

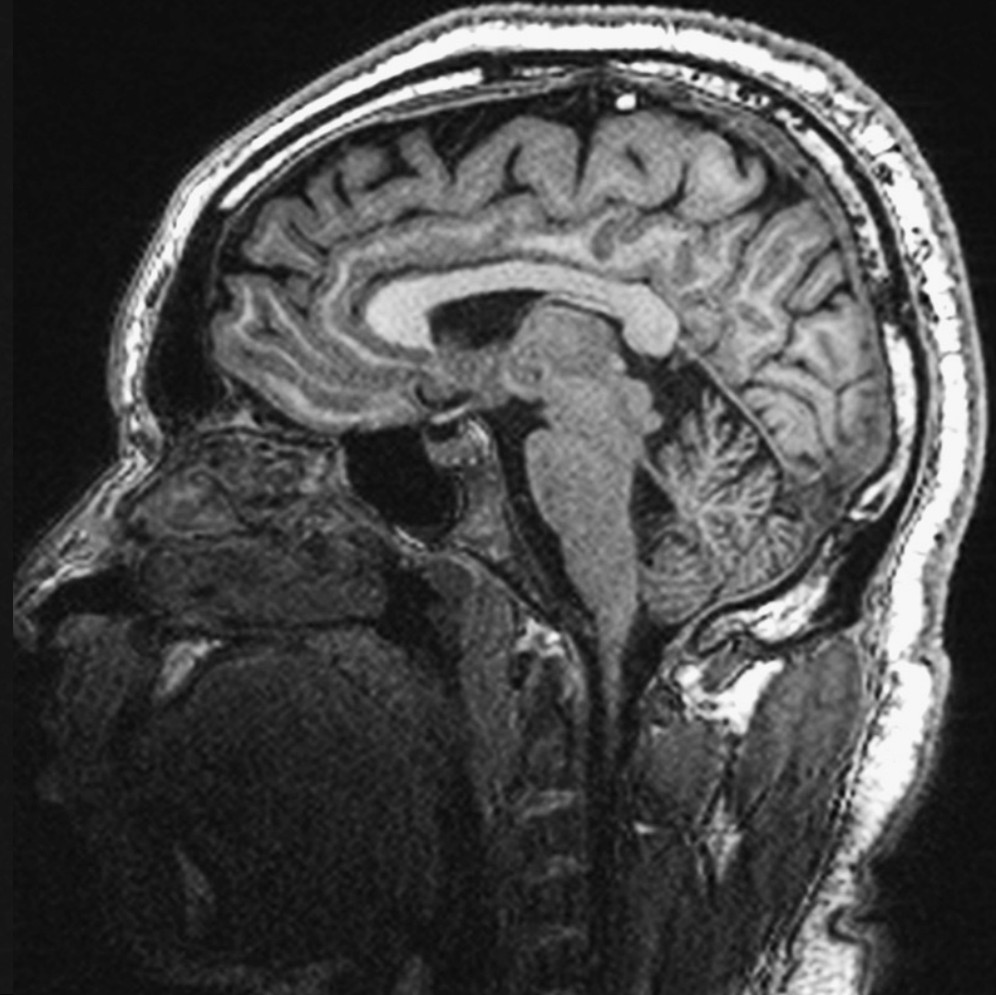
# Quantitative MRI

Govind Nair  
Staff Scientist, NINDS

42 y.o. M  
Multiple sclerosis

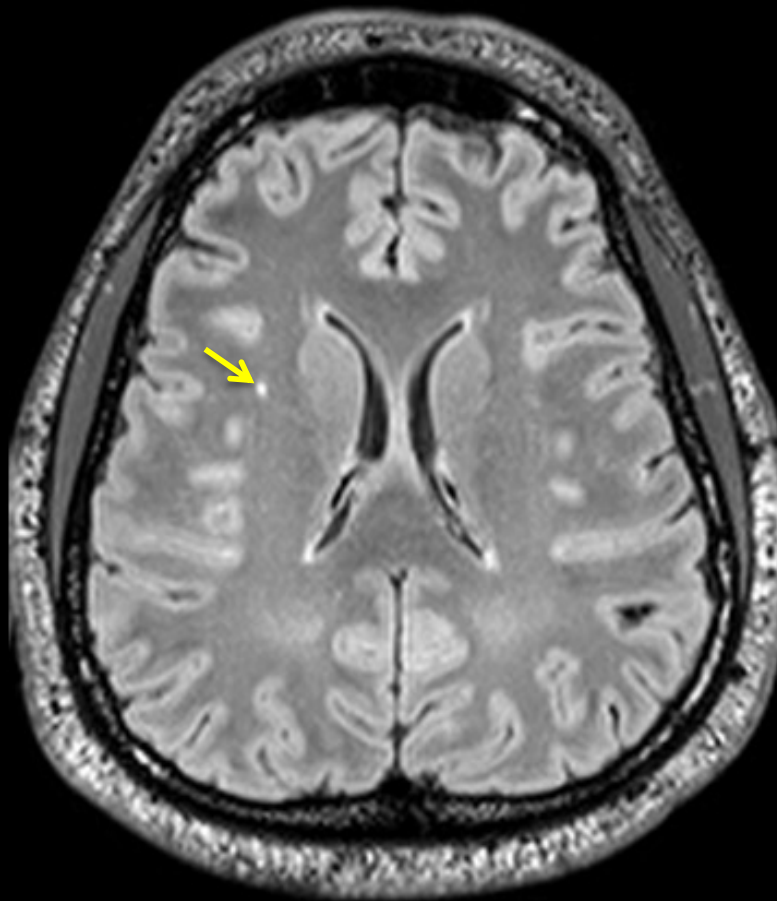


40 y.o. M  
Healthy Volunteer

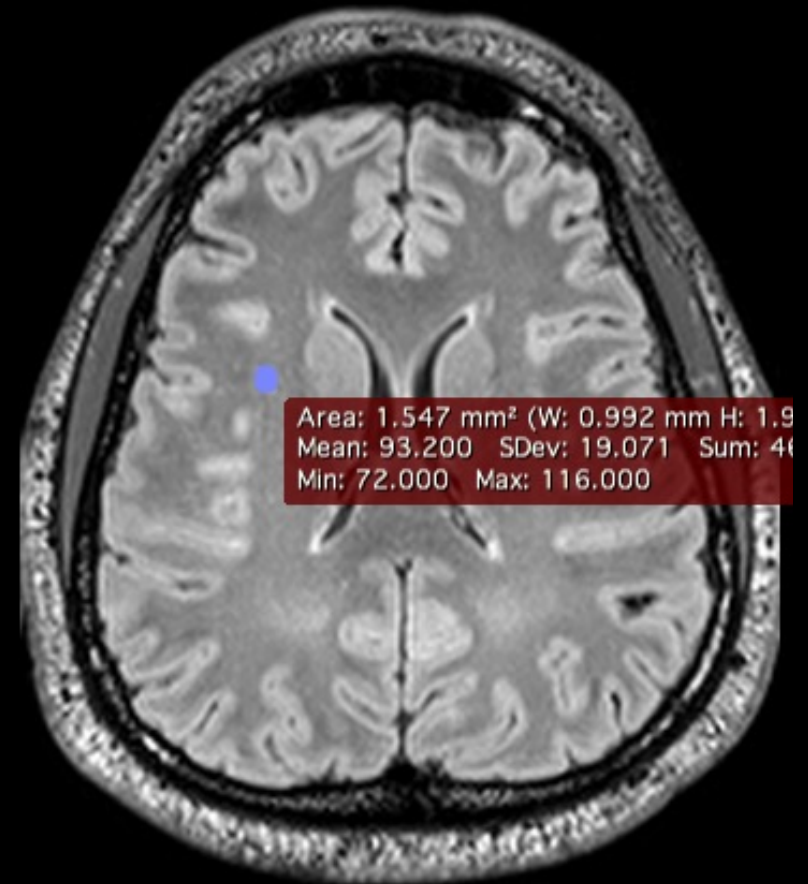


Multiple sclerosis is an immune mediated neurodegenerative disease affecting the myelin, axons, and neurons.

# Qualitative vs. Quantitative

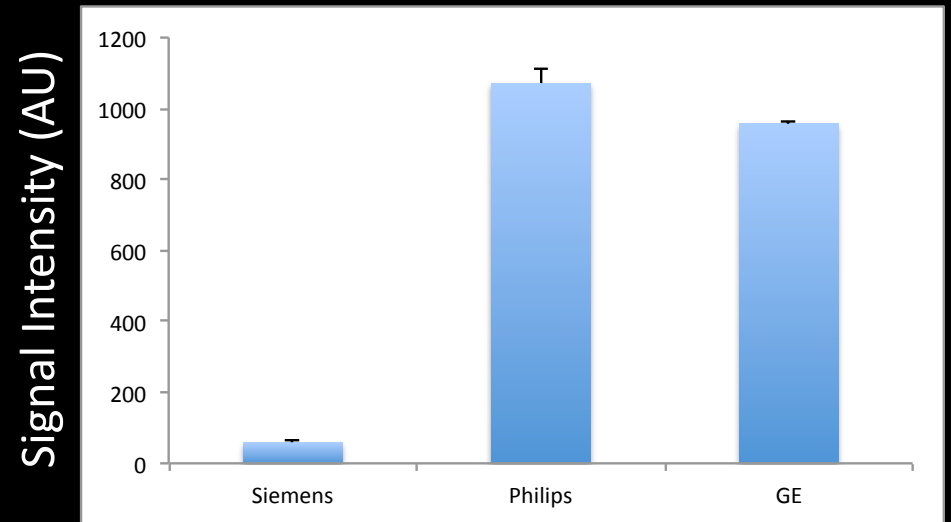
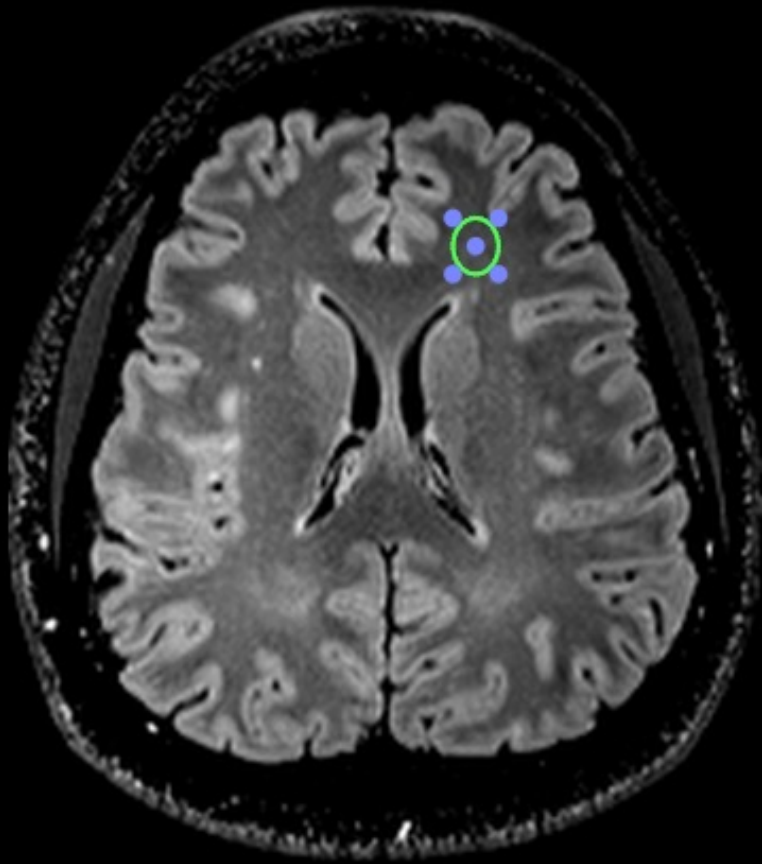


Qualitative: "Hyper-intense lesion seen in the deep white matter"



Fluid-Attenuated Inversion Recovery (FLAIR)

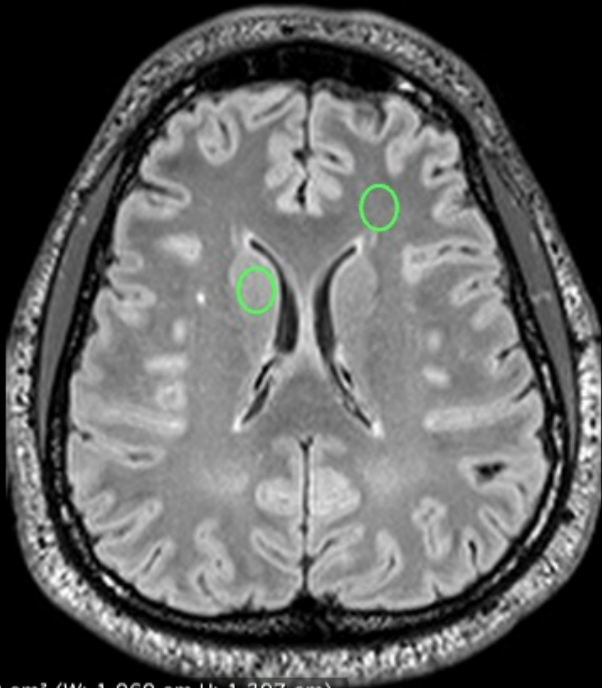
# The Trouble with Quantitation



Different scanners, very similar protocols  
FLAIR

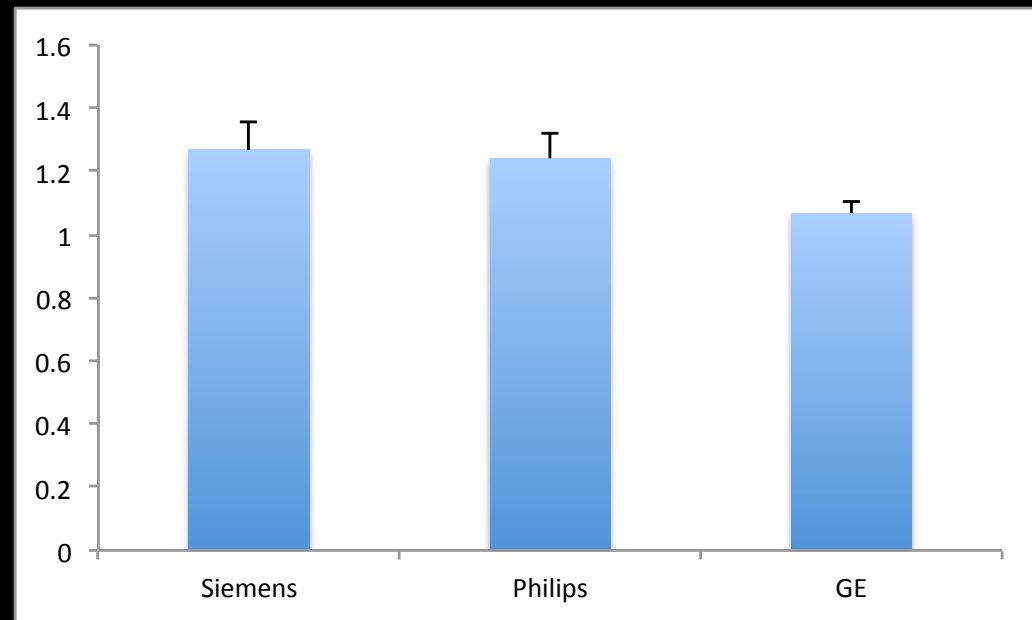
# The Trouble with Quantitation

Area: 1.089 cm<sup>2</sup> (W: 1.060 cm H: 1.307 cm)  
Mean: 60.888 SDev: 2.493 Sum: 7611  
Min: 56.000 Max: 71.000



Area: 1.089 cm<sup>2</sup> (W: 1.060 cm H: 1.307 cm)  
Mean: 77.179 SDev: 3.334 Sum: 9493  
Min: 69.000 Max: 86.000

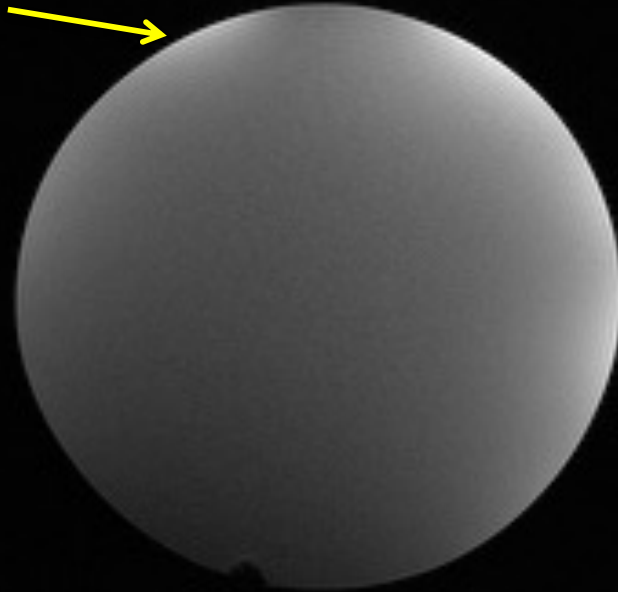
Ratio of Signal Intensities



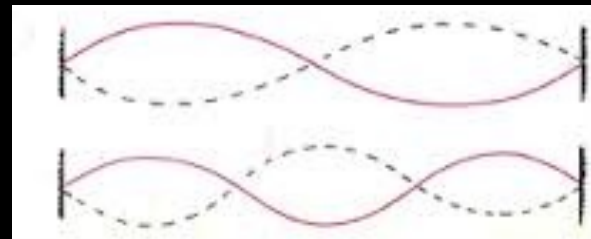
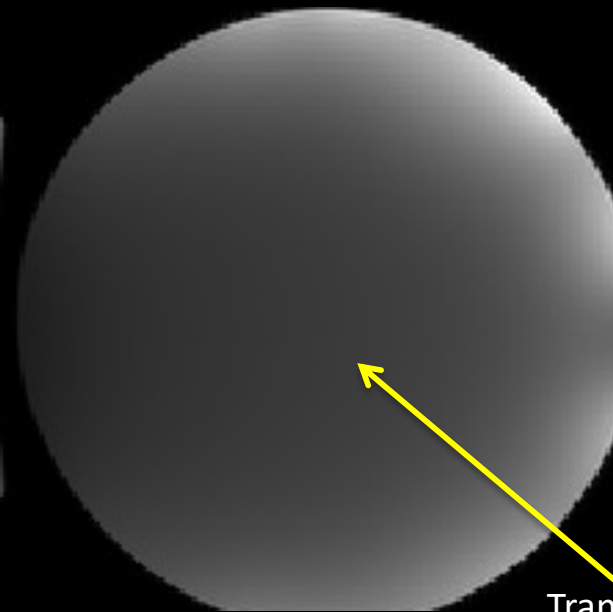
Different scanners, very similar protocols  
FLAIR

# Coil Sensitivities Effect Normalization

Receiver effects

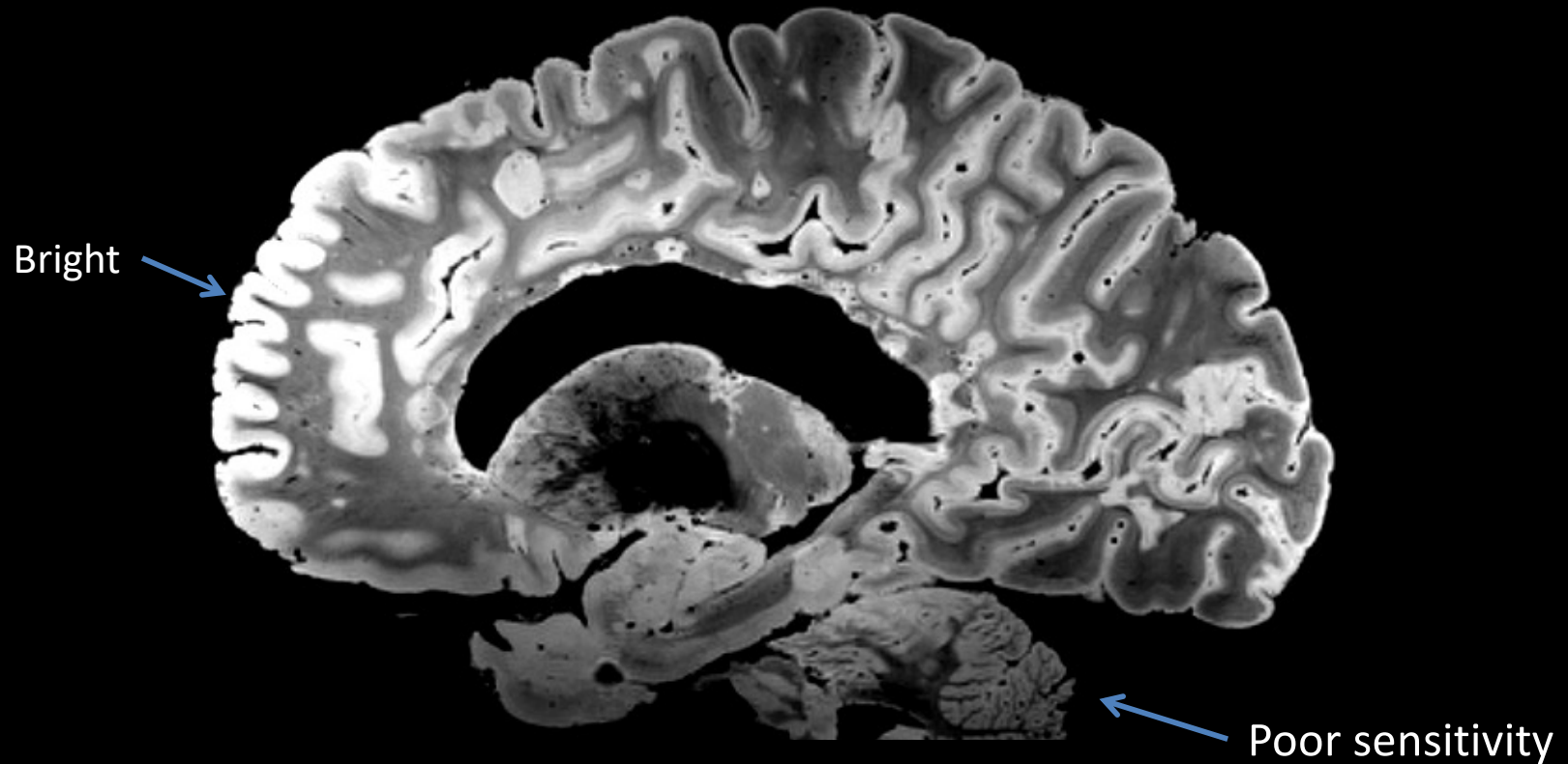


Transmit effects





# Coil Sensitivities Effect Normalization



# Why Bother with Quantitation: Philosophical

*"I often say that when you can measure what you are speaking about, and express it in numbers, you know something about it; but when you cannot measure it, when you cannot express it in numbers, your knowledge is of a meager and unsatisfactory kind; it may be the beginning of knowledge, but you have scarcely in your thoughts advanced to the state of Science, whatever the matter may be."*

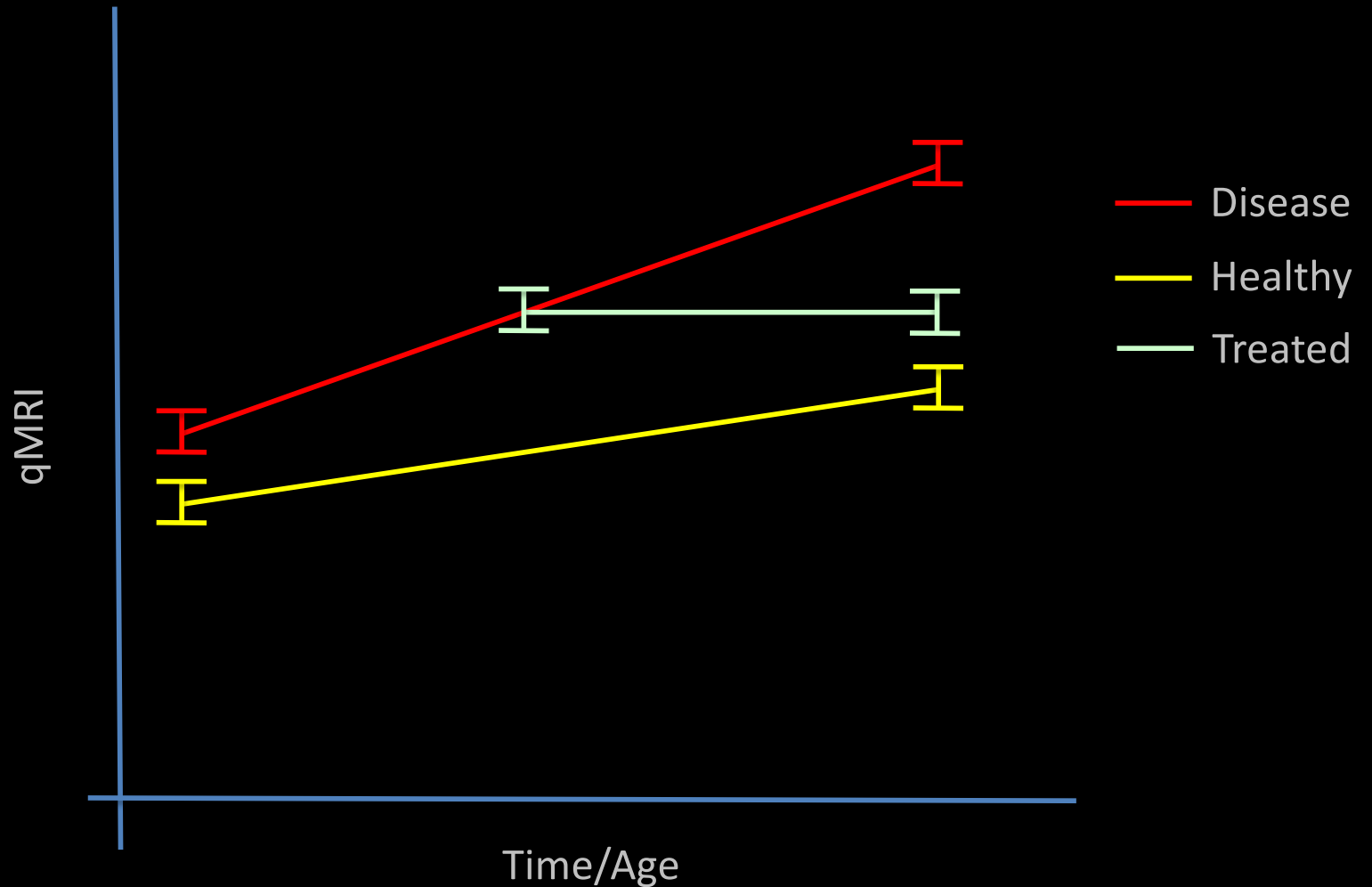
- *Lord Kelvin [PLA, vol. 1, "Electrical Units of Measurement", 1883-05-03]*

Courtesy of Daniel Glen

qMRI parameters may reflect specific biological processes



# Why Bother with Quantitation: Clinical



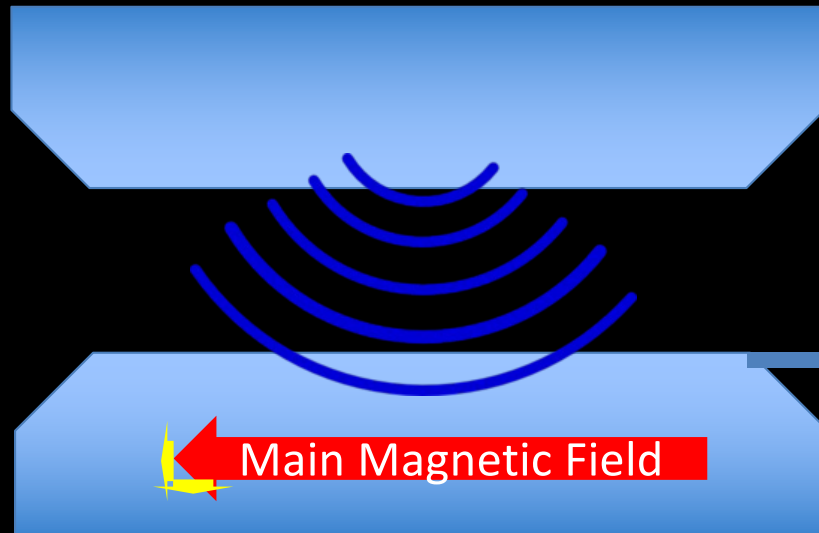
# Commonly used qMRI measures

- Basic MR parameters
  - $T_1$ ,  $T_2$ ,  $T_2^*$  Relaxometry
  - Diffusion of water in tissue
  - Metabolite concentrations using MR Spectroscopy
  - Volumetrics
  - ...
- Derived parameters
  - Blood flowing through tissue (perfusion)
  - Permeability of blood brain barrier
  - ...

# Commonly used qMRI measures

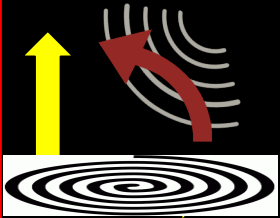
- Basic MR parameters
  - $T_1$ ,  $T_2$ ,  $T_2^*$  Relaxometry
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  - Metabolite concentrations using MR Spectroscopy
  - Volumetrics
  - ...
- Derived parameters
  - Blood flowing through tissue (perfusion)
  - Permeability of blood brain barrier
  - ...

# Back to Fundamentals

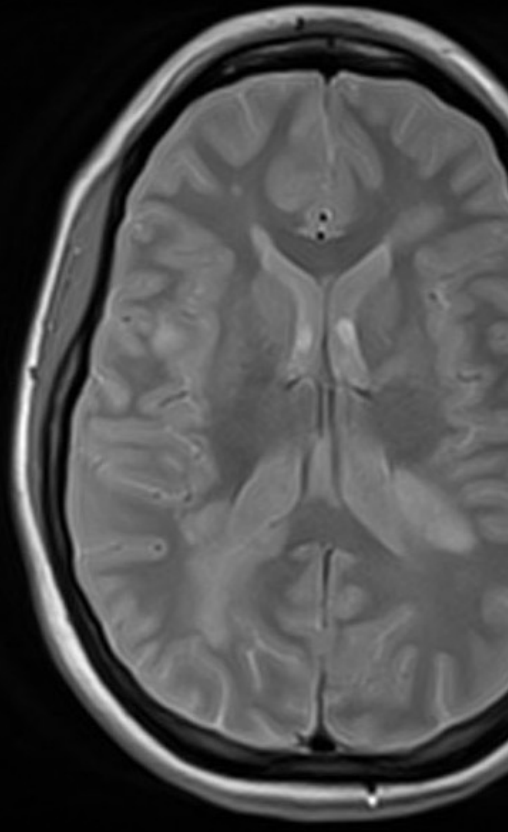


# Quick Review of Basic MRI Contrasts

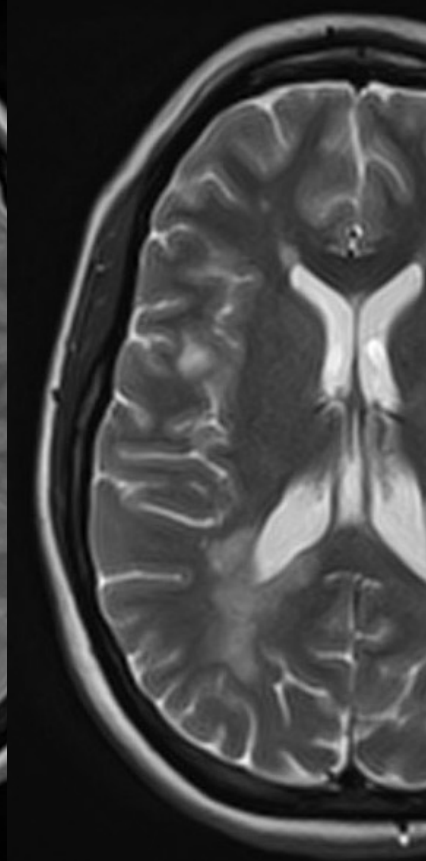
Main Magnetic Field



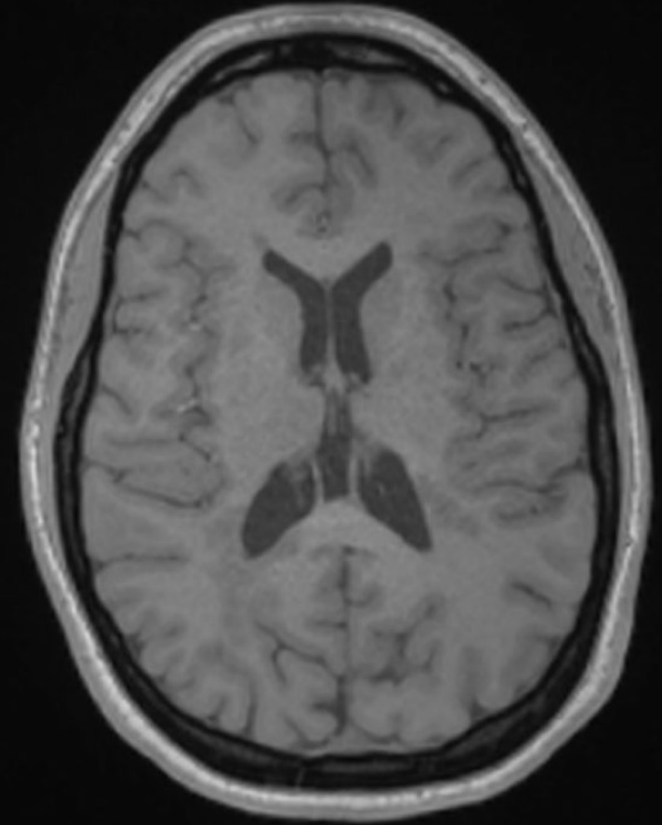
Detector & Recon.



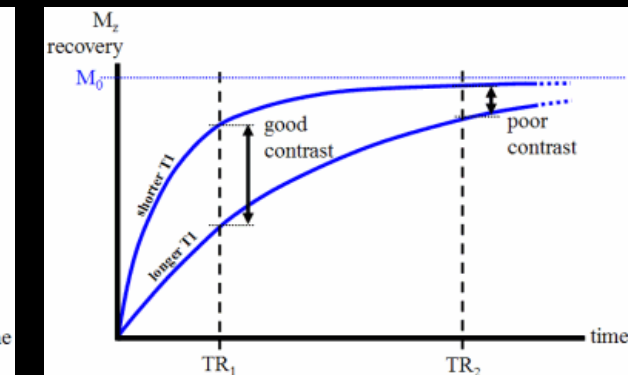
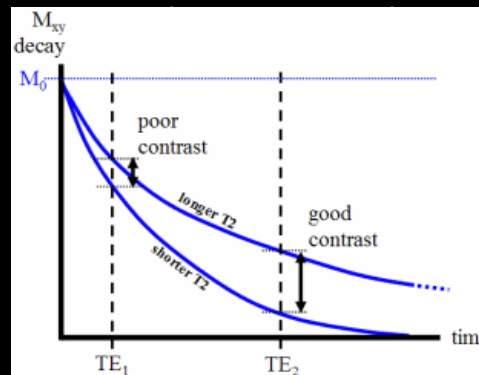
Proton density weighted  
(grey image)



T<sub>2</sub>-weighted

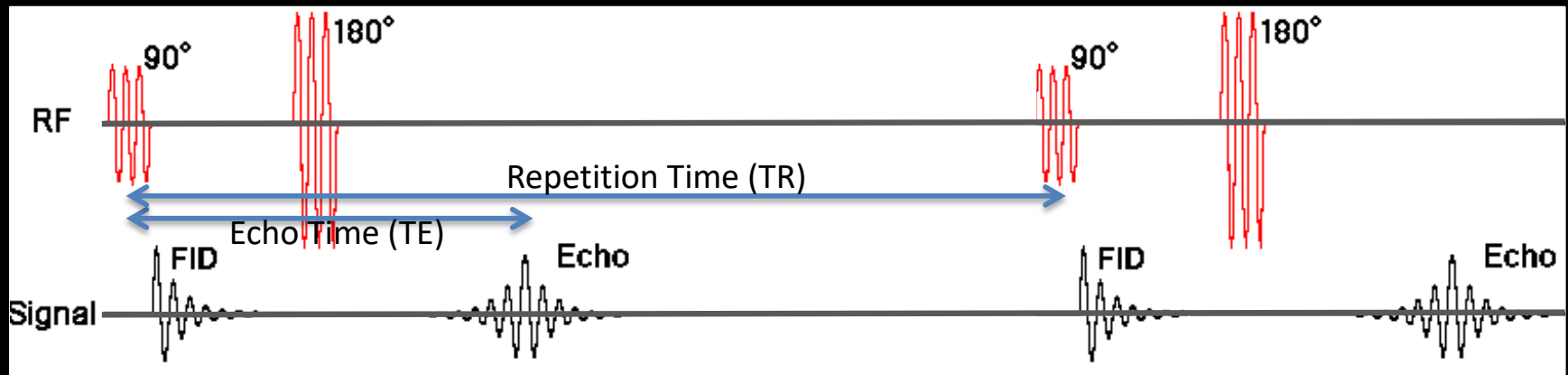


T<sub>1</sub>-weighted



Patient with multiple sclerosis

# Engineering the Contrast



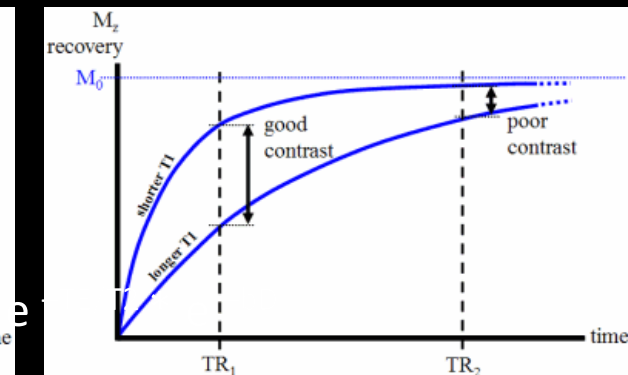
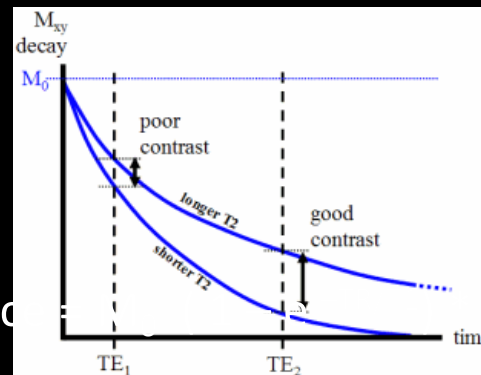
T<sub>2</sub> Relaxation:

$$M = M_0 e^{-TE/T_2}$$

T<sub>1</sub> Relaxation:

$$M = M_0 (1 - e^{-TR/T_1})$$

Signal from Spin Echo sequence



Signal from Gradient Echo Sequence

$$S = k [H] \frac{\sin \alpha (1 - e^{-TR/T1})}{(1 - (\cos \alpha) e^{-TR/T1})} e^{-TE/T2}$$

Signal from MPRAGE

$$\frac{1 - \varphi + \frac{\varphi \cdot \cos(\theta) \cdot (1 - \delta) \cdot (1 - \mu^{N-1})}{1 - \mu} + \varphi \cdot \cos(\theta) \cdot \mu^{N-1} + \rho \cdot \cos(\alpha) \cdot \cos^N(\theta)}{1 - \rho \cdot \cos(\alpha) \cdot \cos^N(\theta)}$$

$$\delta = \exp\left(-\tau/T_1\right), \varphi = \exp\left(-TD/T_1\right), \text{ and } \mu = \delta \cdot \cos(\theta)$$

Signal from Steady State Sequences

$$M_0(\text{sqrt}(\sin(\text{FA}) * E_2(1-E_1)))/[1-(E_1-E_2)*\cos(\text{FA}) - E_1 * E_2]$$

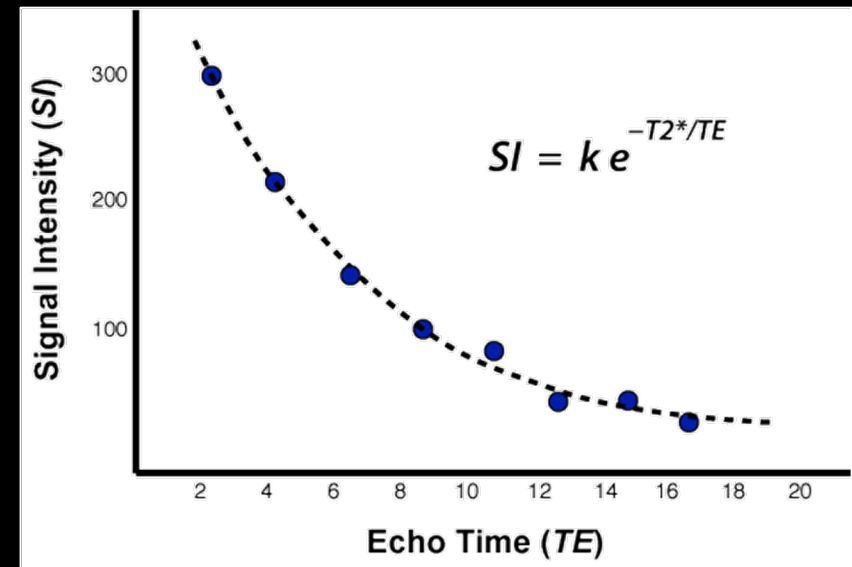
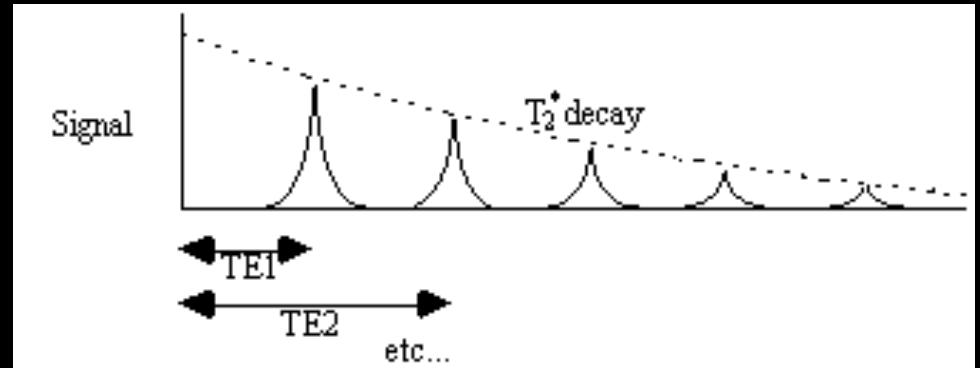
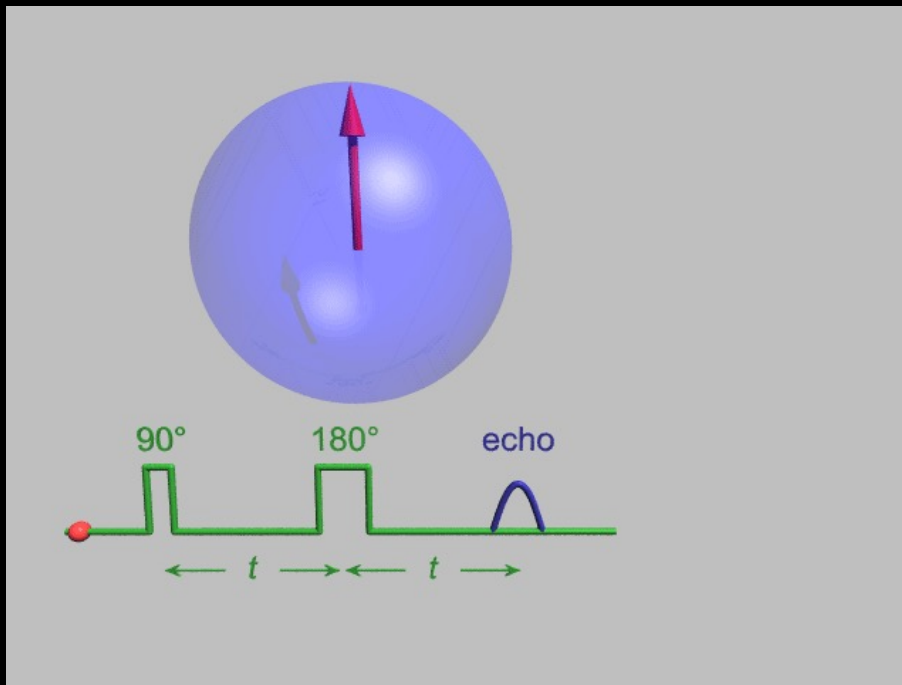
Where  $E_1 = \exp(-T_R/T_1)$  and  $E_2 = \exp(-T_R/T_2)$

$$S_{FISP} = k \tan(\alpha/2) \left[ 1 - (e^{TR/T1} - \cos \alpha) \sqrt{\frac{1 - e^{-2TR/T2}}{(1 - e^{-TR/T1})^2 - e^{-2TR/T2}(e^{-TR/T1} - \cos \alpha)^2}} \right] e^{-TE/T2}$$

$$S_{PSIF} = k \tan(\alpha/2) \left[ 1 - (1 - e^{TR/T1} \cos \alpha) \sqrt{\frac{1 - e^{-2TR/T2}}{(1 - e^{-TR/T1})^2 - e^{-2TR/T2}(e^{-TR/T1} - \cos \alpha)^2}} \right] e^{-TE/T2}$$



# T<sub>2</sub> Relaxation

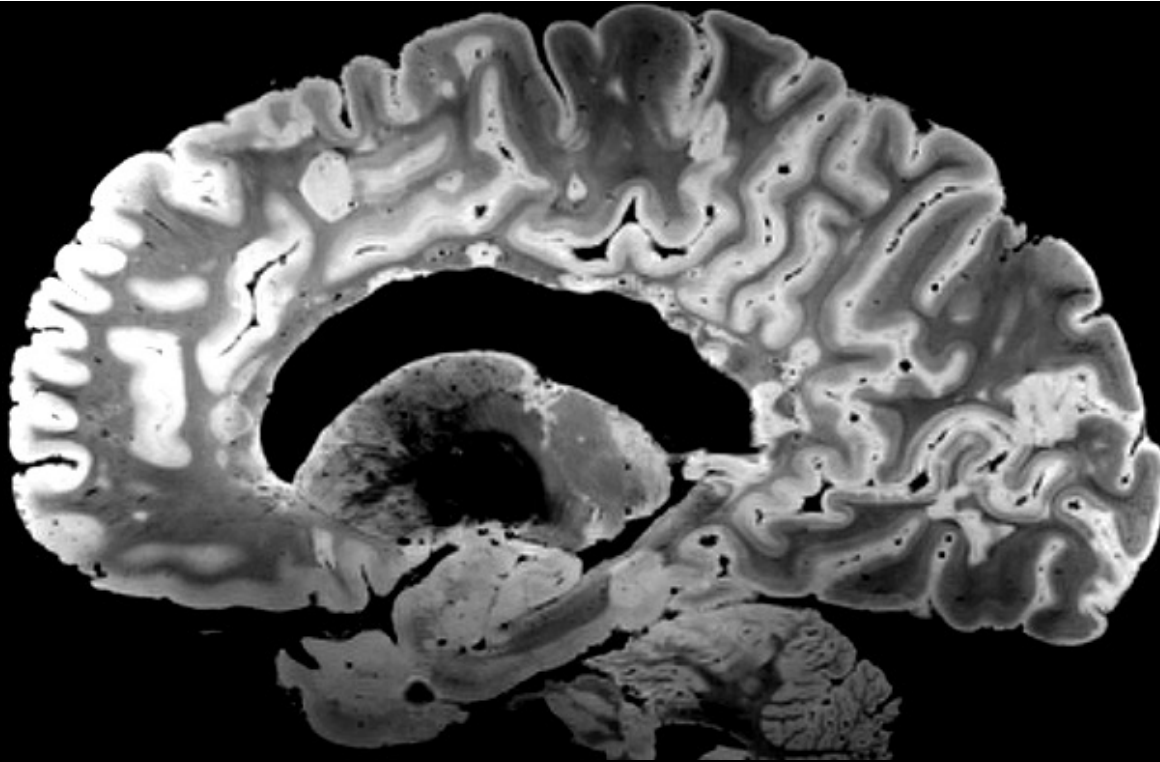


Signal loss due to:

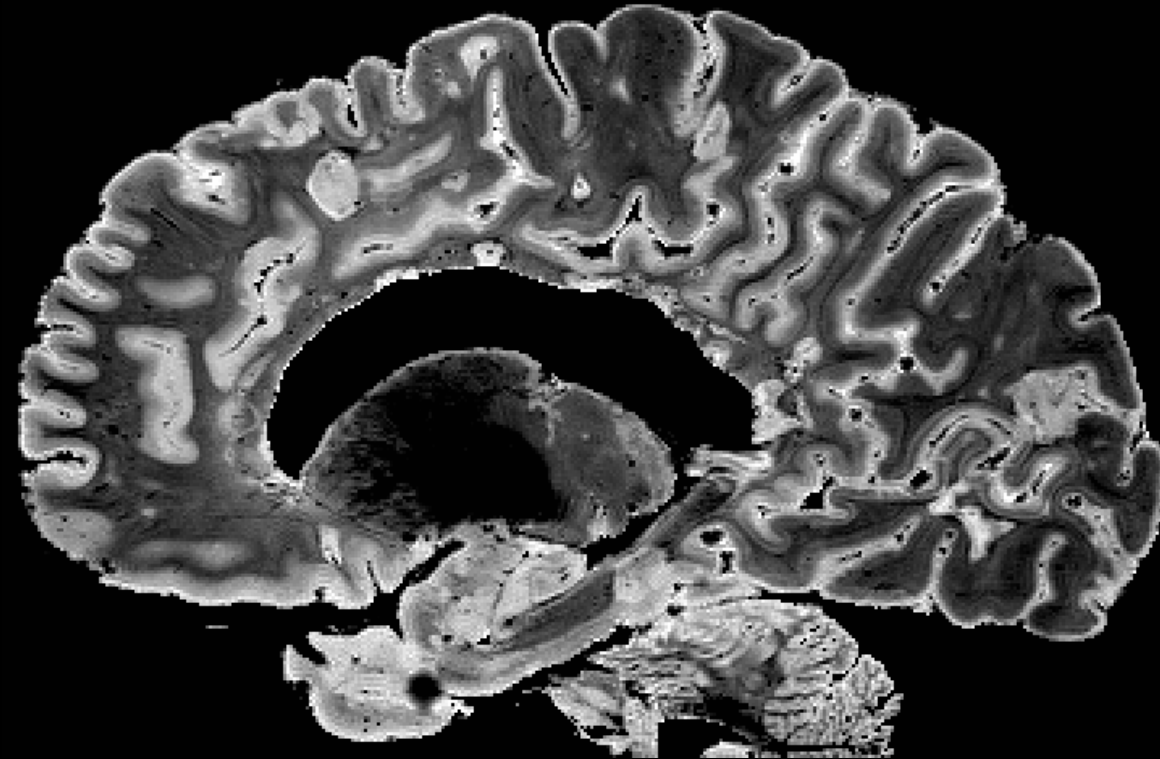
- Macroscopic magnetic field inhomogeneities (refocused by the 180° pulse)
- Local environment (presence of paramagnetic molecules, viscosity...) – T<sub>2</sub>

T<sub>2</sub> map now reflects a property of the tissue

$T_2^*$ -weighted  
TE=16 ms



$T_2^*$ -map



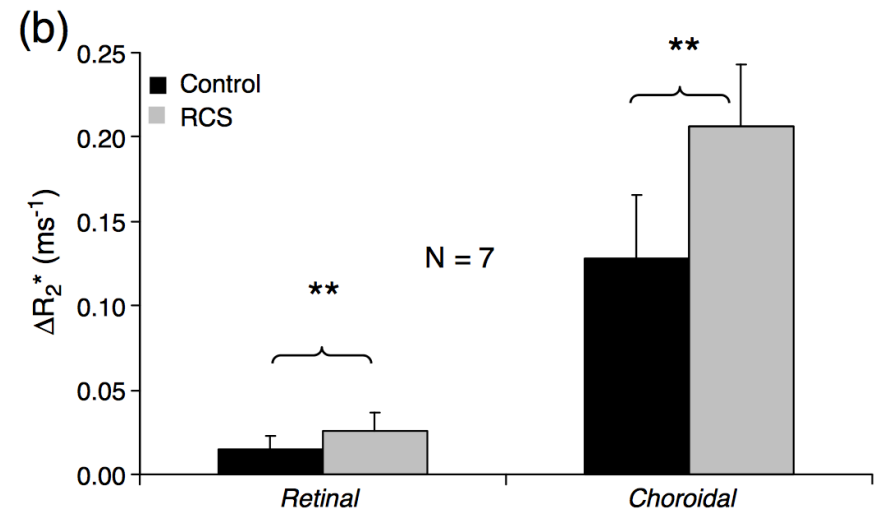
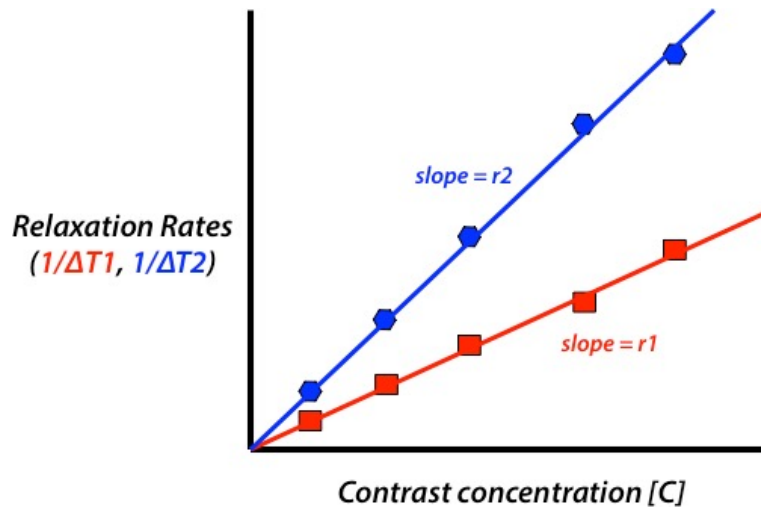
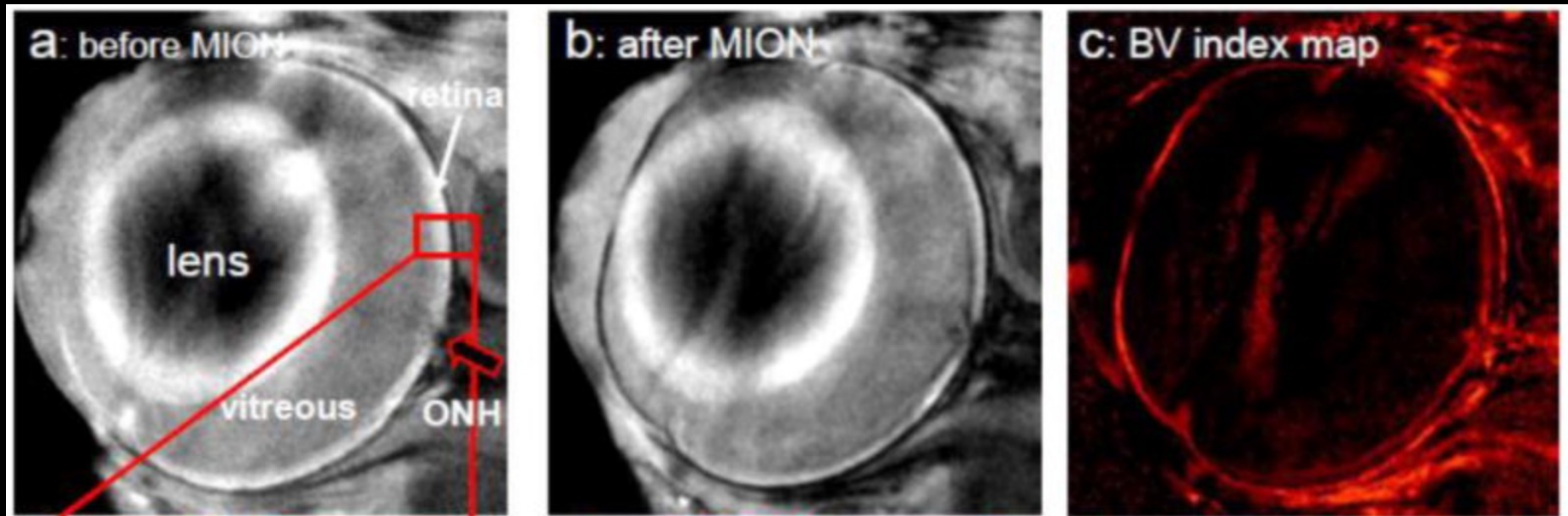
Pros

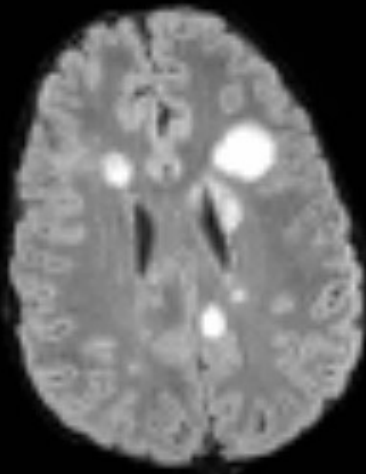
- Intensity may actually mean something

Cons

- Fitting errors and related artifacts

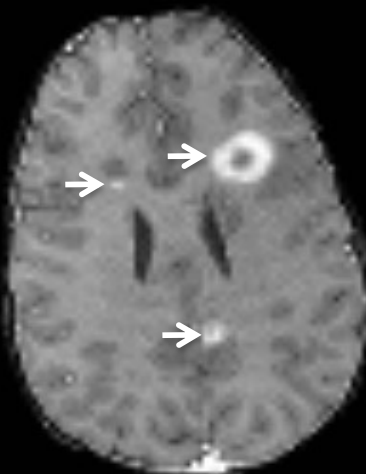
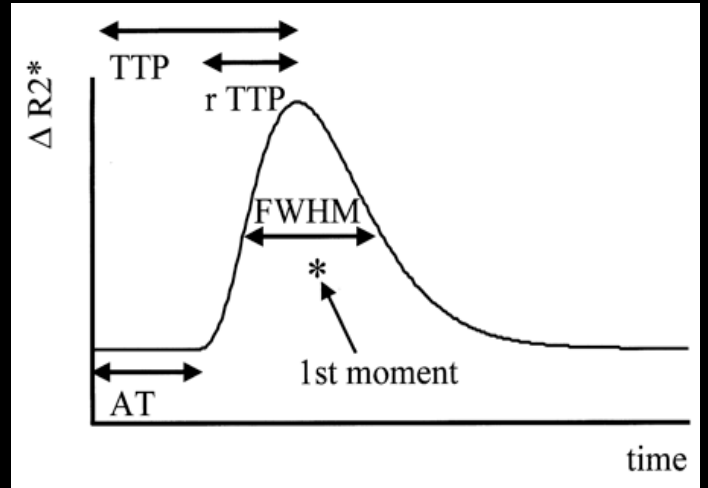
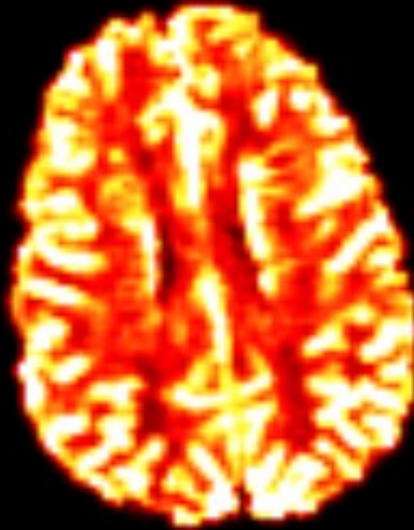
# Applications: Exogenous Contrast Agents





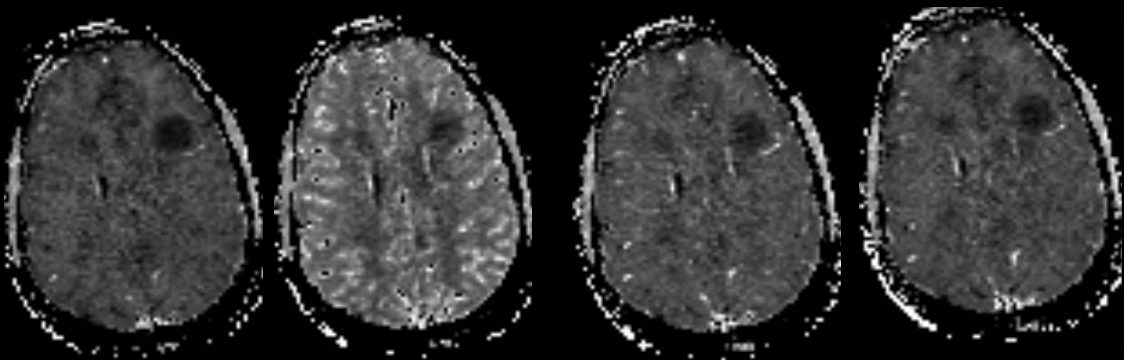
FLAIR

Relative blood flow map



Post-contrast  
T1-wt

R2\*-component



# Application: T<sub>2</sub> of CSF

Elements	Relaxivity r <sub>2</sub>	Concentration in control CSF	Extrapolated R <sub>2</sub> (s <sup>-1</sup> )	% of R <sub>2</sub> change in control CSF
Zn	-8x10 <sup>-3</sup> mM <sup>-1</sup> .s <sup>-1</sup>	3x10 <sup>-4</sup> mM	-2.4x10 <sup>-6</sup>	0%
Cu	0.6 mM <sup>-1</sup> .s <sup>-1</sup>	1.4x10 <sup>-4</sup> mM	7.8x10 <sup>-5</sup>	0.02%
Fe	3x2 mM <sup>-1</sup> .s <sup>-1</sup>	< 5.4x10 <sup>-4</sup> mM	< 1.7x10 <sup>-3</sup>	< 0.4%
Mn	124 mM <sup>-1</sup> .s <sup>-1</sup>	< 2x10 <sup>-5</sup> mM	< 2.5x10 <sup>-3</sup>	< 0.5%
Proteins (BSA)	1.3x10 <sup>-3</sup> mg/dL <sup>-1</sup> .s <sup>-1</sup>	47 mg/dL	6.1x10 <sup>-2</sup>	13%
Glucose	4x10 <sup>-3</sup> mg/dL <sup>-1</sup> .s <sup>-1</sup>	45-80 mg/dL <sup>a</sup>	0.2 – 0.3	39 – 69%

*a. Tichy et al., 1970*

Brain is fully immersed in CSF and changes in brain are often reflected in CSF (But can they be measured using MRI?):

- The low metal concentration doesn't impact CSF T<sub>2</sub> value
- Total protein is responsible for 13% of T<sub>2</sub> value
- Glucose is responsible for ~54% of T<sub>2</sub> value



# Tumor Detection by Nuclear Magnetic Resonance

*Abstract. Spin echo nuclear magnetic resonance measurements may be used as a method for discriminating between malignant tumors and normal tissue. Mea-*

Table 1. Spin-lattice ( $T_1$ ) and spin-spin ( $T_2$ ) relaxation times (in seconds) of normal tissues.

Rat No.	Weight (g)	Tissue							
		Rectus muscle		Liver		Stomach $T_1$	Small intestine $T_1$	Kidney $T_1$	Brain $T_1$
		$T_1$	$T_2$	$T_1$	$T_2$				
1	156	0.493	0.050	0.286	0.050	0.272	0.280	0.444	0.573
2	150	.548	.050	.322	.060	.214	.225	.503	.573
3	495	.541	.050	.241	.050	.260	.316	.423	.596
4	233	.576 (0.600)*	.070	.306 (0.287)*	.048	.247 (0.159)*	.316 (0.280)*	.541 (0.530)*	.620 (0.614)*
5	255	.531		.293		.360	.150	.489	.612
		<i>Mean and standard error</i>							
		0.538 ± 0.015	0.055 ± 0.005	0.293 ± 0.010	0.052 ± 0.003	0.270 ± 0.016	0.257 ± 0.030	0.480 ± 0.026	0.595 ± 0.007

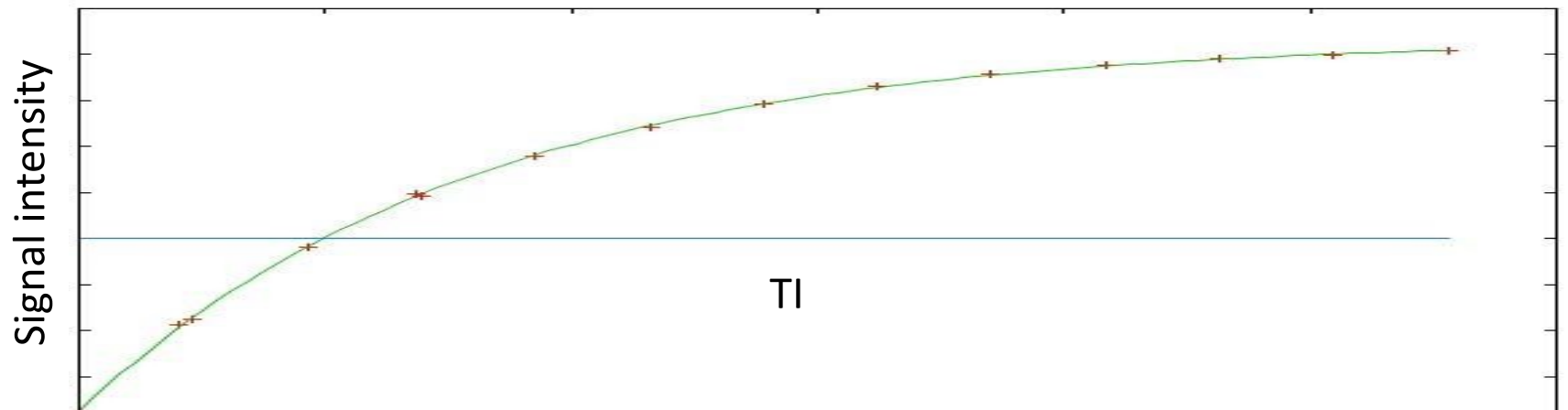
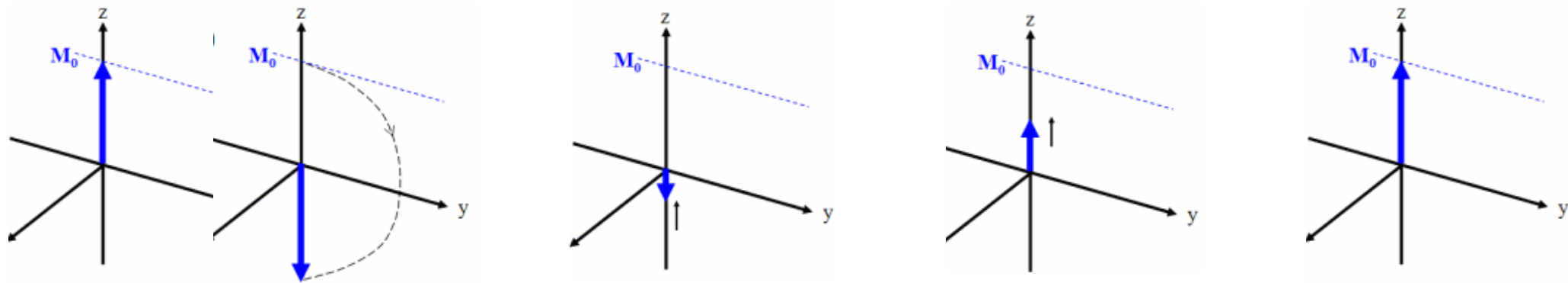
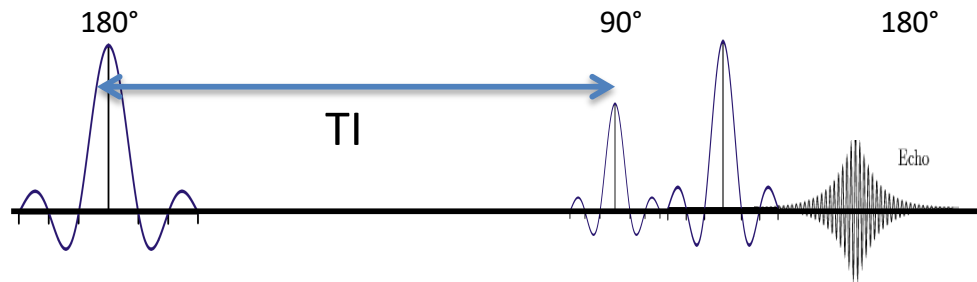
\* Spin-lattice relaxation time after the specimen stood overnight at room temperature.

Table 2. Spin-lattice ( $T_1$ ) and spin-spin ( $T_2$ ) relaxation times (in seconds) in tumors.

Rat No.	Weight (g)	$T_1$	$T_2$
<i>Walker sarcoma</i>			
6	156	0.700	0.100
7	150	.750	.100
8	495	.794 (0.794)*	.100
9	233	.688	
10	255	.750	
Mean and S.E.		0.736 ± 0.022	.100
P		< .01†	
<i>Novikoff hepatoma</i>			
11	155	0.798	0.120
12	160	.852	.120
13	231	.827	.115
Mean and S.E.		0.826 ± 0.013	0.118 ±
P		< .01†	0.002

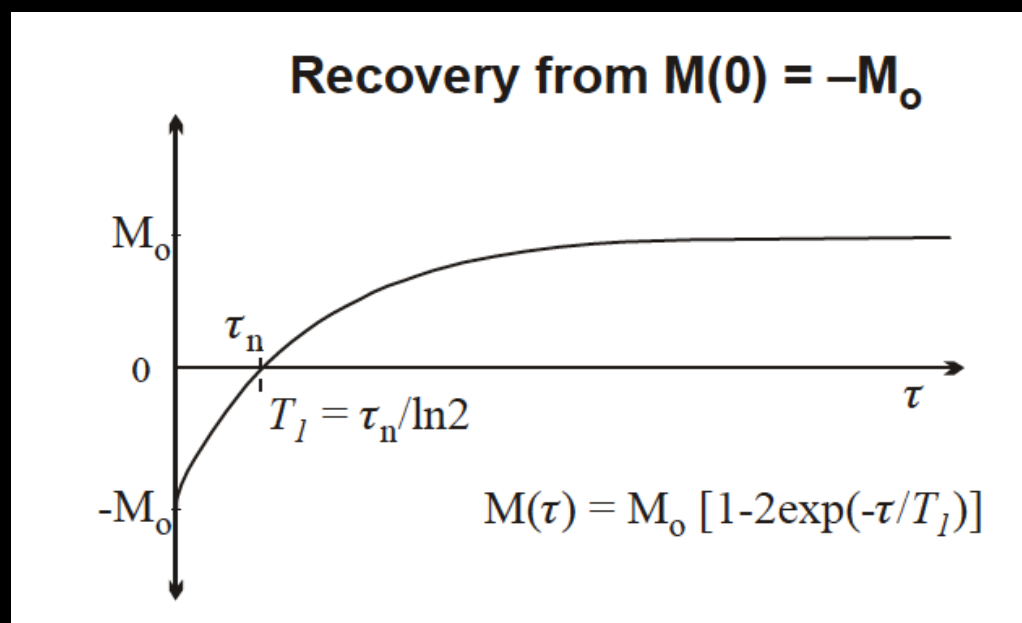
tion. The considerable increase in relaxation times for the hepatoma ( $T_1$ , 0.826 second;  $T_2$ , 0.118 second) relative to normal liver ( $T_1$ , 0.293 second;  $T_2$ , 0.050 second) suggests a significant decrease in the degree of ordering of intracellular water (2) in malignant tissue. In addition, it is apparent from the prolonged relaxation times of the two malignant tumors reported in Table 2 that NMR techniques would make it possible for one to detect the presence of metastatic infiltrates of the liver from either Walker sarcoma or Novikoff hepatoma.

# $T_1$ mapping Using Inversion Preparation





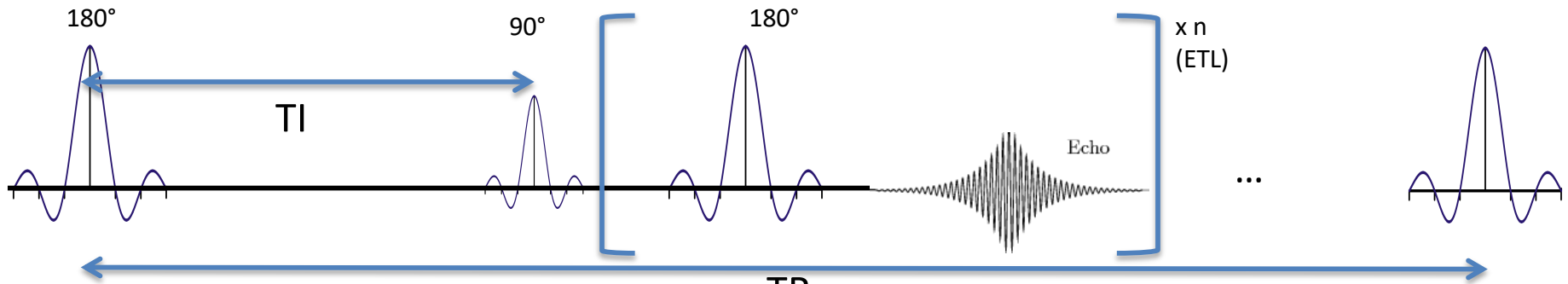
# Inversion Preparation



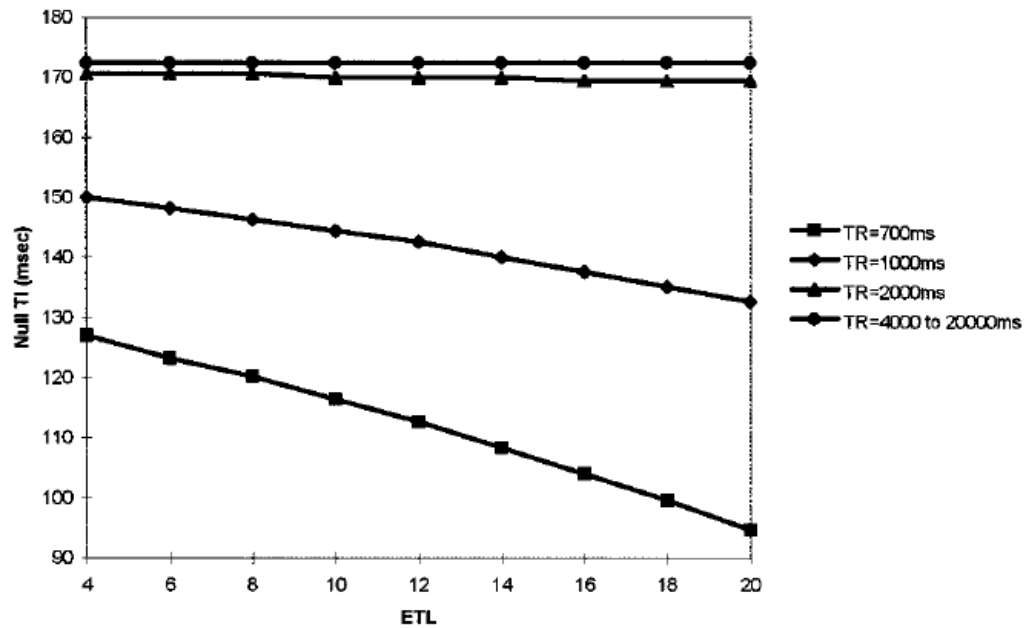
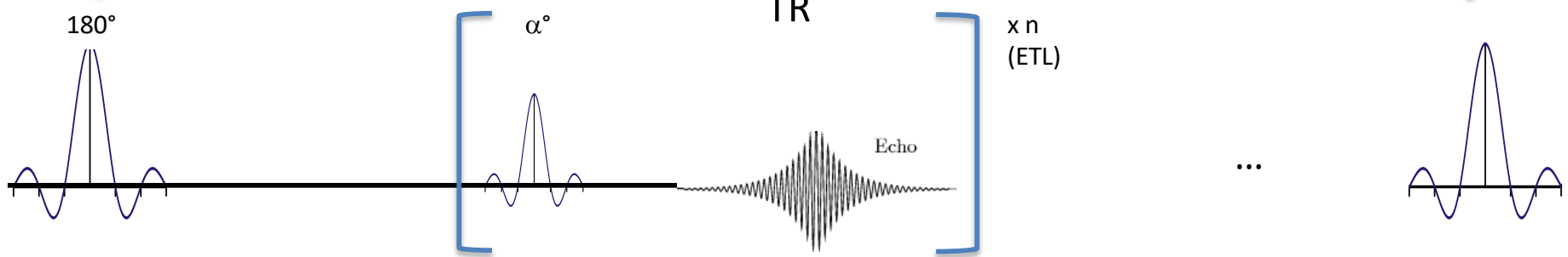
- Gold standard, but extremely long experiment
  - $TR \sim 5 \times T_1$ .
  - 5 to 6  $T_1$ s for reliable data fitting.
  - Not practical on awake human subjects.

# Speeding it up

IR-TSE



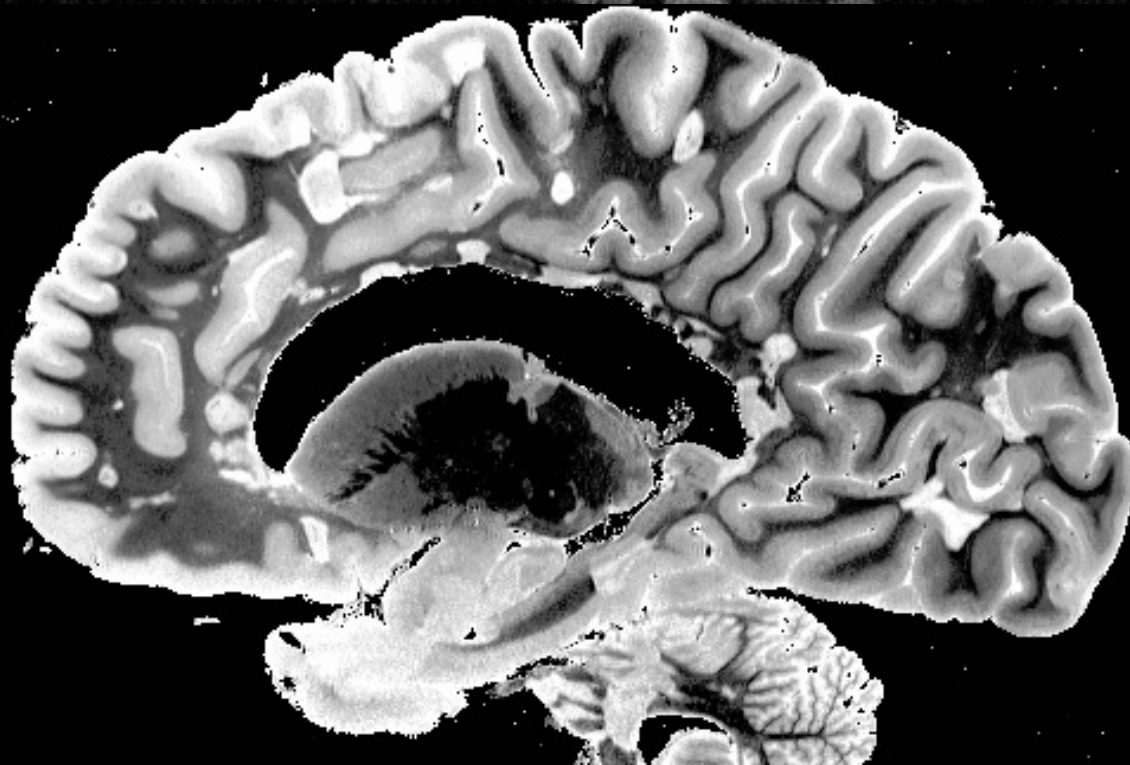
IR-TFE



$T_1$ -weighted  
TI=250 ms



$T_1$ -map



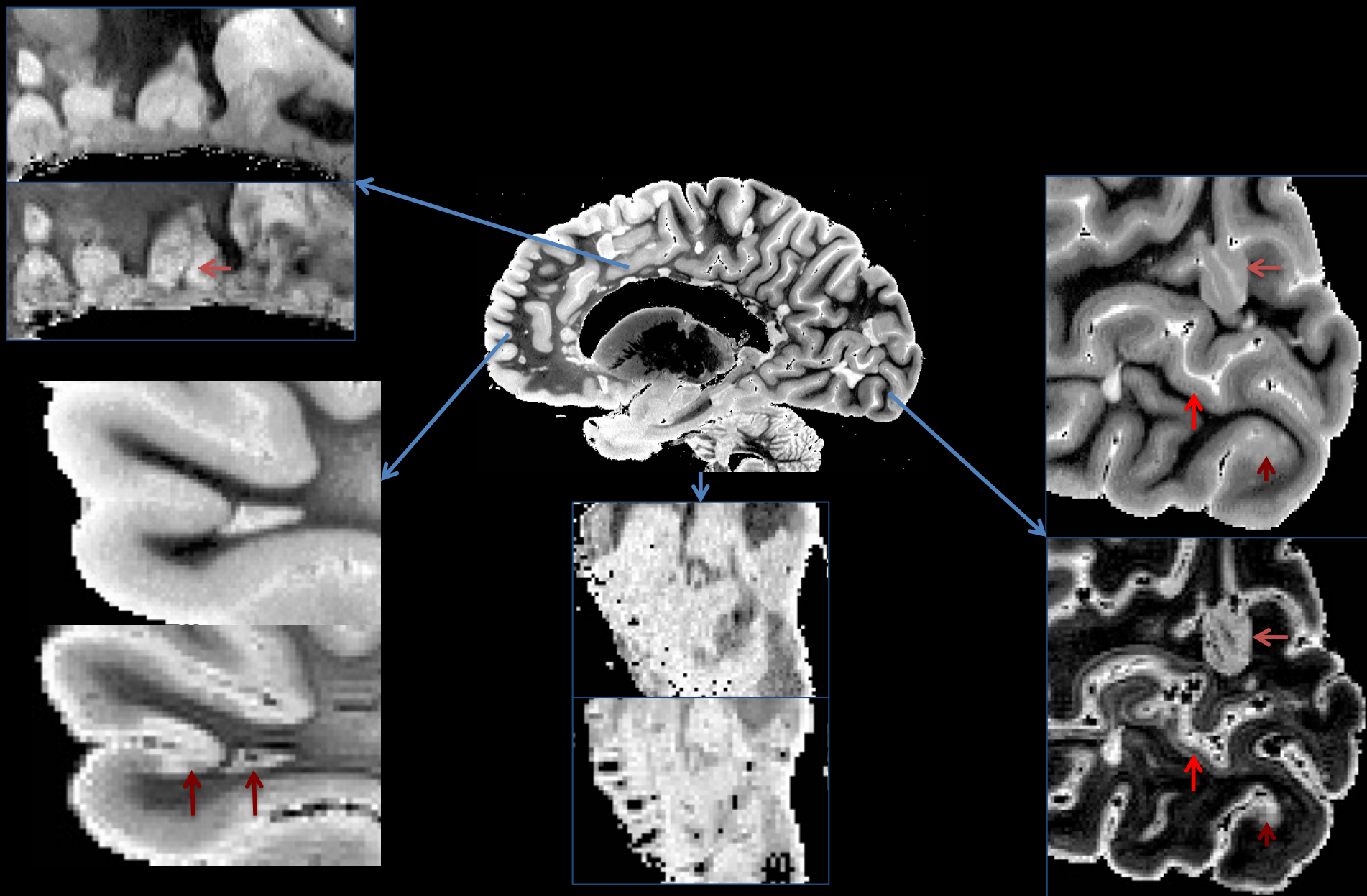
Pros

- Signal may actually mean something

Cons

- Fitting errors and related artifacts
- Slow

# Do we need both $qT_1$ and $qT_2$



# Rapid $T_1$ calculation

$$S = M_0 \frac{(1 - e^{-TR/T_1}) \sin \theta}{1 - e^{-TR/T_1} \cos \theta}$$

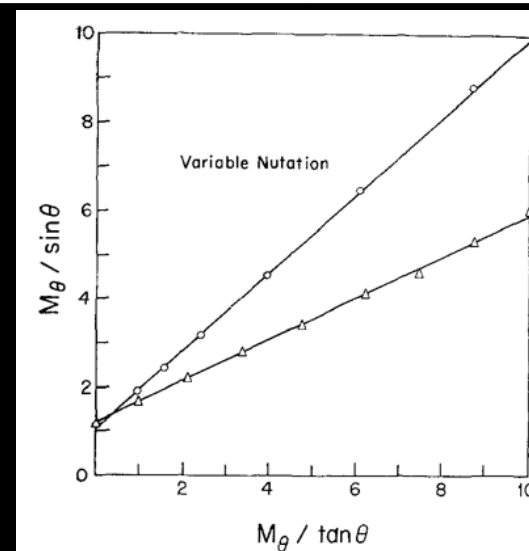
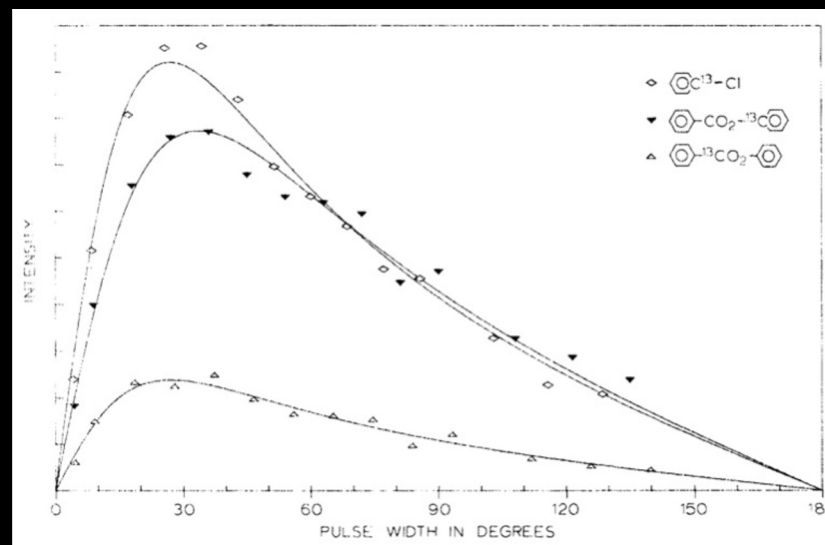
$\theta$  is the flip angle and S the signal at that flip

$$\frac{M_\theta}{\sin \theta} = e^{-T/T_1} \frac{M_\theta}{\tan \theta} + M_0(1 - e^{-T/T_1})$$

Of the form:  $Y = bX + a$

$$T_1 = -\frac{TR}{\ln b}$$

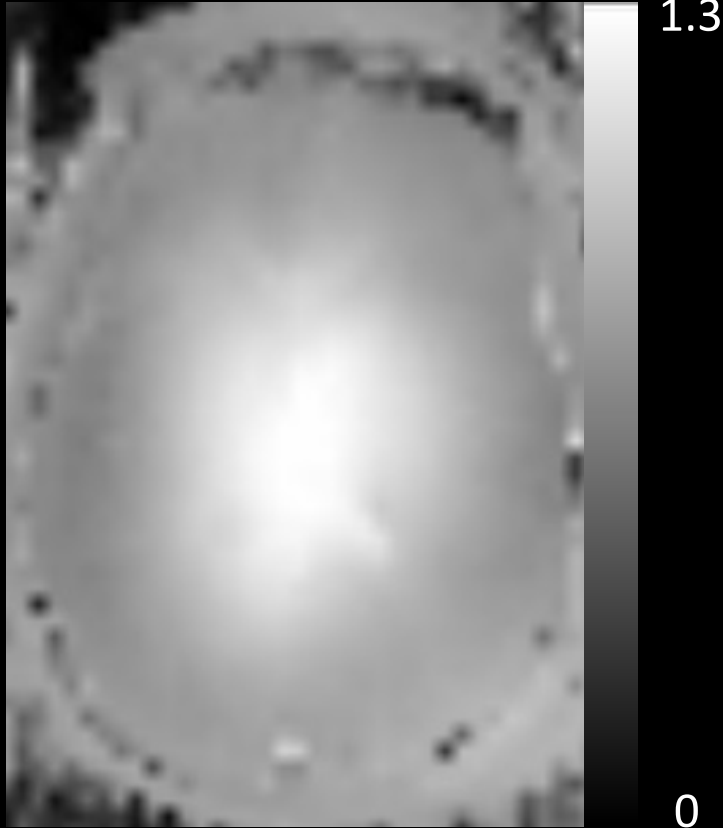
However, transmit coil profiles are not corrected automatically since FA needs to be specified.



Line fitting

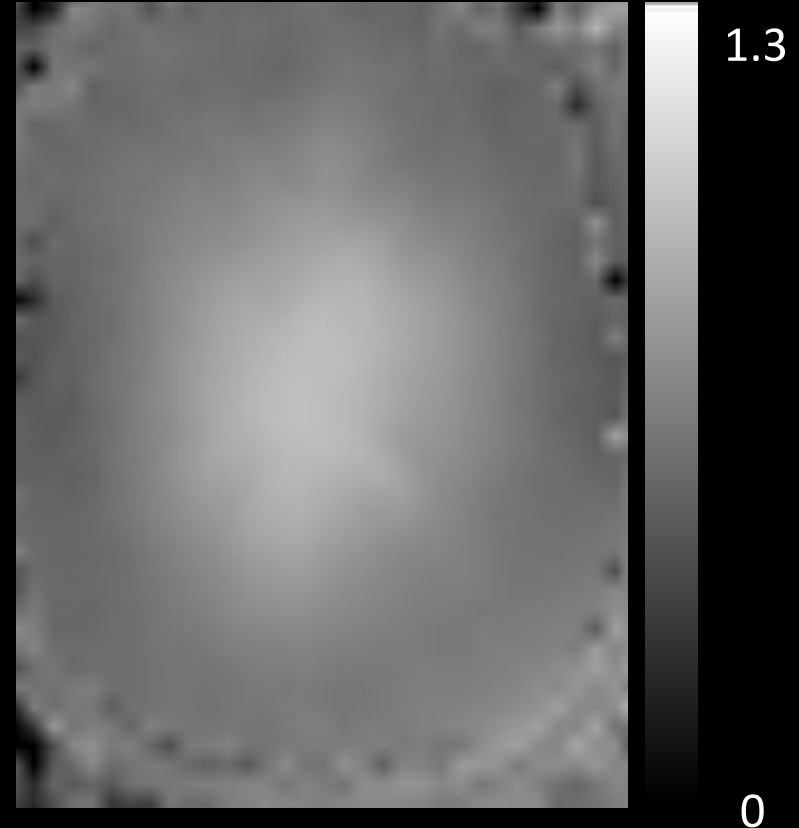
# Volumetric B1-map

Double-angle method



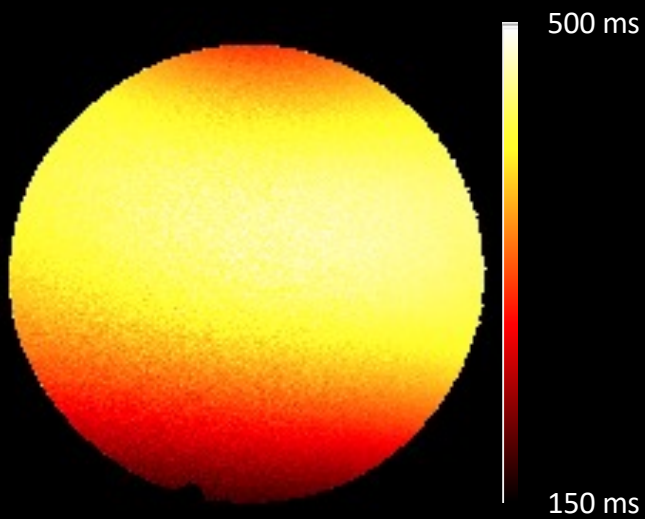
2D acquisition,  $\alpha$ - $2\alpha$  method,  
Tissue T1 dependent,  
Relative to applied voltage

Bloch-Siegert method

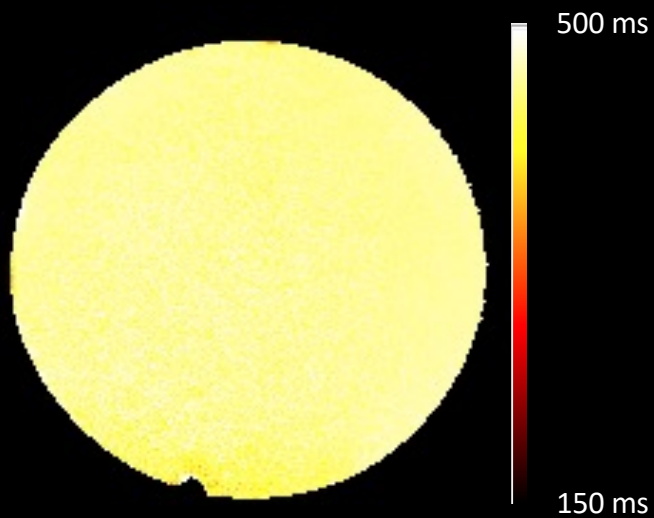


Volumetric acquisition,  
Tissue T1 independent,  
As a fraction of RF pulse angle

## Uncorrected $T_1$ map



+ B1 map

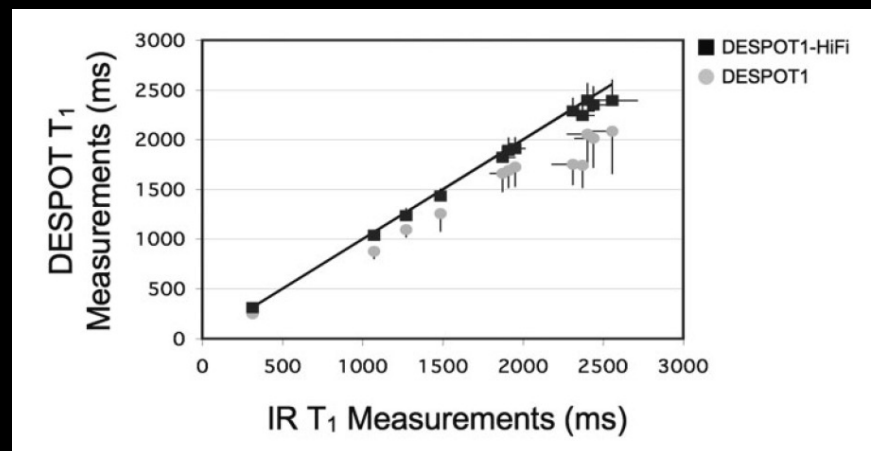
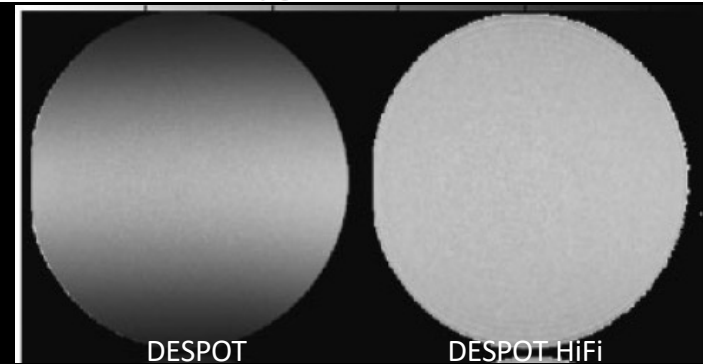


Corrected  $T_1$  map

## DESPOT1-HiFi Correction

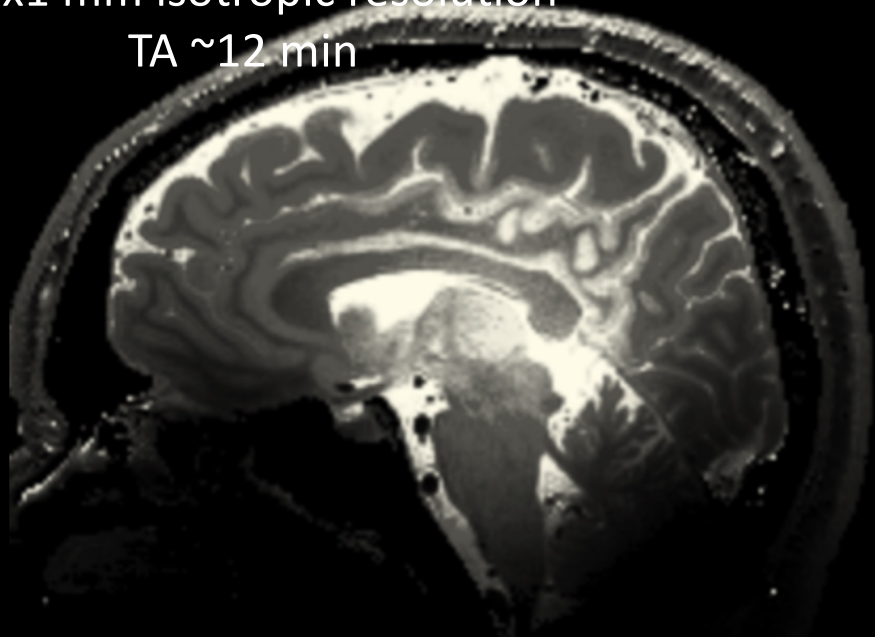
From the combined multiangle DESPOT1 and IR-SPGR data, a unique solution for  $\kappa$ ,  $T_1$ , and  $\rho$  can be found through the least squares minimization of the combined DESPOT1 and IR-SPGR data to Eqs. [1] and [6] for the three parameters, i.e., minimization of the function:

$$f(\rho, T_1, \kappa) = \sum_{i=1}^{i=NTI} [\rho \sin \kappa \alpha_P (1 - 2e^{-T_1/T_1 + e^{-T_1/T_1}}) - S_{IR-SPGR}(i)]^2 + \sum_{i=1}^{i=N\alpha} \left[ \frac{\rho(1-E_1) \sin \kappa \alpha_{P,i}}{1-E_1 \cos \kappa \alpha_{P,i}} - S_{SPGR}(i) \right]^2 \quad (7)$$

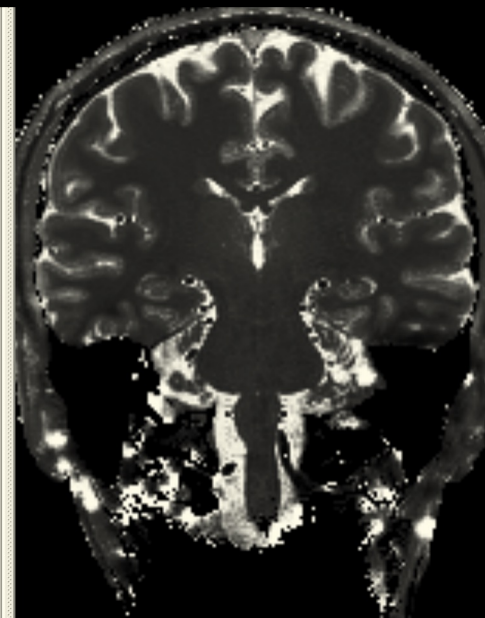
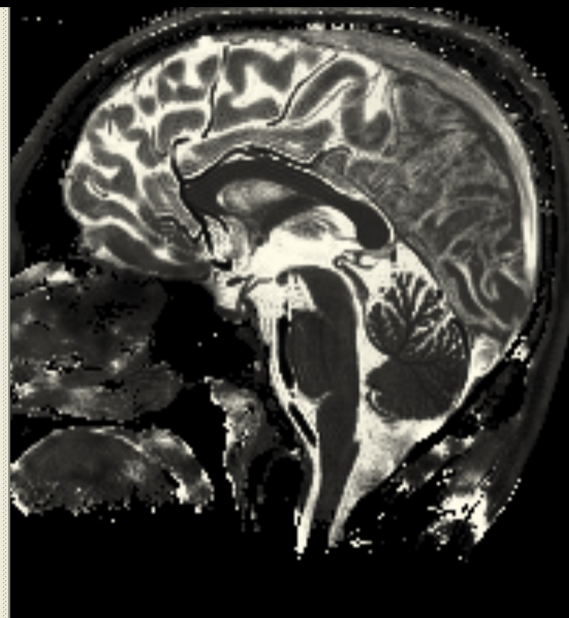
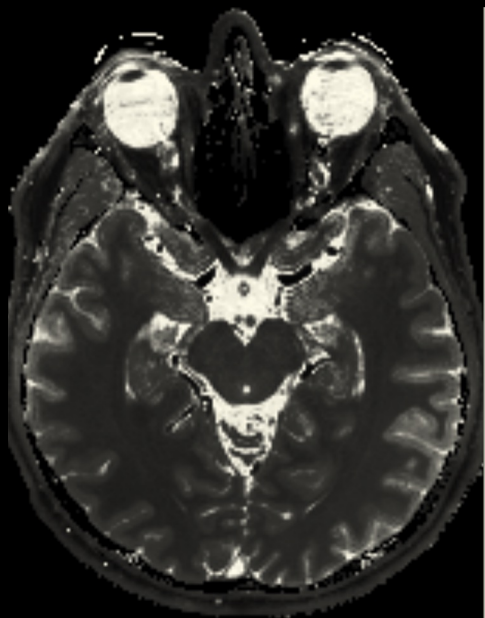
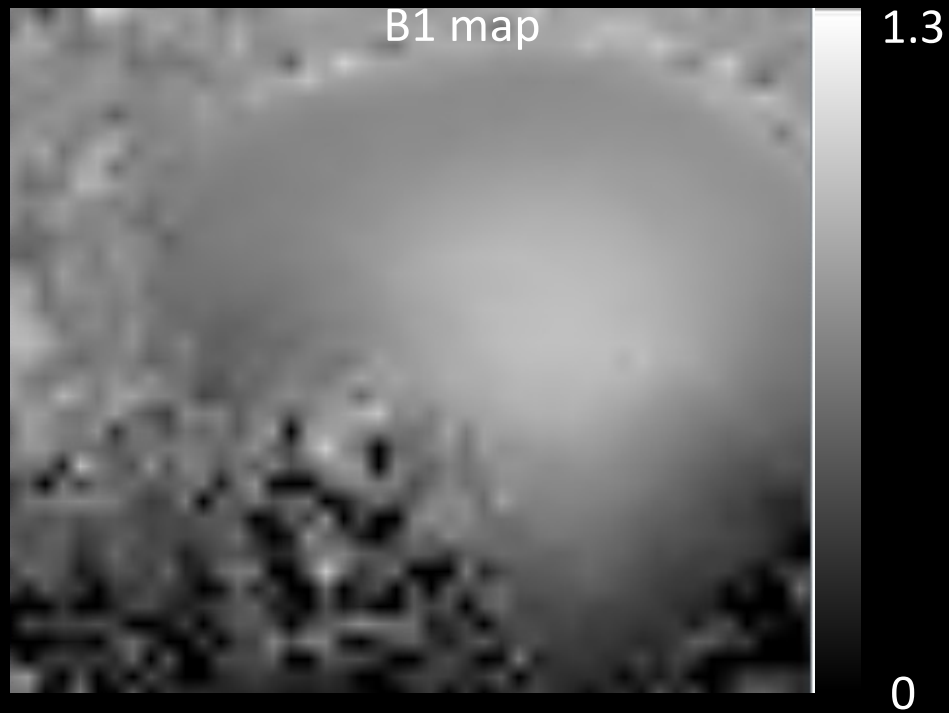




Uncorrected  $T_1$  map  
1x1x1 mm isotropic resolution  
TA ~12 min



B1 map

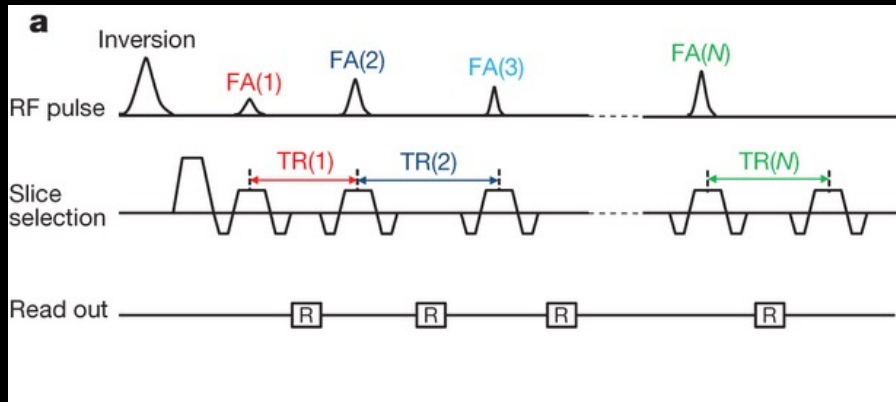


5s

B1 corrected  
 $T_1$  map  
TA ~16 min

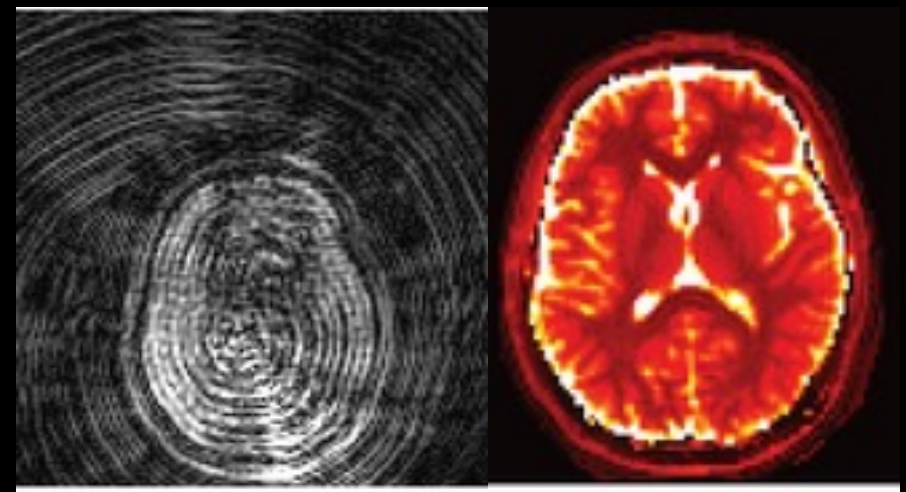
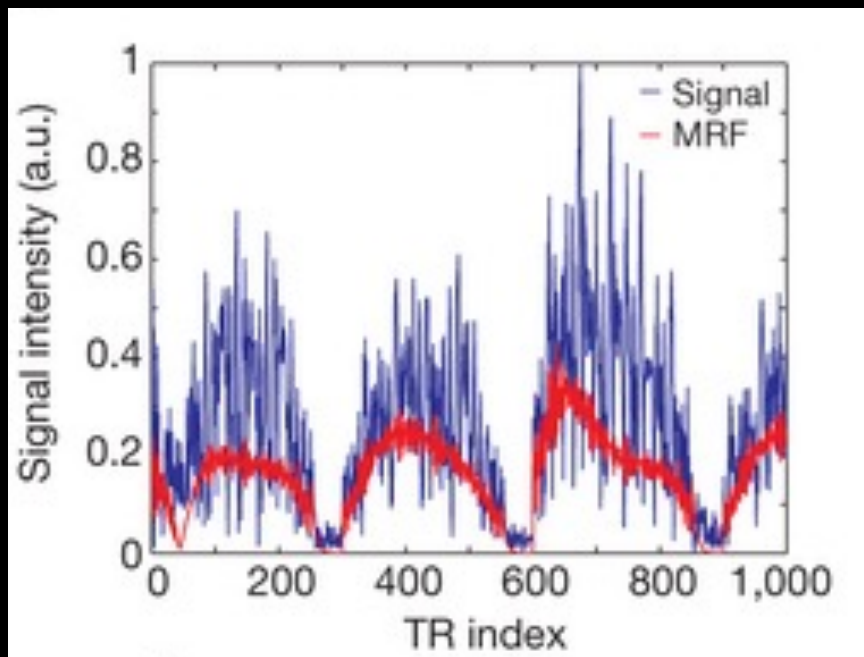
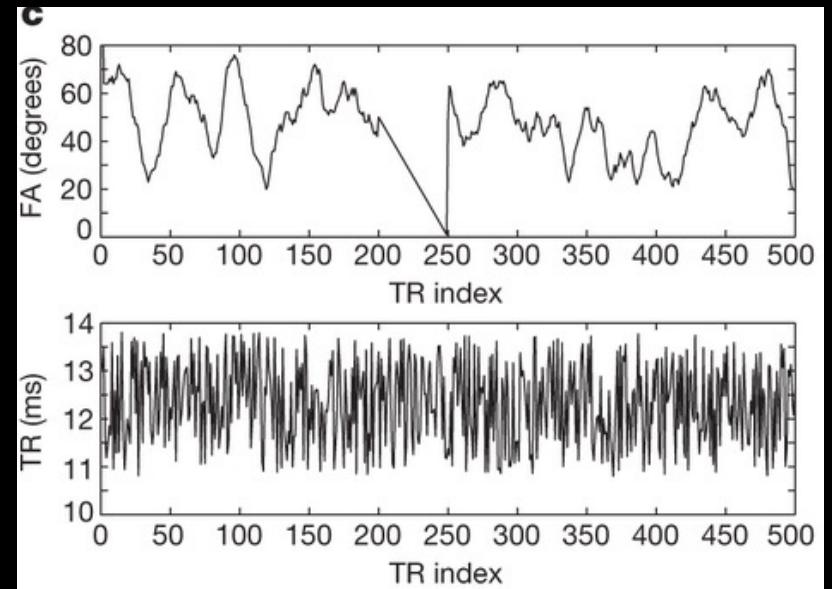
0

# MR Fingerprinting

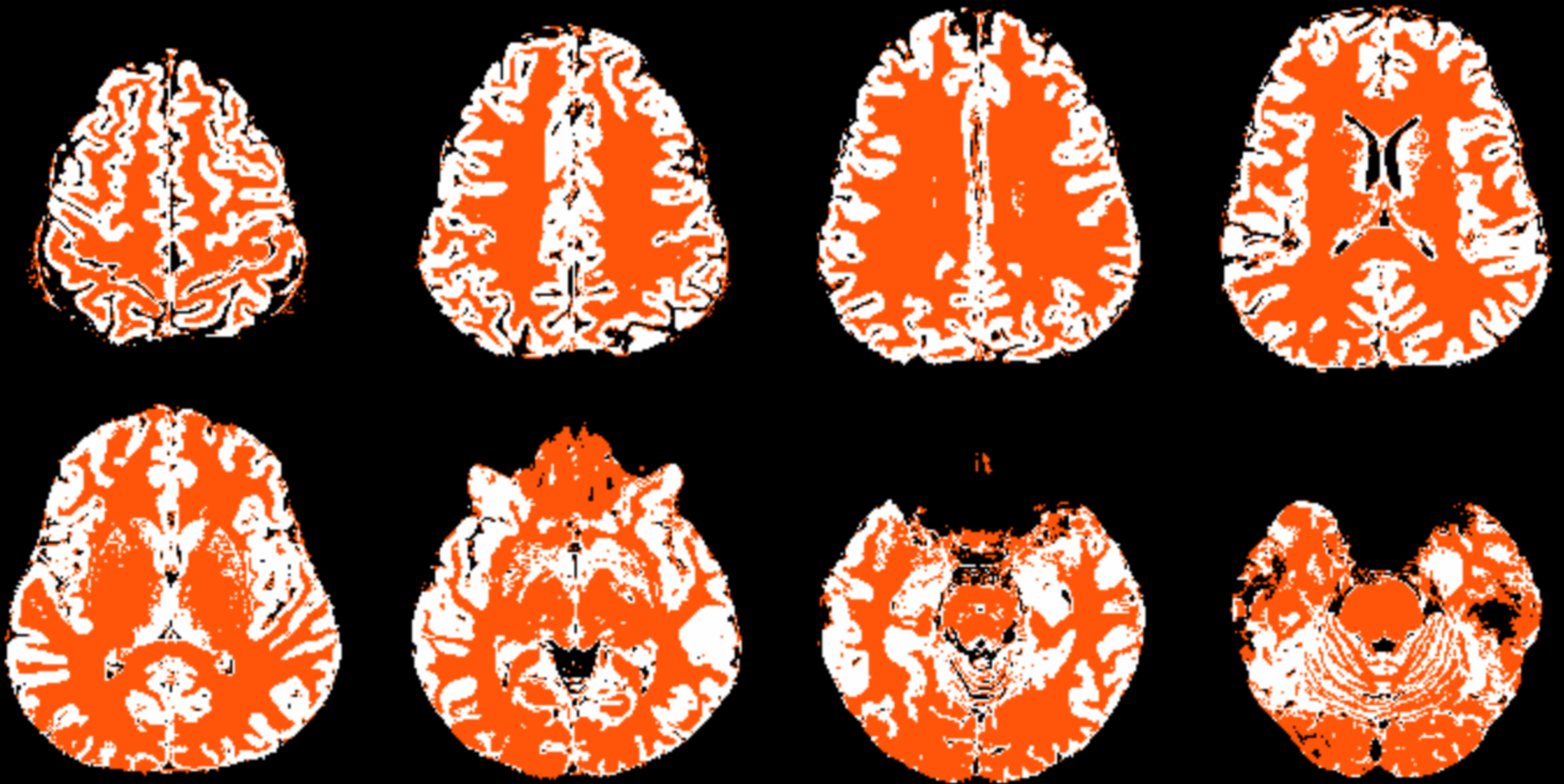


$$M_0[\sqrt{\sin(\text{FA}) * E_2(1-E_1)}] / [1 - (E_1 - E_2) * \cos(\text{FA}) - E_1 * E_2]$$

Where  $E_1 = \exp(-T_R/T_1)$  and  $E_2 = \exp(-T_R/T_2)$



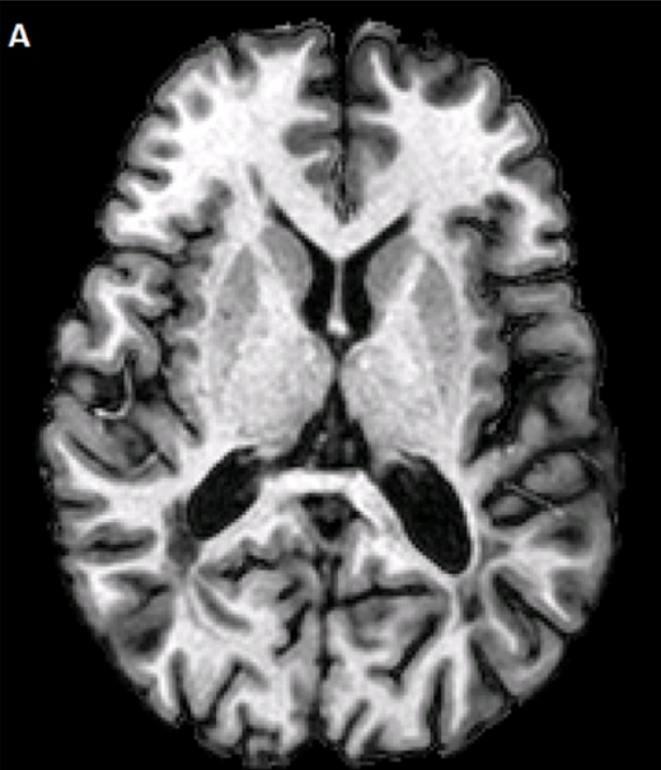
# Applications: image segmentation



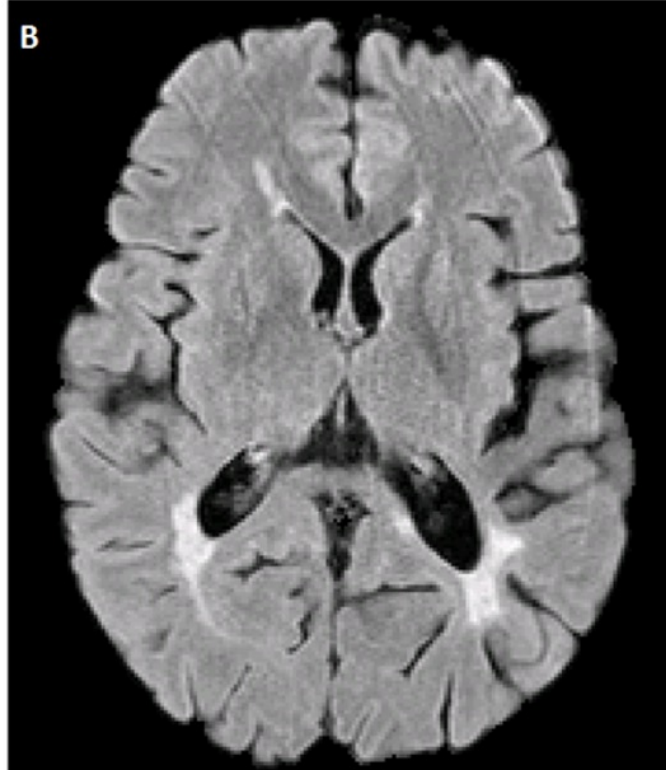
40 y.o. M



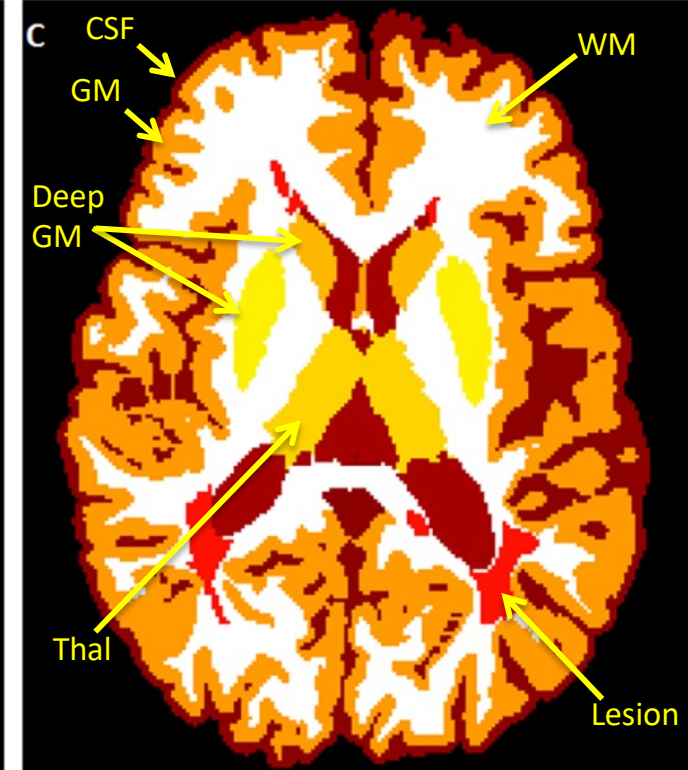
# Volumetrics - LesionTOADS



MPRAGE



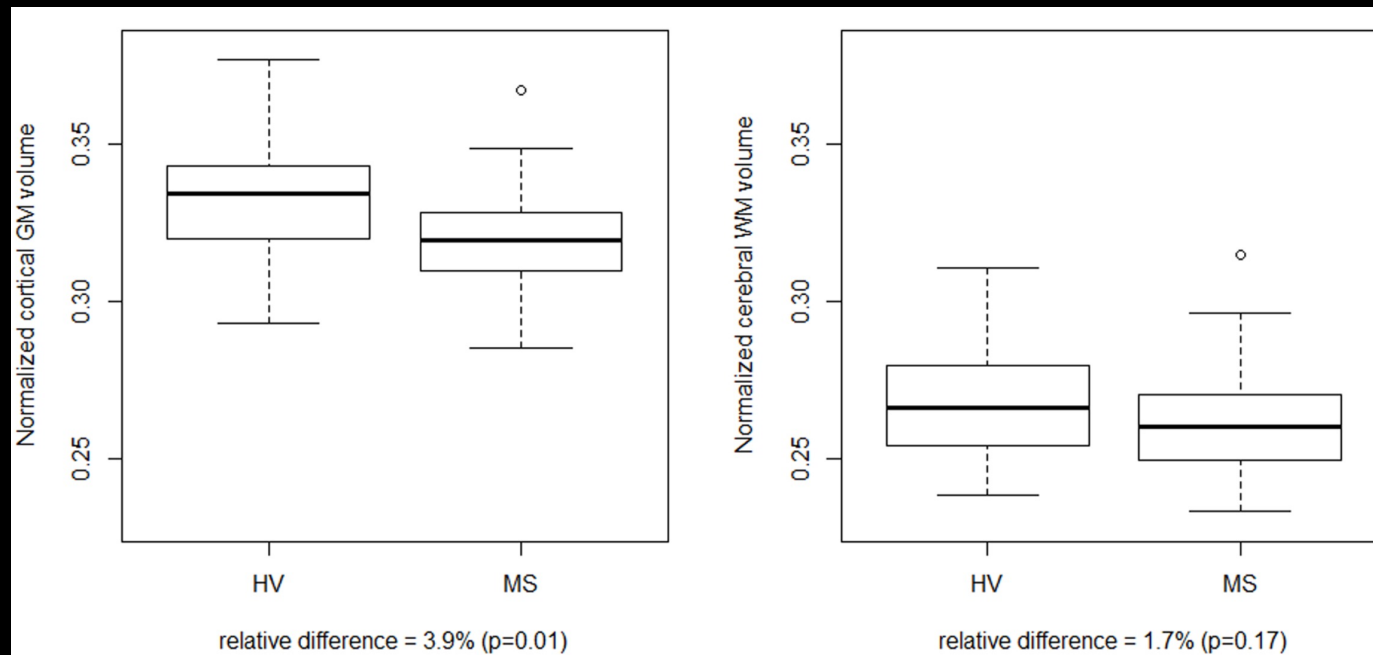
2D FLAIR



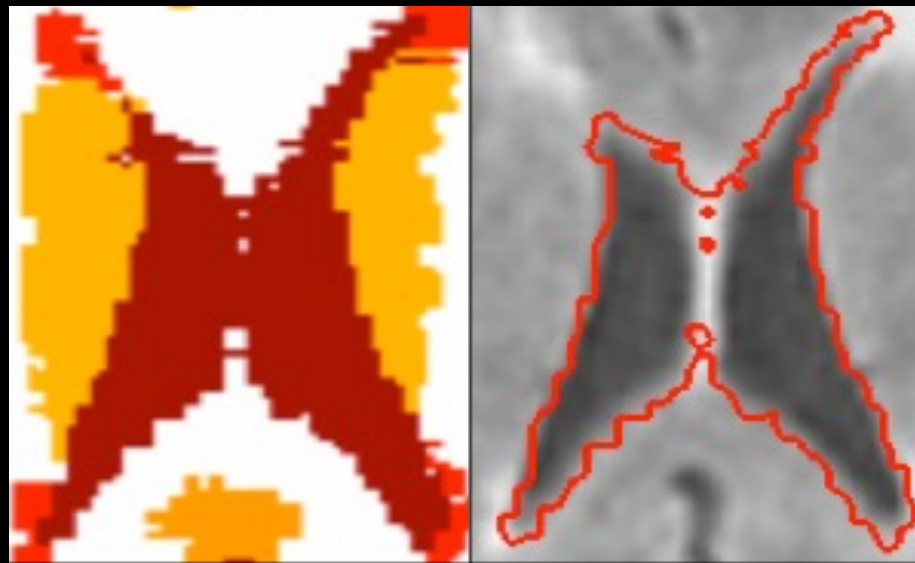
Tissue classification

Freesurfer,  
AFNI,  
FSL,  
Slicer...

# Estimating Brain Atrophy - LesionTOADS



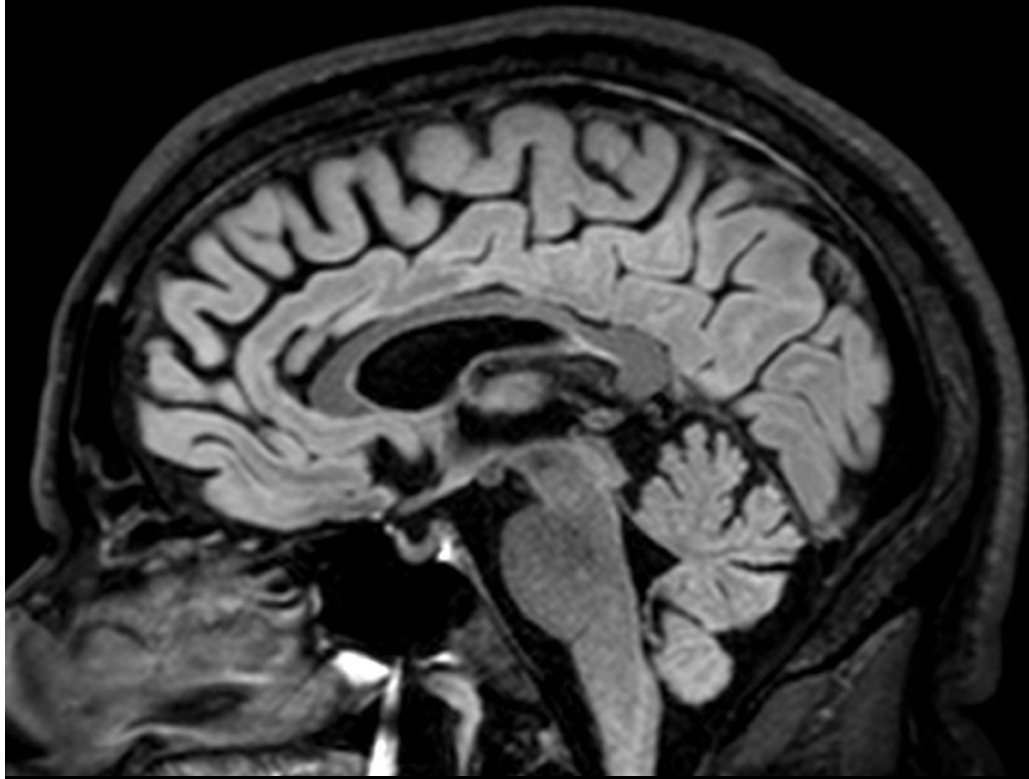
# Tissue Segmentation Errors



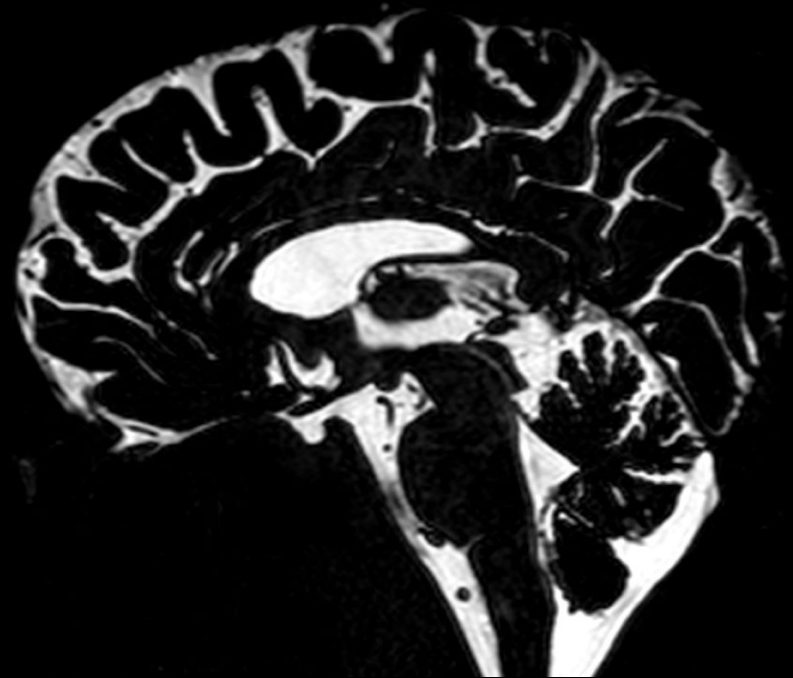
Segmentation

FLAIR

# Global Cerebral Atrophy – Brain Free Water Imaging



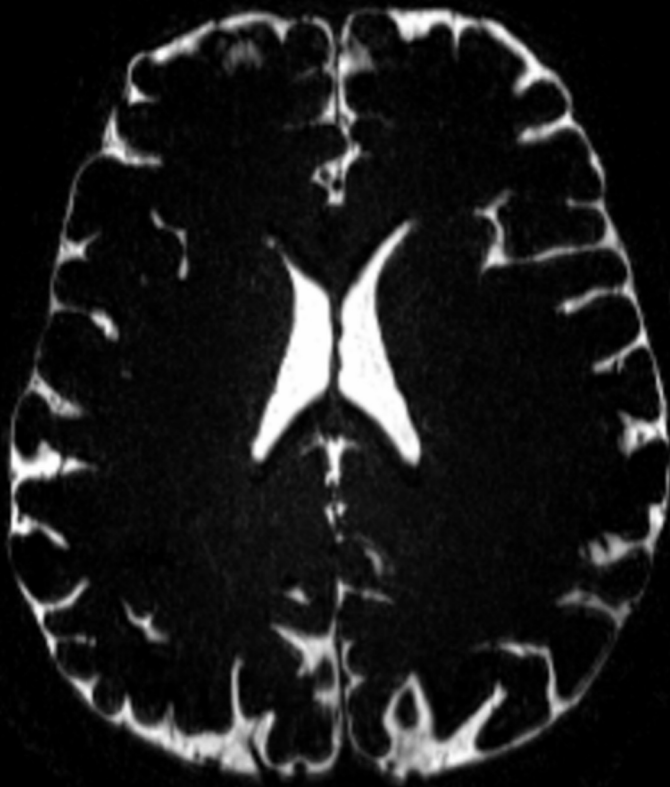
FLAIR



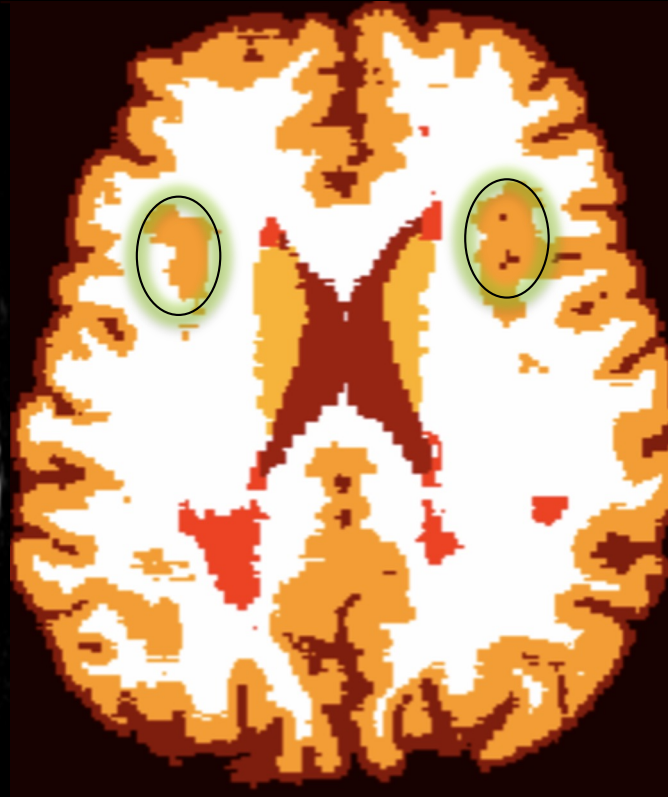
Brain Free-Water Imaging  
The only thing that is bright is CSF



# Comparison: BFWI vs. LesionTOADS



Original



LesionTOADS - processed

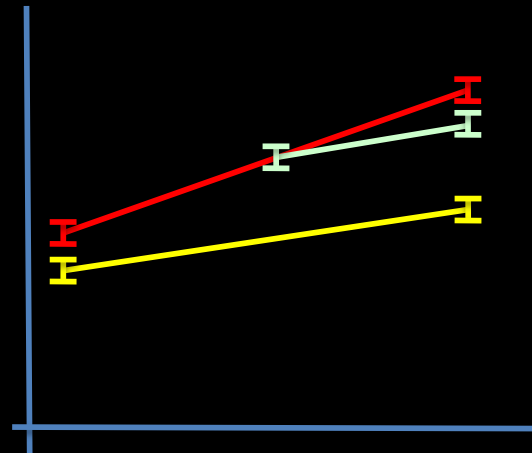


BFWI - processed

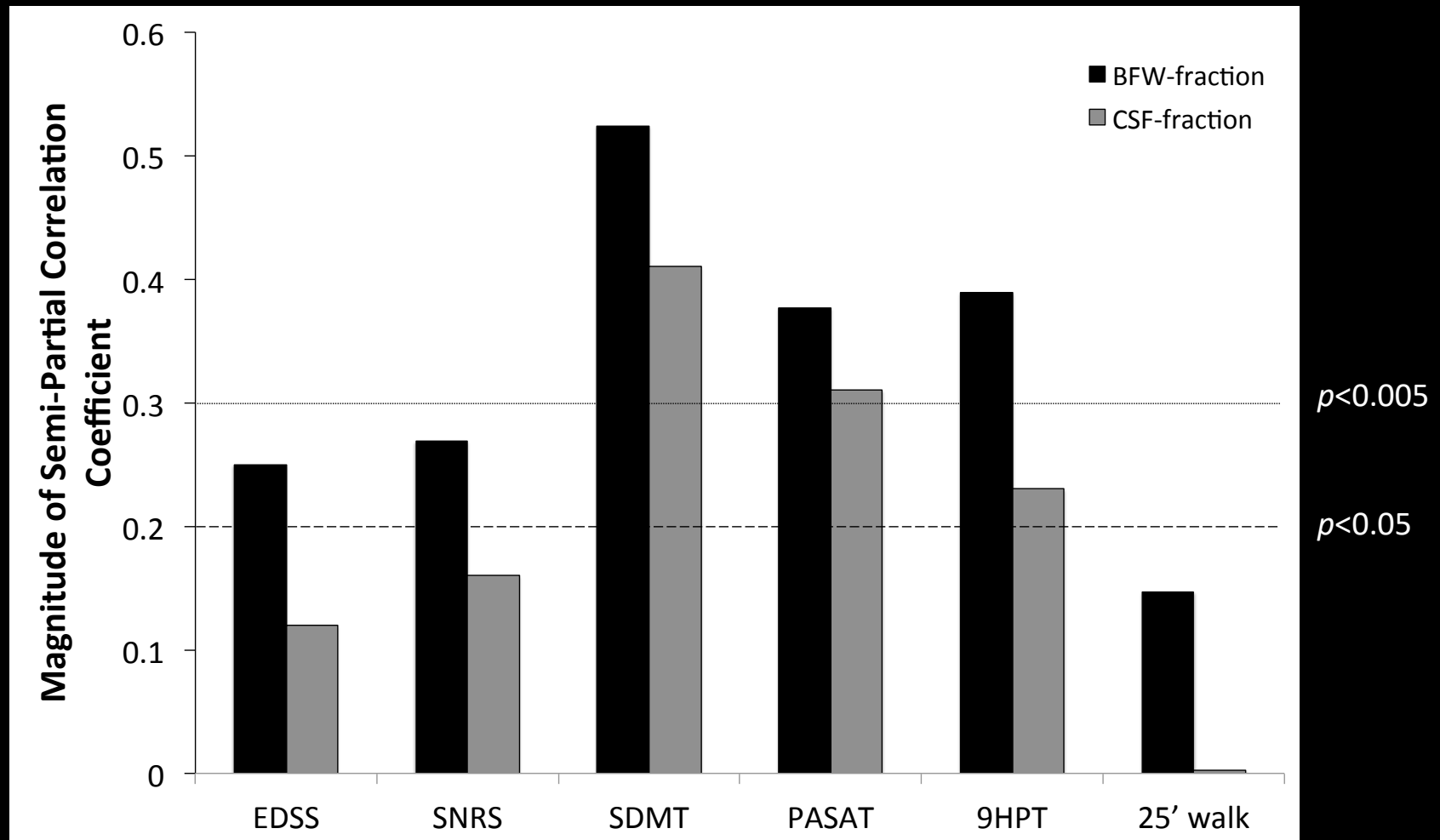
# Reproducibility

Mean COVs in 12 subjects

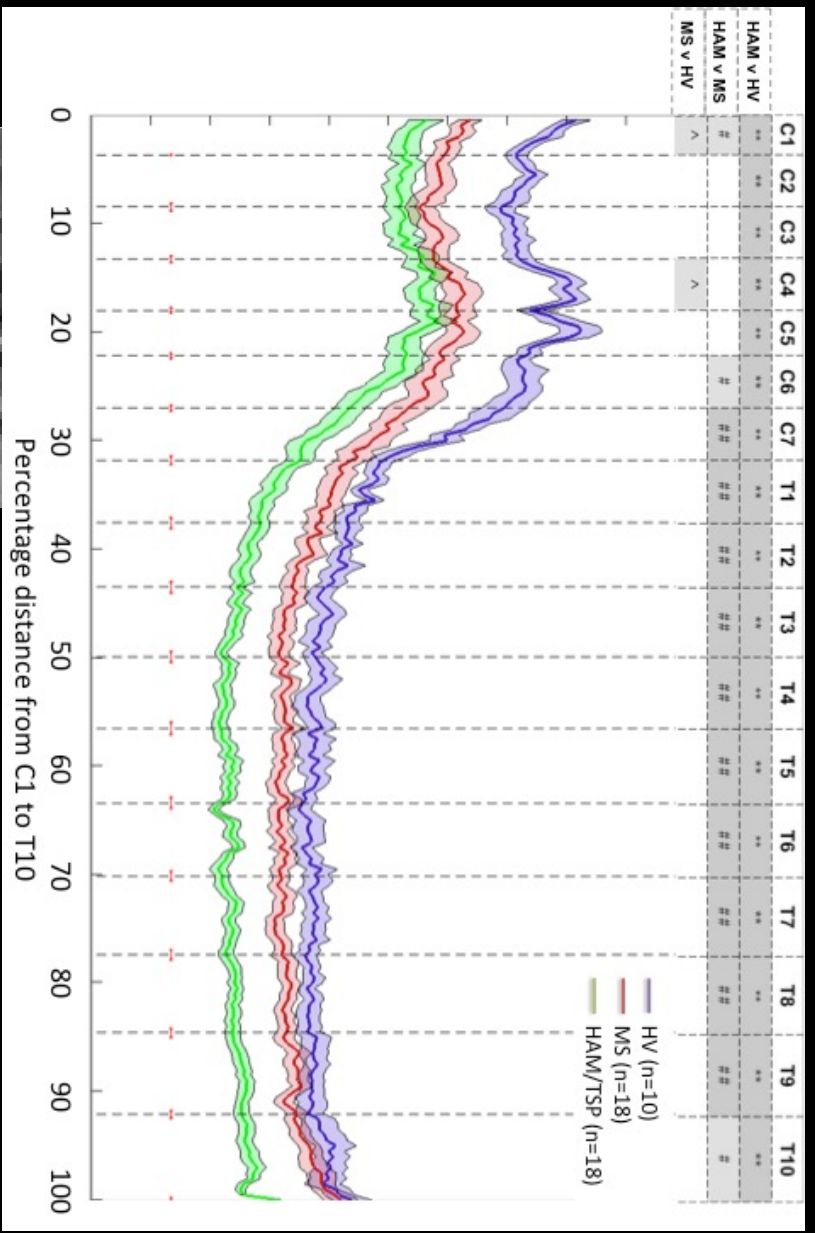
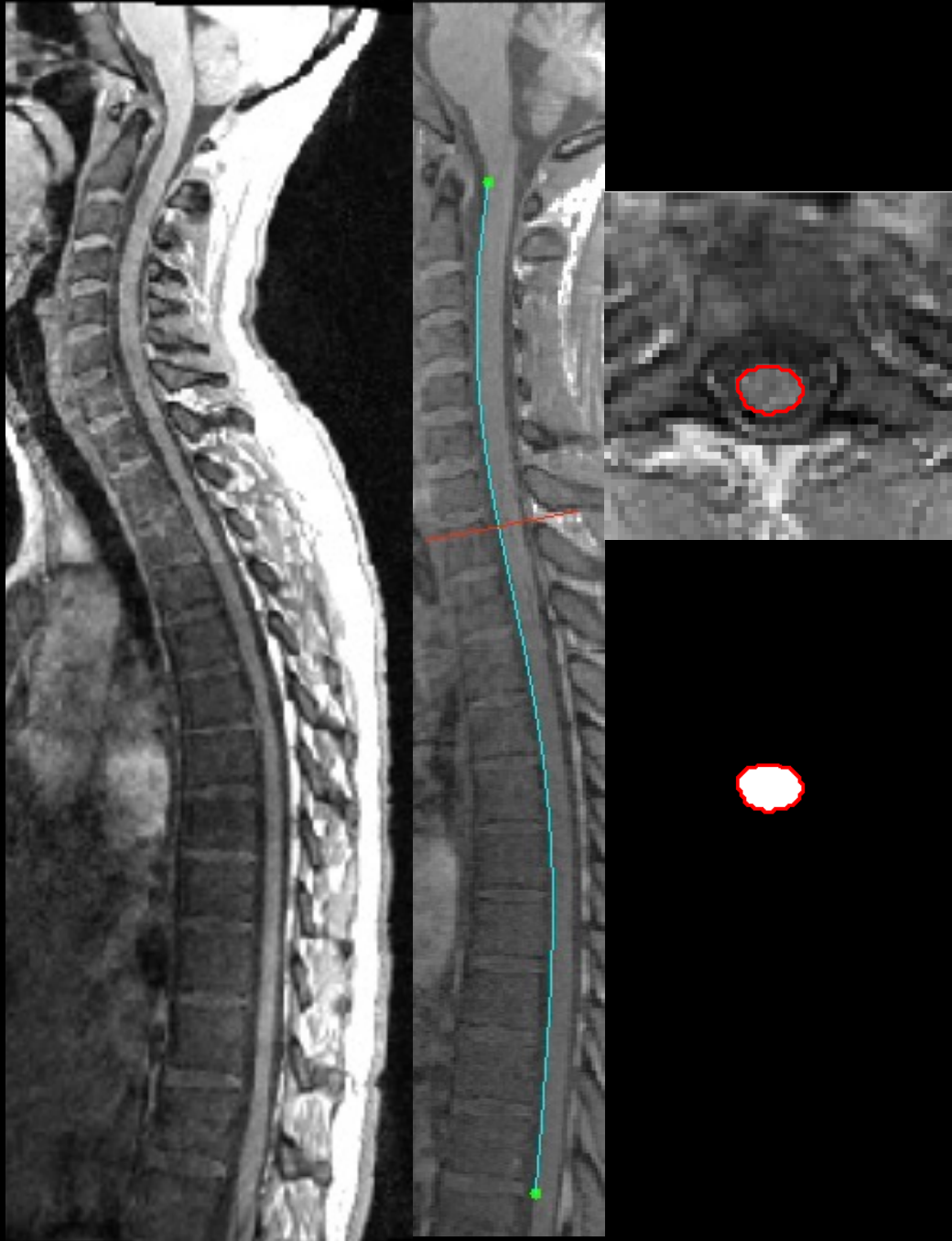
	CSF volume	Brain volume
Brain free water	1.5%	~0.3%
LesionTOADS	0.6%	
SIENAX		2.3%

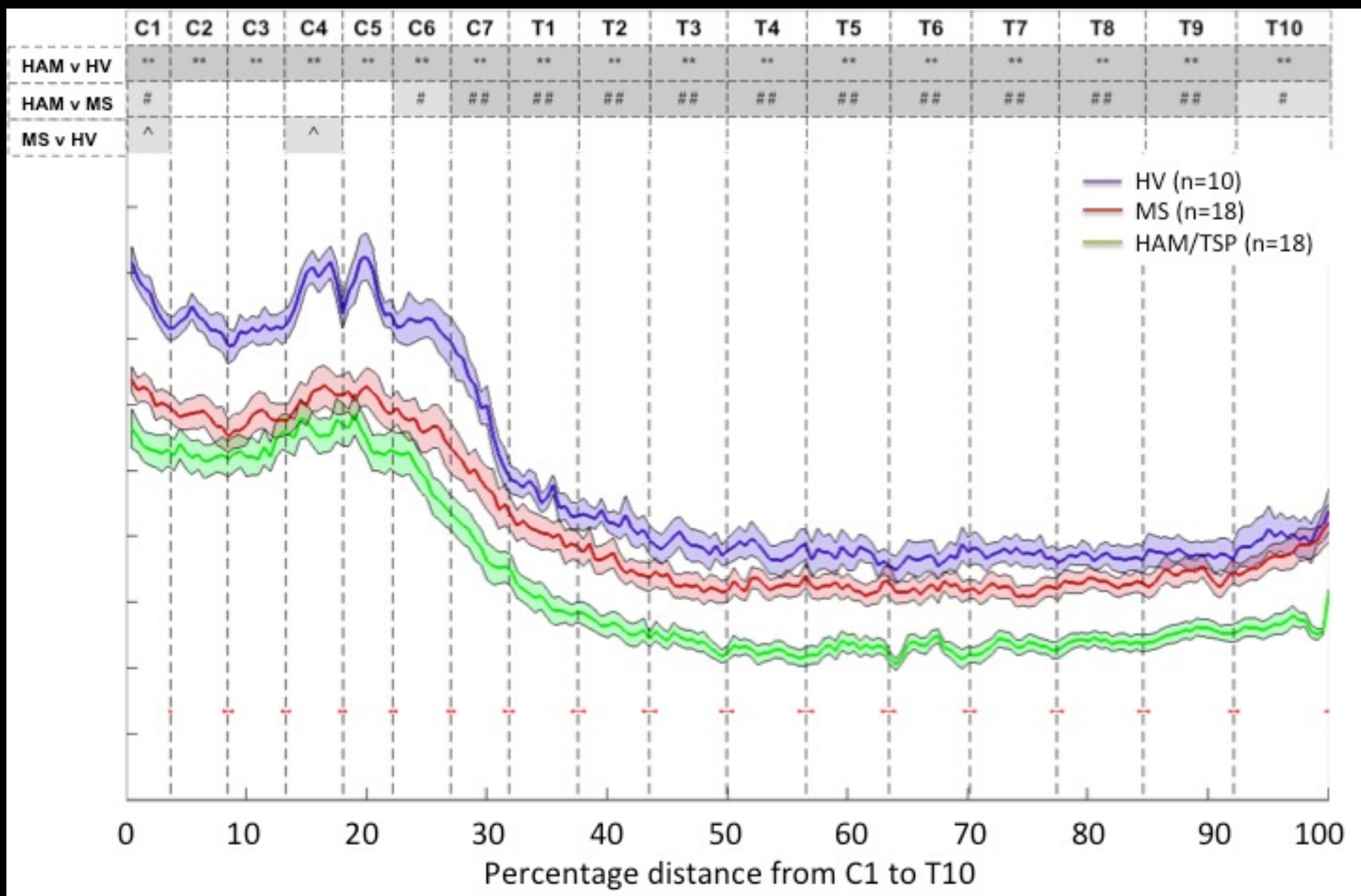


# What does it mean clinically?



Adjusted for age and gender





# Conclusion

- Several qMRI techniques have shown sensitivity to biological and disease processes
  - Correction for various scanner effects and bias fields are available, and have to be used.
  - Can be acquired in clinically acceptable time at high resolution (~1 mm isotropic).
  - Careful experimental design, avoid over-interpretation.
- However, the specificity remains an issue
  - qMRI value could change from an unrelated process.

# Source of Errors and Variability

- User induced
  - Sequence and protocol selection (filters, distortion correction, resolution/ETL...)
  - Analysis methods, assumptions, and models...
- Manufacturer dependent
  - Equivalent sequences may still be slightly different (RF pulse, gradient slopes, coil combination, acceleration)
  - Hardware (e.g. OEM 7T head coil, gradient distortions, eddy current)



# Future: Understanding the Origins

Solution in a tube:

$$\frac{1}{T_1} = \frac{6}{20} \frac{\hbar^2 \gamma^4}{b^6} \left[ \frac{\tau_c}{1 + \omega^2 \tau_c^2} + \frac{4\tau_c}{1 + 4\omega^2 \tau_c^2} \right],$$

$$\frac{1}{T_2} = \frac{3}{20} \frac{\hbar^2 \gamma^4}{b^6} \left[ 3\tau_c + \frac{5\tau_c}{1 + \omega^2 \tau_c^2} + \frac{2\tau_c}{1 + 4\omega^2 \tau_c^2} \right].$$

*In vivo*: “Presence of locally disordered macromolecular environments”  
- compartments with solids, couplings, and different exchange regimes...

**Extremely Heterogeneous Environment**

**Thank you.**