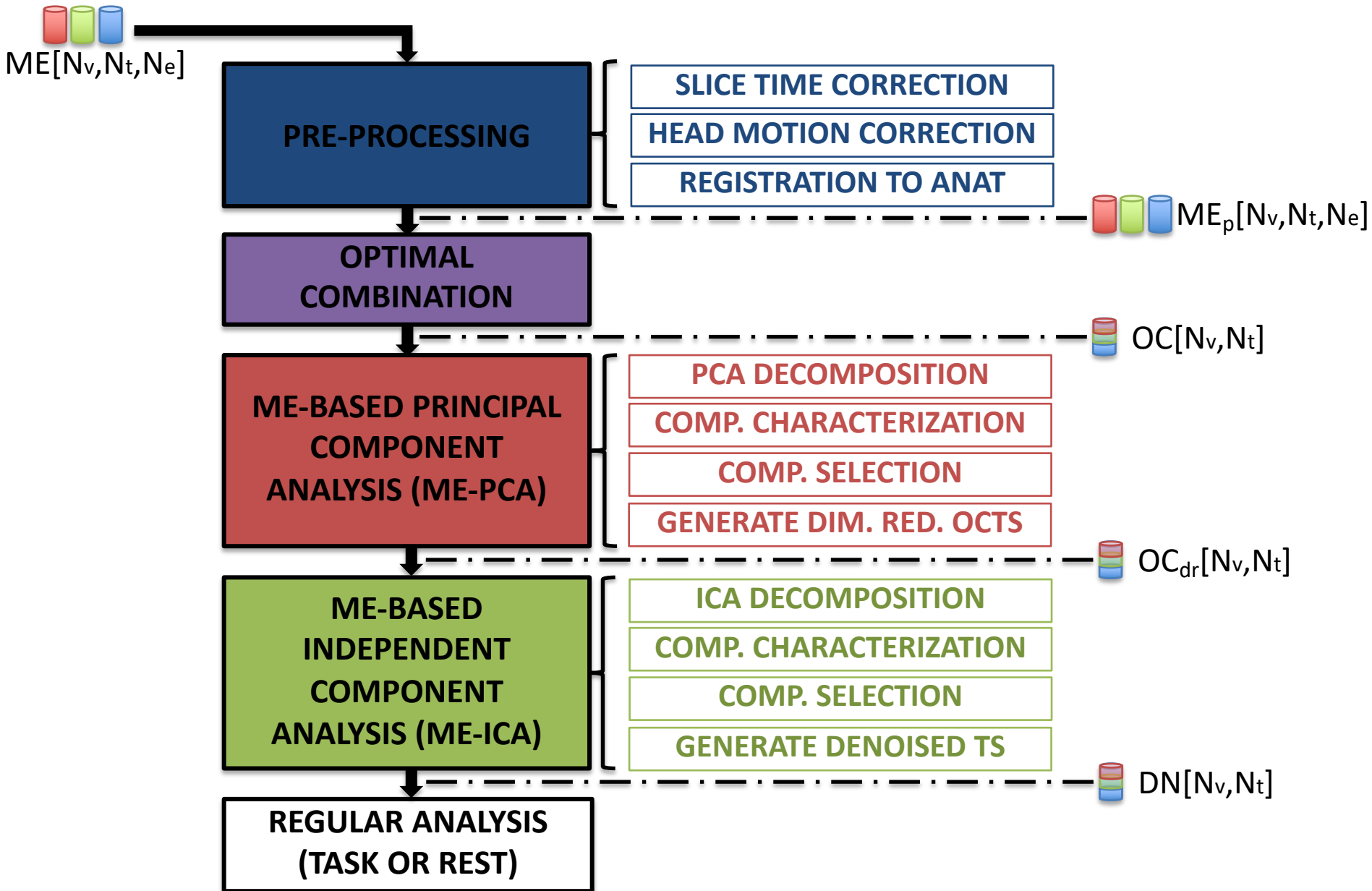
c  $\rho$ -spectrum across subjects

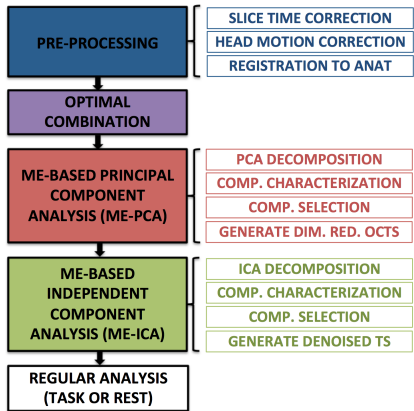


d  $\Delta S_0$  maps of top  $\rho$ -ranked components for a representative subject









## ME-PCA

- Uses PCA Decomposition (orthogonality).
- Yet, estimation of model order (Ncomp) is not based on variance, but on  $\kappa$  and  $\rho$  thresholds.
  - $\kappa_{thr} = f(\kappa_{elbow}, \kappa_{daw})$ ; Default  $\kappa_{daw} = 10$
  - $\rho_{thr} = f(\rho_{elbow}, \rho_{daw})$ ; Default  $\rho_{daw} = 1$
  - SELECTION RULE:  $\kappa > \kappa_{thr}$  are kept
  - SELECTION RULE:  $\rho > \rho_{thr}$  are kept

## ME-ICA

- Uses fast-ICA algorithm (spatial independence).
- Component Characterization includes:

- Variance Explained

- $\kappa$  ("BOLD likeliness")

- $\rho$  ("Non-BOLD likeliness")

- Nvoxels that significantly fit the  $S_0$  model

- Nvoxels that significantly fit the  $R_2^*$  model

- Spatial overlap (D) between ICA map and  $FR_2^*$  map

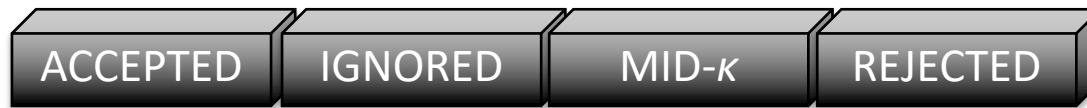
- Spatial overlap (D) between ICA map and  $FS_0$  map

- Other...

$\left. \begin{array}{l} \kappa \\ \rho \end{array} \right\} \rightarrow \text{If } \kappa_c < \rho_c \rightarrow \text{Discard } c$

$\left. \begin{array}{l} N_{so,c} \\ N_{R2,c} \end{array} \right\} \rightarrow \text{If } N_{so,c} < N_{R2,c} \rightarrow \text{Discard } c$

$\left. \begin{array}{l} \text{Spatial overlap (D) between ICA map and } FR_2^* \text{ map} \\ \text{Spatial overlap (D) between ICA map and } FS_0 \text{ map} \end{array} \right\} \rightarrow \text{If } D_{so,c} < D_{R2,c} \rightarrow \text{Discard } c$



Denoised Time series



## INPUTS

- Minimum: fMRI Datasets for all echoes, echo times
- Extras: Anatomical, Pre-processing options, kdaw, rdaw,

## OUTPUTS

- T2\* Static Map: *t2v.nii*
- So Static Map: *s0v.nii*
- Optimally Combined time series: *ts\_OC.nii*
- Denoised time series: *dn\_ts\_OC.nii*
- Spatial Maps for all ICA components: *betas\_OC.nii*
- Spatial Maps for Accepted Components only: *betas\_hik\_OC.nii*
- Time series for all PCA Components: *mepca\_mix.1D*
- Time series for all ICA Components: *meica\_mix.1D*
- Summary of ICA Decomposition: *comp\_table.txt*
  - List of accepted components
  - List of rejected components
  - List of Mid-k components
  - List of ignored components
  - Kappa and Rho values for all components
  - Total Variance Explained by the ICA decomposition

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## Your ME-ICA Report!

The program meica.py was created to form an algorithmic method for performing independent component analysis on multi-echo data and then algorithmically deciding which components represent BOLD-like phenomena.

The following content is a report that has taken information provided by meica.py and summarizes a few of the results.

This report form was created by the Section on Functional Imaging Methods in the NIMH. The creators of this report form are Benjamin Gutierrez, Prantik Kundu, Daniel Handwerker, Javier Gonzalez-Castillo, Souheil Inati, and Peter Bandettini.

Contents:

- Intro
- Preliminary Diagnostics
  - [TSNR](#)
- Component Visualization
  - Graphs
  - Accepted Components with anatomical
  - Rejected Components
  - Middle Components
  - Ignore Components

## Search

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file:///spin1/users/SFIMJGC/TALK\_fMRIClassME/PrCsData/SBJ02/D03\_Meica/SBJ02\_502Run10/meica.Report.SBJ02\_502Run10/html/diagnostics.html#tsnr

## ❖ WHAT IS MULTI-ECHO (ME) FMRI

## ❖ BASIC OPERATIONS WITH ME DATA

- Compute static  $S_0$  and  $T_2^*$  Maps
- Compute voxel-wise time-series of  $S_0$  (Non-BOLD) and  $T_2^*$  (BOLD)
- Combine echoes to improve SNR/spatially equalize functional contrast
- Echo Time Dependence Analysis

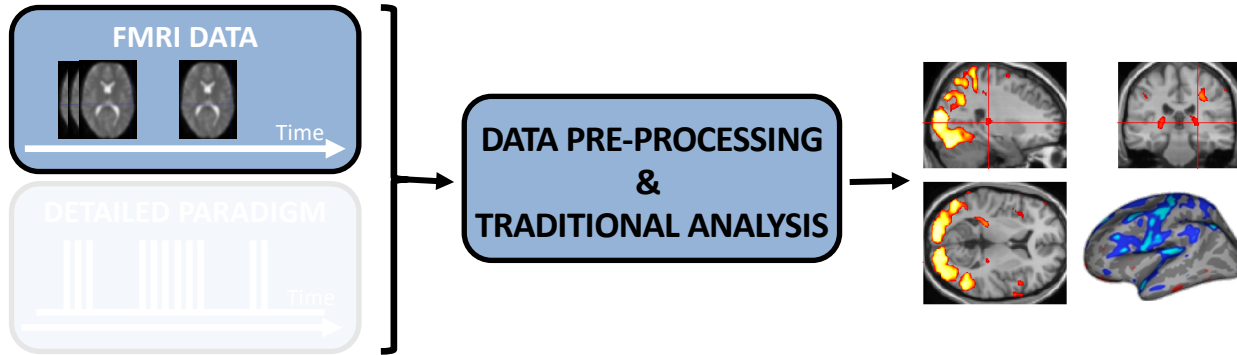
## ❖ ADVANCE AUTOMATIC DENOISING WITH ME-ICA

- ME-ICA Pipeline
- ME-ICA Outputs
- ME-ICA Web Reporting Tool

## ❖ EVENT DECONVOLUTION WITH ME-SPFM

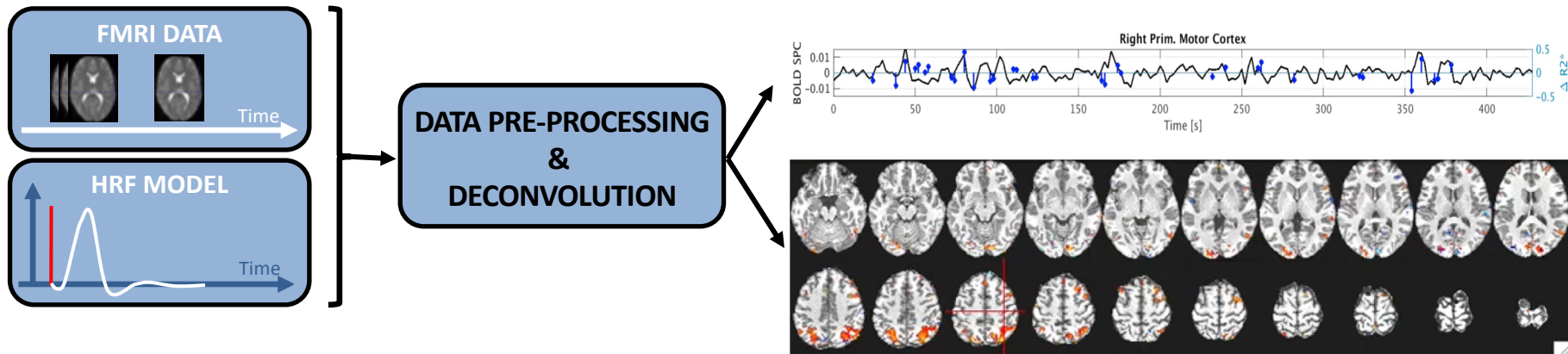
- What are fMRI Deconvolution Methods
- ME – Formulation for fMRI Deconvolution based on SPFM
- Example / Validation Experiments

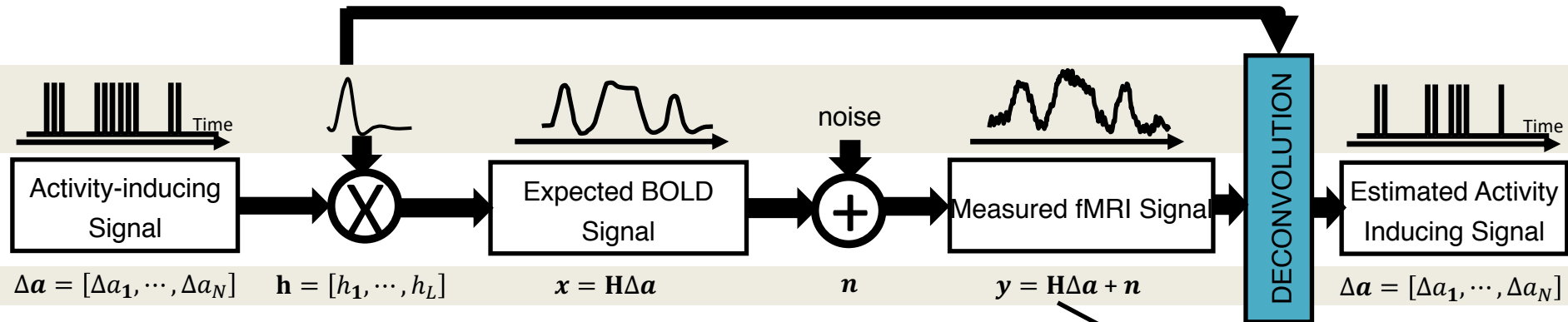
# What are deconvolution methods?



- There are experimental scenarios where event timing might be missing:
- Naturalistic paradigms
  - Clinical studies (e.g., interictal events)
  - Resting State

Deconvolution methods are an alternative in such scenarios:





If one assumes the underlying activity-inducing signal to consist of brief, sparse events, then the formulated deconvolution problem can be solved using LASSO regularization:

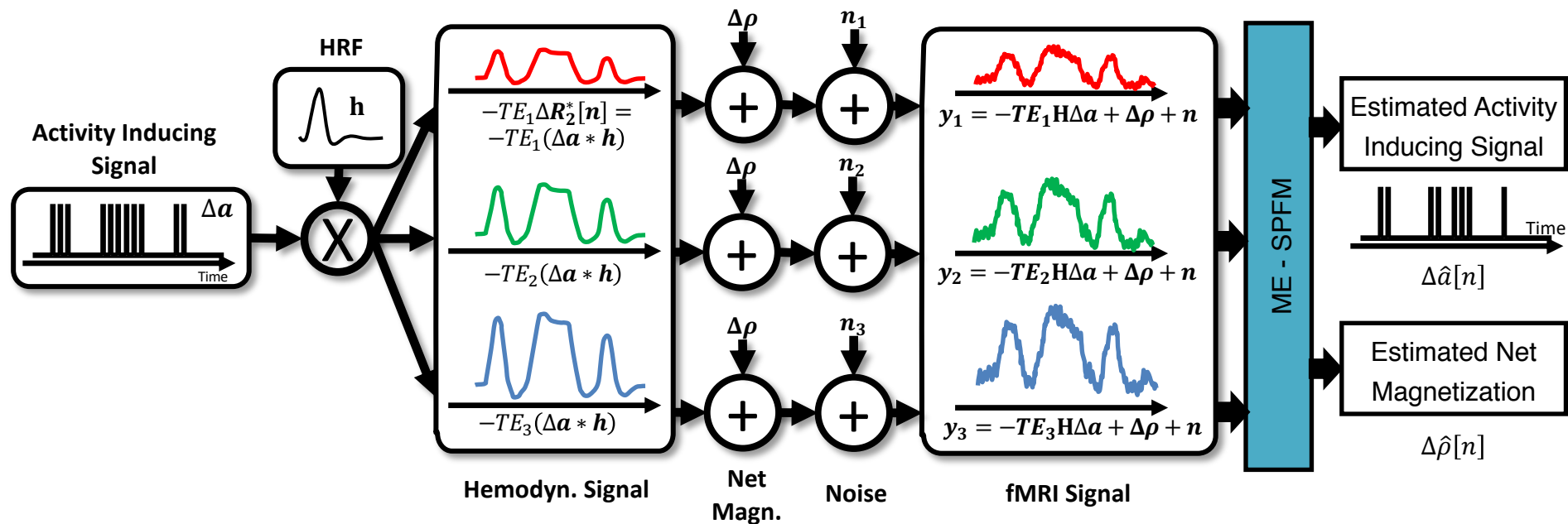
$$\Delta \hat{a} = \arg \min_{\Delta a} \frac{1}{2} \underbrace{\|y - H\Delta a\|_2^2}_{\text{Error Minimization Term}} + \lambda \underbrace{\|\Delta a\|_1}_{\text{L1-Norm Regularization (Sparseness)}}$$

Single Echo Sparse Free Paradigm Mapping Algorithm



3dPFM





$$\bar{\mathbf{y}} \stackrel{\text{def}}{=} \begin{bmatrix} \mathbf{y}_1 \\ \vdots \\ \mathbf{y}_K \end{bmatrix} = \underbrace{\begin{bmatrix} \mathbf{I} \\ \vdots \\ \mathbf{I} \end{bmatrix}}_{\bar{\mathbf{I}}} \Delta \rho - \underbrace{\begin{bmatrix} TE_1 \mathbf{H} \\ \vdots \\ TE_K \mathbf{H} \end{bmatrix}}_{\bar{\mathbf{H}}} \Delta a$$

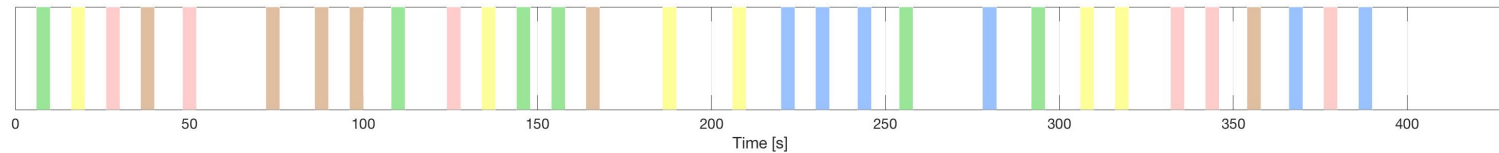
Assuming sparsity in both unknowns, we can solve using LASSO regularization

$$\Delta \hat{a}, \Delta \hat{\rho} = \arg \min_{\Delta a, \Delta \rho} \frac{1}{2} \|\bar{\mathbf{y}} - \bar{\mathbf{H}} \Delta a - \bar{\mathbf{I}} \Delta \rho\|_2^2 + \lambda_1 \|\Delta a\|_1 + \lambda_2 \|\Delta \rho\|_1$$

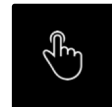
- 10 Subjects (5M/5F)
- GRE – EPI @ 3T / 32 Channel Coil
- TE = 16.3/32.2/48.1 ms
- TR = 2 seconds
- Resolution = 3 x 3 x 4 mm<sup>3</sup>
- ASSET = 2

Rapid Event Related with 5 different tasks / 6 trials per task per run / events are approx. 4 seconds long

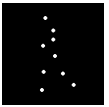
### SCHEMATIC OF ONE FUNCTIONAL RUN



Listen to an audio clip and select instrument being played from the ones displayed on the screen.



Press button at an approx. rate of 0.5Hz (following a counter on the screen).



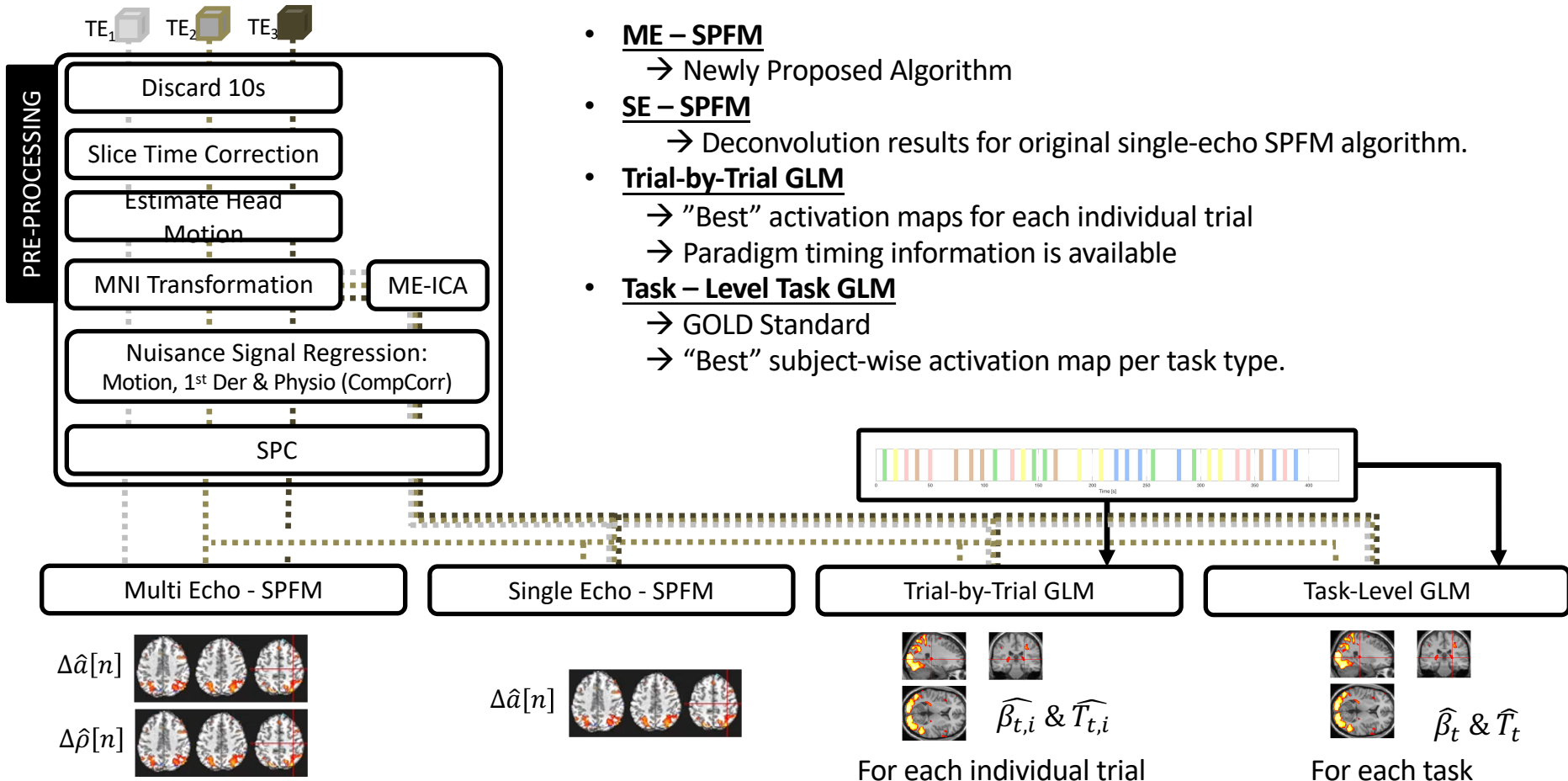
Passive viewing of dots patterns resembling different types of biological motion.



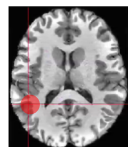
Silently read sentences that appear on the screen one word at a time.



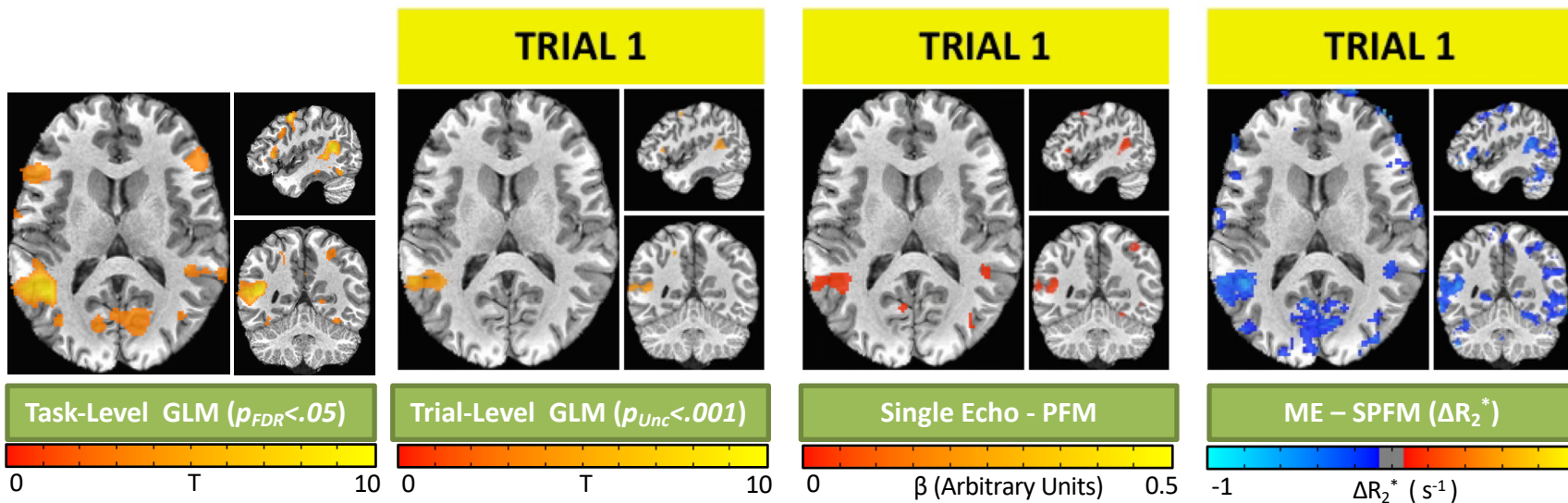
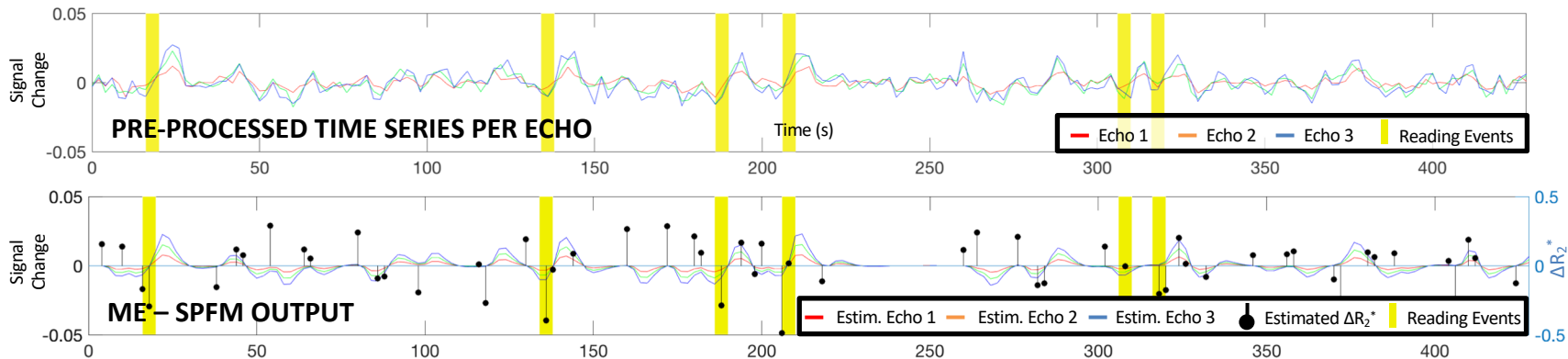
Passive viewing of images of houses



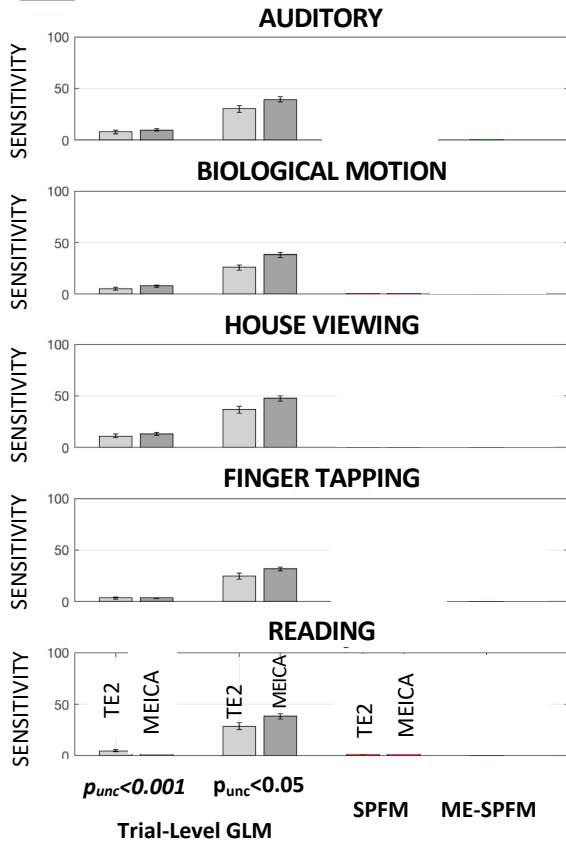




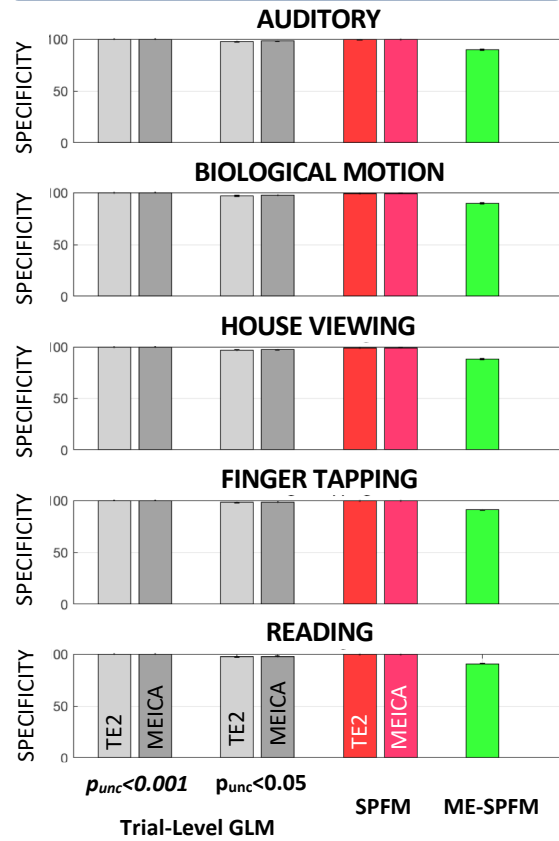
READ THIS



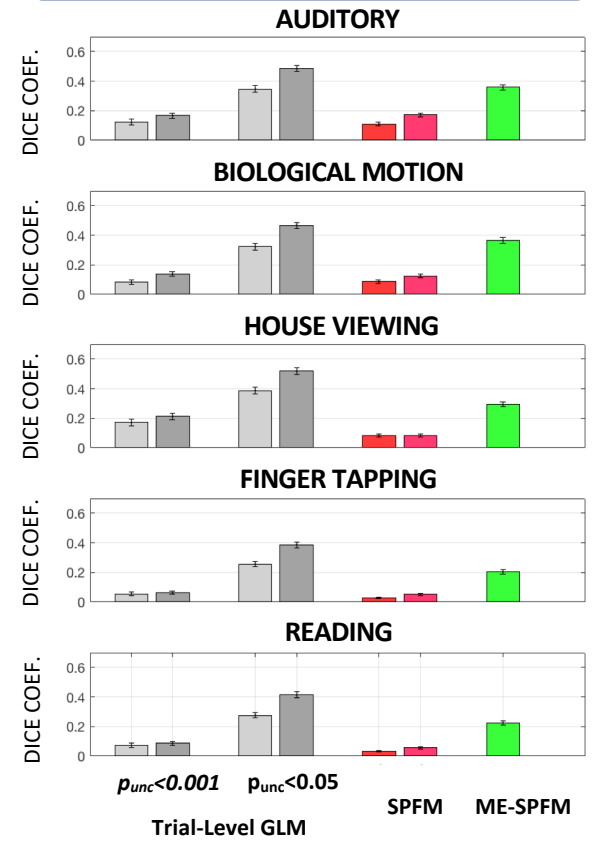
## SENSITIVITY vs. TASK-LEVEL GLM

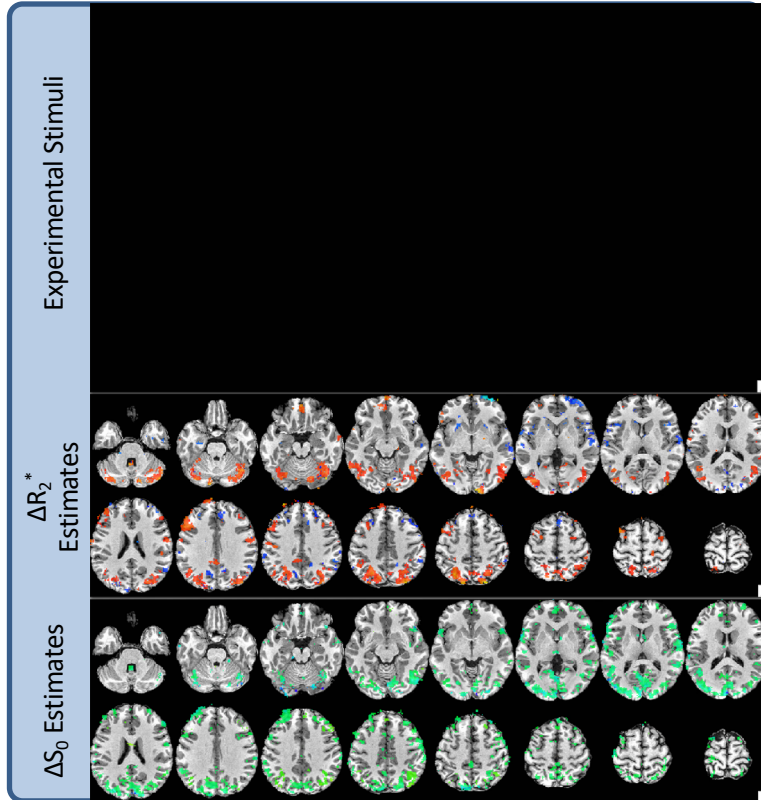


## SPECIFICITY vs. TASK-LEVEL GLM



## DICE COEFFICIENT



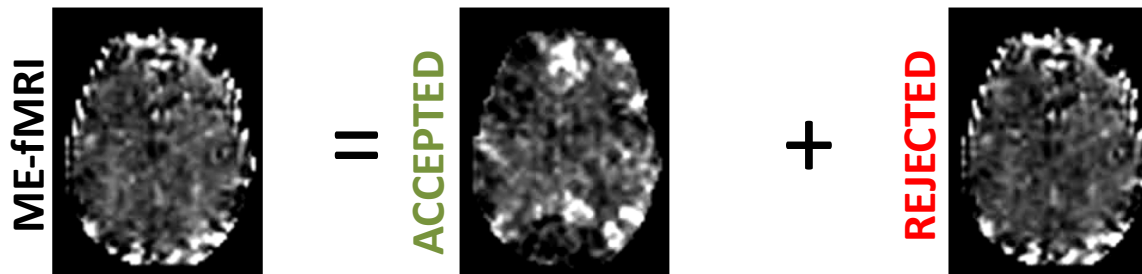


- Understand the pros/cons of different formulations for the ME deconvolution problem.

	Models	Sparsity
$\Delta\hat{\mathbf{a}} = \arg \min_{\Delta\mathbf{a}} \frac{1}{2} \ \mathbf{y} - \mathbf{H}\Delta\mathbf{a}\ _2^2 + \lambda \ \Delta\mathbf{a}\ _1$	$\Delta R_2^*$	$\Delta R_2^*$
$\Delta\hat{\mathbf{a}}, \Delta\hat{\boldsymbol{\rho}} = \arg \min_{\Delta\mathbf{a}, \Delta\boldsymbol{\rho}} \frac{1}{2} \ \mathbf{y} - \mathbf{H}\Delta\mathbf{a} - \mathbf{I}\Delta\boldsymbol{\rho}\ _2^2 + \lambda_1 \ \Delta\mathbf{a}\ _1 + \lambda_2 \ \Delta\boldsymbol{\rho}\ _1$	$\Delta R_2^*, \Delta S_0$	$\Delta R_2^*, \Delta S_0$
$\Delta\hat{\mathbf{a}}, \Delta\hat{\boldsymbol{\rho}} = \arg \min_{\Delta\mathbf{a}} \frac{1}{2} \ \mathbf{y} - \mathbf{H}\Delta\mathbf{a} - \mathbf{I}\Delta\boldsymbol{\rho}\ _2^2 + \lambda \ \Delta\mathbf{a}\ _1$	$\Delta R_2^*, \Delta S_0$	$\Delta R_2^*$

- Explore the limitations of the algorithm in terms of event duration, temporal overlap of events, etc.
- Adapt the method to accommodate spatial heterogeneity in hemodynamic response shape.
- Explore its application to scientifically and clinically relevant scenarios.

- ❑ Multi-echo fMRI allows to capture additional information with minimal costs in terms of temporal and spatial resolution.
- ❑ Such additional information can be used to:
  - ❑ Increase CNR in drop-out regions (e.g., Optimal Combination of Echoes).
  - ❑ Automatically separate BOLD-like from Non-BOLD-like components (ME-ICA).
  - ❑ Significantly increase the sensitivity of BOLD deconvolution algorithms
- ❑ ME-ICA is a denoising methodology that combines ICA with TE-Dependence Analysis:
  - ❑ Will not clean every single artifact in the data.
  - ❑ Still under development.
  - ❑ Can substantially improve the SNR of the data → Quality of the results.



- ❑ ME-SPFM can help us reliably detect individual BOLD events without a-priori information about their timing.



## Section on Functional Imaging Methods

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 Linqing Li



3dMEPFM will be soon available in

